

RUNAWAY IN THE  
LANDSCAPE

STRINGS OF  
MADRID JUNE 2007

MELANIE BECKER

# RUNAWAY IN THE LANDSCAPE

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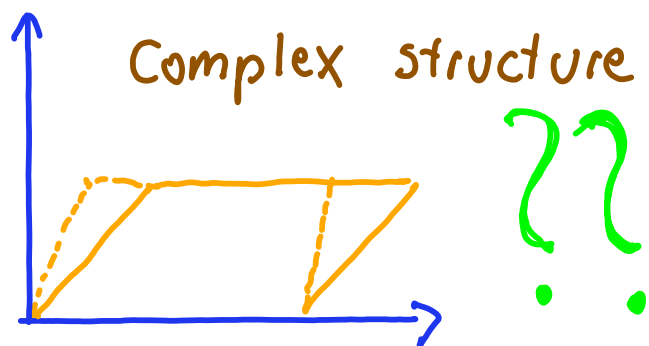
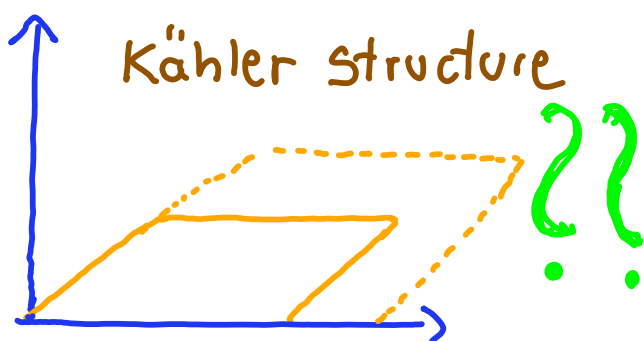
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## CALABI-YAU MANIFOLDS

MANY ASPECTS OF THE 4D THEORY CAN  
BE TRACED BACK TO THE TOPOLOGY OF  
THE INTERNAL MANIFOLD

MODULI FIELDS  $\Rightarrow$  FLUX COMPACTIFICATIONS!

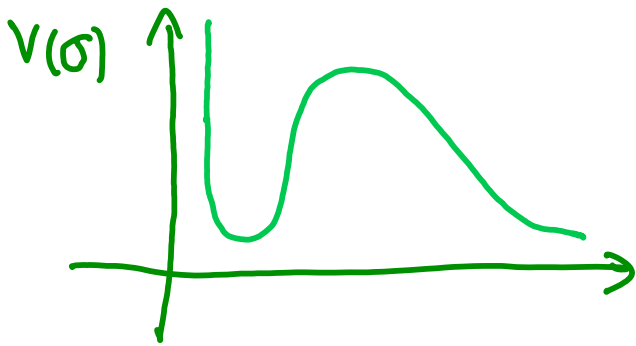


# SCENARIOS

BEFORE OUR PAPER THERE WERE (ROUGHLY SPEAKING) 2 SCENARIOS:

## ① KKLT LIKE SCENARIOS

Kachru  
Kalosh  
Linde + Trivedi



- x fluxes (plx. st.)
- x np effects (Kähler)
- x  $\overline{D3}$ 'S ( $\Lambda > 0$ )

## ② STABILIZATION WITH ONLY FLUXES (GEOMETRIC)

MODULI STABILIZATION AT THE CLASSICAL LEVEL WITH FLUXES ONLY IN SUGRA APPROX.

MASSIVE IIA ON ORIENTIFOLD

$$AdS_4 \times T^6 / \mathbb{Z}_3 \times \mathbb{Z}_3$$

De Wolfe  
Siryavets  
Kachru + Taylor

PARAMETRIC CONTROL: SMALL PARAMETER  $\epsilon$

$$\frac{1}{N} < \epsilon$$

FLUX NUMBER  $N \rightarrow \infty$

- \* GEOMETRIC DESCRIPTION
- \* IIA MODEL IS CONSTRAINT TO  $\Lambda < 0$
- \* MASSES OF MODULI TOO SMALL

**GOAL:** CONSTRUCT A SIMPLE TYPE IIB MODEL IN WHICH MODULI STABILIZATION CAN BE ACHIEVED BEYOND THE SUPERGRA APPROXIMATION IN TERMS OF FLUXES ONLY

- ① MODULI STABILIZATION IN A NON-GEOMETRIC MODEL (MIGHT BE THE ONLY WAY TO STABILIZE SUSIC VACUA
- ② SUSIC VACUA OF ADS/MINKOWSKI TYPE WITH ALL MODULI STABILIZED

# A NONGEOMETRIC TYPE IIB MODEL

IN THE TYPE IIB THEORY THERE IS A  
SUPERPOTENTIAL FOR COMPLEX STRUCTURE  
MODULI

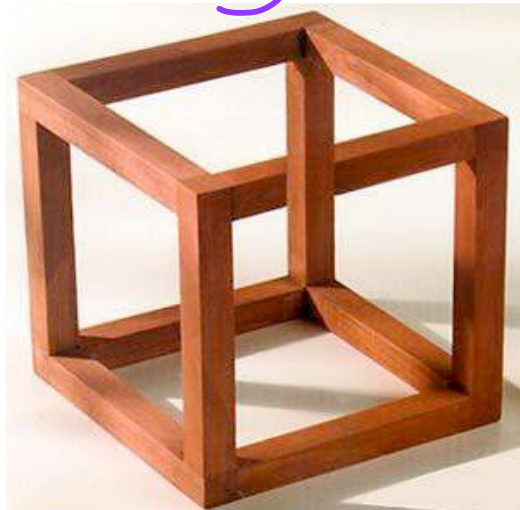
Gukov, Vafa + Witten

$$W = \int_{H_6} \Theta \wedge \Omega \quad \Theta = H_{RR} - \tau H_{NS}$$

TAKE A MODEL WITH  $h_{2,1} = 84$   $h_{1,1} = 0$   
cplx. str. Kähler str.

NO RADIAL MODULUS  $\Rightarrow$  NON-GEOMETRIC  $\blacktriangledown$   
NOT A CALABI-YAU (WHICH HAVE A SIZE)  $\bullet$

$\mathcal{N} = 2$  SCFT  $\Rightarrow$  LANDAU-GINZBURG MODEL  
with  $c = 9$  (ORIENTIFOLD)



Non-geometric  
cube 

GOAL : CONSTRUCT THIS MODEL

## CONSTRAINTS ON THE MODEL

### ① SUPERSYMMETRY

UNBROKEN SUSY DEMANDS

$$D_i W = \partial_i W + (\partial_i K) W = 0 \quad (*) \quad i = \tau, \text{ cplx. structure moduli}$$

$$K(\tau) = -4 \log |\tau - \bar{\tau}| \quad ; \quad K(z_a) = -\log (i \int \Omega \wedge \bar{\Omega})$$

$$W = \int \mathcal{G} \wedge \Omega = W_{RR} - \tau W_{NS} \quad \text{space-time superpotential}$$

$$D_\tau W = -\frac{1}{\tau - \bar{\tau}} \int (3\mathcal{G} + \bar{\mathcal{G}}) \wedge \Omega = 0 \Rightarrow \tau = \frac{W_{RR}}{2W_{NS}} (3 - e^{i\varphi})$$

$$D_i W = \int \mathcal{G} \wedge \chi_i = 0 \quad \chi_i : \text{harmonic } (2,1) \text{ forms}$$

$$\mathcal{G} = A^i \chi_i + A^0 (-3\Omega + \bar{\Omega}) \quad \text{3-FORM FLUX}$$

MINKOWSKI  
 $W = 0$

AdS<sub>4</sub>  $W \neq 0$

## ② TADPOLE CANCELLATION

FOR A COMPACT MODEL THE TOTAL CHARGE HAS TO CANCEL. CONSIDER FOR NOW MINKOWSKI UACUA

$$\int H_{RR} \wedge H_{NS} = \frac{1}{(\tau - \tau^*)} \int G \wedge G^* = -Q(O_3)$$

↑  
O<sub>3</sub>-PLANE CHARGE

NEGATIVE O<sub>3</sub> PLANE CHARGE IS

PROVIDED BY ORIENTIFOLDS OF  
LANDAU-GINZBURG MODELS

Brunner, Hori  
Hosomichi  
Walcher ...

## LANDAU GINZBURG ORIENTIFOLDS

THE LANDAU GINZBURG MODEL IS  
CONSTRUCTED IN TERMS OF 9 COPIES OF  
 $C=1$  MINIMAL MODELS

$$W = \sum_{i=1}^9 X_i^3 \quad \text{WORLD SHEET SUPERPOTENTIAL AT FERMAT POINT}$$

DIVIDED BY THE ORBIFOLD PROJECTION

$$\mathbb{Z}_3 : X_i \rightarrow \omega X_i \quad \text{WITH} \quad \omega = e^{\frac{2\pi i}{3}}$$

MODULI FIELDS CORRESPOND TO PRIMARY FIELDS IN THE CONFORMAL FIELD THEORY.

HOW DO THESE LOOK PRECISELY?





# ORIENTIFOLD ACTION

SOURCES OF NEGATIVE CHARGE ARE  
OBTAINED BY ORIENTIFOLDING

$$X(\tau, \sigma) \simeq P X(\tau, -\sigma)$$

↓ WORLDSHEET PARITY  
↑ INVOLUTION  $P^2 = 1$

WHAT ARE THE ALLOWED INVOLUTIONS?

THE WORLDSHEET ACTION HAS AN  
F-TERM

$$\int d\theta^+ d\theta^- W(x) \xrightarrow{P_\Omega} - \int d\theta^+ d\theta^- W(Px)$$

$$W(x) = -W(Px) \quad \text{SHOULD BE ODD}$$

# INVOLUTIONS

THERE ARE 5 CHOICES OF INVOLUTIONS WHICH CONSIST IN AN OVERALL SIGN FLIP AND PAIRWISE EXCHANGE OF LG COORDINATES

$$(X_1 X_2 \dots X_8 X_9) = - (X_1 X_2 \dots X_8 X_9)$$

$$P_1: (X_1 X_2 \dots X_8 X_9) = - (X_2 X_1 X_3 X_4 \dots X_8 X_9)$$

• • •

03 PLANE

STATES SHOULD BE INVARIANT UNDER ORIENTIFOLD ACTION (UP TO A SIGN)

$$X_1 X_2 X_j \quad 7$$

$$X_i X_j X_k \Rightarrow X_i X_j X_k \quad 30$$

(84 states)

$$X_1 X_i X_j + X_2 X_i X_j \quad \frac{21}{\text{states } 63}$$

# SUSIC CYCLES IN LANDAU-GINZBURG

Iqbal, Hori + Vafa

FLUXES NEED TO BE INTEGRATED OVER SUSIC CYCLES TO CHECK TADPOLE CANCELLATION

WE ARE CONSIDERING AN  $N=2$  LG THEORY ON A MANIFOLD WITH BOUNDARY. THE SUPERPOTENTIAL  $W$  IS AN F-TERM THAT UNDER SUSY GIVES A TOTAL DERIVATIVE. BOUNDARY TERM = 0

① A-CYCLES (SLABS)

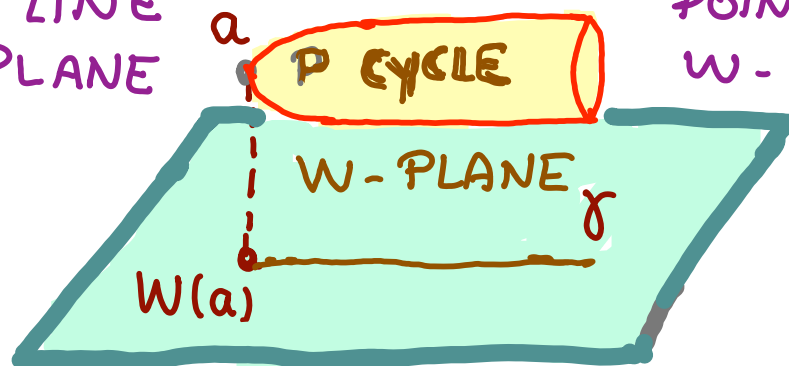
② B-CYCLES (Cplx)

$$\text{Im} W = 0 \text{ (odd)}$$

$$W = 0 \text{ (even)}$$

STRAIGHT LINE  
IN W-PLANE

POINT IN  
W-PLANE

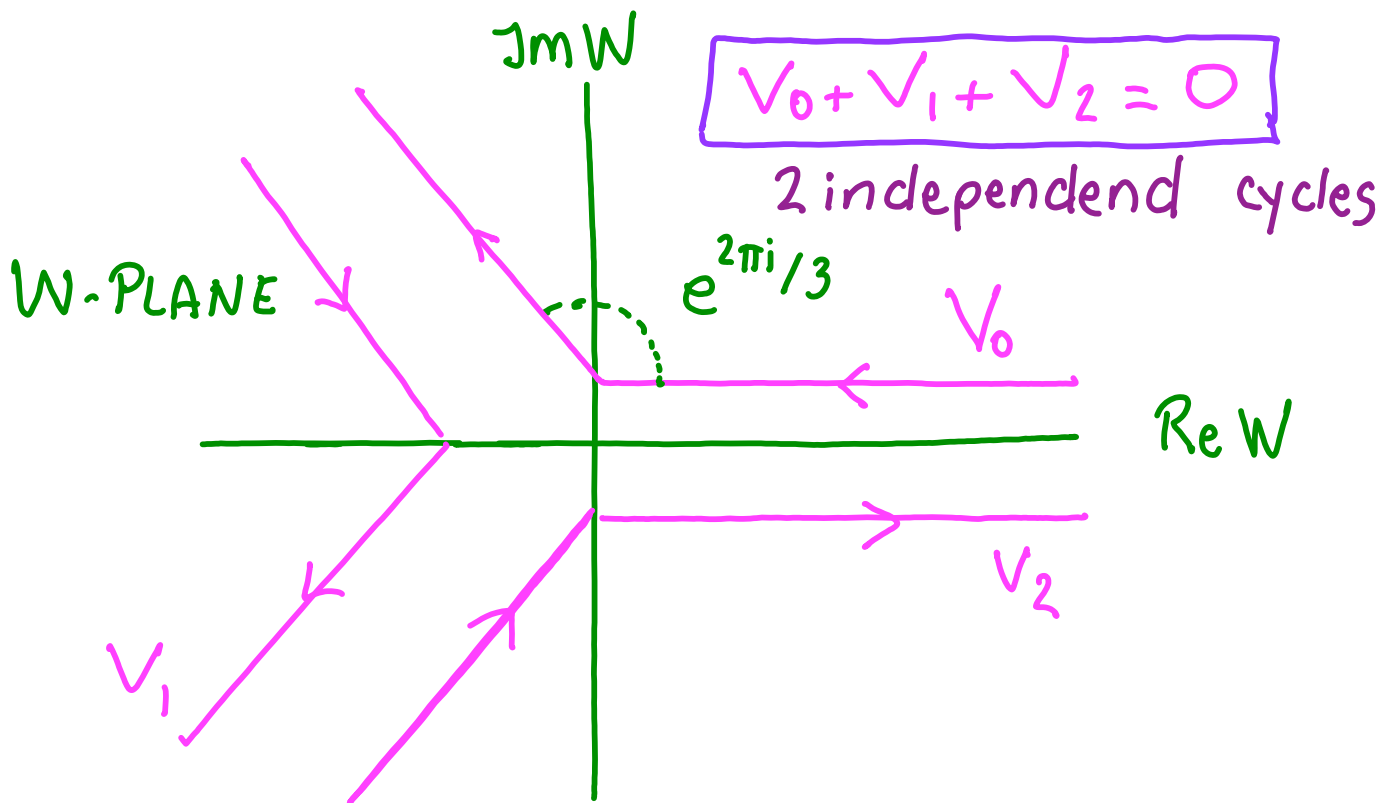


# SIMPLE EXAMPLE

CONSIDER ONE  $c=1$  MINIMAL MODEL

$$W(x) = x^3$$

$$\text{Im } W = 0$$



WE NEED TO BUILD A  $\mathbb{Z}_3$  INVARIANT  
COMBINATION OF THE TWO CYCLES AND  
CONSIDER 9 MINIMAL MODELS

WE WOULD LIKE TO INTEGRATE THE  
R-R GROUND STATES (BASIS)

$$x^{\ell-1} \equiv |e\rangle \quad \ell = 1, 2$$

OVER A-CYCLES  $\langle V_m |$

THERE IS A NATURAL PAIRING THAT  
DEFINES THE INTEGRATION OF STATES  
OVER CYCLES

Cecotti, Hori + Vafa

$$\langle V_m | e \rangle = \int_{V_m} x^{\ell-1} e^{-x^3} dx \quad \ell = 1, 2$$

intersection matrix

TADPOLE:

$$\frac{1}{\tau - \tau^*} \int \Theta \wedge \Theta^* = \frac{1}{\tau - \tau^*} \langle e | V_m \rangle \overset{\downarrow}{I}^{mm} \langle V_m | e' \rangle$$

THESE ARE ALL THE TOOLS WE NEED!

## SUMMARY OF CONDITIONS

CONSIDER MINKOWSKI SOLUTIONS FOR NOW

① SUPERSYMMETRY  $G = H_{RR} - \tau H_{NS} \in H^{2,1}$

$$\int G \wedge \Omega = \int G \wedge \Omega^* = \int G \wedge \chi_{2,1} = 0$$

② TADPOLE CANCELLATION

$$\int H_{RR} \wedge H_{NS} = \frac{1}{\tau - \tau^*} \int G \wedge G^* = 12 - N_{D3}$$

③ FLUX QUANTIZATION

$$\int_{\Pi_{\vec{m}}} G = N^{\vec{m}} - \tau M^{\vec{m}} \leftarrow \begin{array}{l} \vec{m} = (m_1 \dots m_g) \\ \text{NS flux } \times \\ \text{RR-flux } \times \end{array}$$

$\leftarrow$  cycles

TAKING THIS INTO ACCOUNT WE

OBTAIN A LARGE SYSTEM OF DIOPHANTINE EQS.

HARD TO SOLVE !

# SAMPLE STRONG COUPLING SOLUTION

ALL MINKOWSKI SOLUTIONS EMERGE AT STRONG COUPLING  $\nabla$  (ADS SOLUTIONS ALSO EXIST)  
(NOT IN THIS MODEL THOUGH)

$$G = |111122121\rangle - |111122112\rangle - |111121221\rangle + |111121212\rangle$$

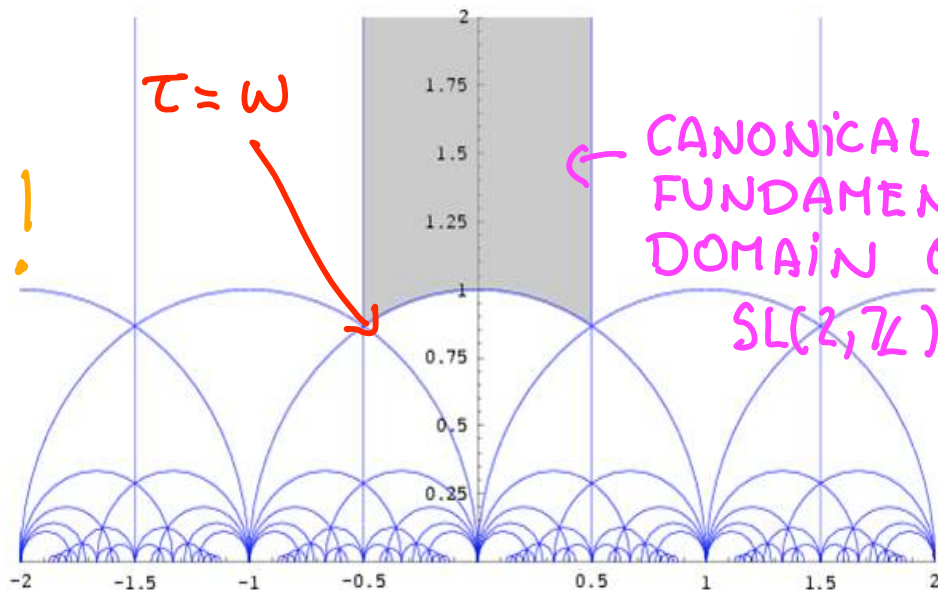
$$|e\rangle = |l_1, l_2, \dots, l_g\rangle \text{ with } |l\rangle = \chi^{l-1}$$

$$l = 1, 2$$

$$\tau = \omega = e^{\frac{2\pi i}{3}}$$

$\uparrow$  WEAK COUPLING (NORTH)

STRONG COUPLING!





# NON-RENORMALIZATION THEOREM

THE TYPE IIB FLUX SUPERPOTENTIAL DOES NOT RECEIVE ANY CORRECTIONS IN  $g_s$

↑  
string coupling

$$W_{IIB} = \int G \wedge \Omega$$



Vafa  
Dijkgraaf + Vafa

Burgess, Escoda + Quevedo

## ① PERTURBATIVE CORRECTIONS

THE  $N=1$  ACTION STILL HAS FEATURES OF THE  $N=2$  THEORY

(NO COUPLING BETWEEN HYPERS + VECTORS)

## ② NON-PERTURBATIVE CORRECTIONS:

NO CANDIDATE INSTANTON AVAILABLE

THIS ENSURES THE EXISTENCE OF VACUA!  
MASSES OF MODULI?? SUSY BREAKING?



## TYPE IIB FLUX VACUA AT WEAK COUPLING

**GOAL :** SEARCH FOR VACUA IN THE LARGE  
COMPLEX STRUCTURE AND SMALL  $g_s$  LIMIT

**MIRROR** TO MASSIVE IIA MODEL OF D6KT  
(LARGE RADIUS, SMALL  $g_s$ )

$$W = \sum_{i=1}^9 x_i^3 + a_1 x_1 x_2 x_3 + a_2 x_4 x_5 x_6 + a_3 x_7 x_8 x_9 + \dots$$

BULK MODULI :  $t_1, t_2, t_3$  RELATED TO  $a_i$   
COMPLEX STRUCTURE OF  $T^6 = (T^2)^3$

BLOW UP MODES : STABILIZED

# FLUX SUPERPOTENTIAL AND MODULI

WE WOULD LIKE TO DERIVE  $W_{\text{IB}}(t_1, t_2, t_3)$ .

$$W_{\text{IB}} = \int (H_R - \tau H_{\text{NS}}) \wedge \Omega$$

$\downarrow$   $H_R = M^a \alpha_a - \tilde{M}^a \beta_a$        $\nwarrow$   $H_{\text{NS}} = N^a \alpha_a - \tilde{N}^a \beta_a$   
 SYMPLECTIC BASIS

## SPECIAL GEOMETRY

$$z_{\text{I}} = \oint_{A_{\text{I}}} \Omega \quad \frac{\partial \mathcal{F}}{\partial z_{\text{I}}} = \oint_{B_{\text{I}}} \Omega \quad \text{PREPOTENTIAL}$$

$$\mathcal{F}(z) = -\frac{1}{3!} \mathcal{R}_{\text{IJK}} \frac{z^{\text{I}} z^{\text{J}} z^{\text{K}}}{z^0} ; \quad \mathcal{R}_{123} = \mathcal{R} = 1$$

$t_1 = t_2 = t_3 = t$

$$W_{\text{RR}} = -t^3 M_0 + 3t^2 M_2 + 3t M_4 + M_6$$

$$W_{\text{NS}} = -t^3 N_0 + 3t^2 N_2 + 3t N_4 + N_6$$

$$W_{\text{IB}} = W_{\text{RR}} - \tau W_{\text{NS}}$$

MODULI [FLUX XX] THEN EASILY

FOLLOWS BY SOLVING TADPOLE

AND

$$\begin{cases} D_t W = D_z W = 0 \\ W = 0 \text{ (MINKOWSKI)} \end{cases}$$



WHAT DID WE SEE ? ?

① MINKOWSKI SOLUTIONS ARE  
CONFINED TO STRONG COUPLING

② AdS SOLUTIONS EXIST FOR  
LARGE  $t$  AND SMALL  $g_s$   
WE WORKED OUT SPECIFIC  
EXAMPLES

## EXAMPLE: MIRROR OF MASSIVE IIA

A SIMPLE SOLUTION WHICH IS MIRROR TO  
THE MASSIVE TYPE IIA MODEL IS

---

$$W_{NS} = N_6 \quad W_{RR} = -t^3 M_0 + 3t^2 M_2 + 3t M_4 + M_6$$

TADPOLE

$$\int H_{RR} \wedge H_{NS} = -M_0 N_6$$

$M_2, M_4, M_6 \rightarrow \infty$  NOT BOUNDED!

PARAMETRIC CONTROL!

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## SOLUTION

$$t_1 = \frac{M_2}{M_0} \quad t_2 = \sqrt{-\frac{M_2^2}{M_0^2} - \frac{M_4}{M_0}} \quad t = t_1 + it_2$$

$$\tau_2 \approx \frac{M_0}{N_6} (t_2)^3$$



$t$  IS LARGE,  $g_s = \frac{1}{\tau_2}$  IS SMALL!

## A CONJECTURE



A SURPRISE ARRIVED FROM THE MASS MATRIX



$$M_{ij}(t, \tau) \sim \Lambda_{\text{Ads}} \mathcal{O}_{ij}(1)$$

MASSSES ARE OF THE ORDER OF THE 4D COSMOLOGICAL CONSTANT!

SITUATION IS RATHER **GENERIC** FOR ALL TYPE IIB SOLUTIONS AS WELL AS FOR THE MASSIVE IIA MODEL OF D6KT

Gukov, Ooguri + Vafa

## CONJECTURE

"ANY SEQUENCE OF SUPERSYMMETRIC WEAKLY COUPLED STRING VACUA HAS SOME MODULI FIELDS WITH MASSES OF THE ORDER OF THE COSMOLOGICAL CONSTANT..."

FOR SUSIC VACUA MODULI MIGHT ONLY BE STABILIZED IN THE NON-GEOMETRIC PHASE !!!

Kalloshtco  
Saueressig  
Theis +  
Vandoren

## UPLIFTING TO DE SITTER

THE SITUATION MAY IMPROVE ONCE WE UPLIFT TO DE SITTER SPACE AND MODULI MIGHT BE HEAVY

\* WE CAN UPLIFT WITH  $\bar{D}3$ 's (KKLT)

\* SUSY BREAKING WITH FLUX ONLY

ONCE SUSY IS BROKEN AND IN MODELS WITH A RICHER STRUCTURE THERE MIGHT BE AN ALTERNATIVE TO  $\bar{D}3$ 's INVOLVING ONLY FLUX.

Aganagic, Beem  
Heckman + Vafa  
(non-compact)

INGREDIENTS:

\* PERTURBATIVE CORRECTIONS TO  $W(\Phi)$

\* NON-PERTURBATIVE CORRECTIONS TO  $W(\Phi)$ , WHICH ARE ALLOWED IN MORE COMPLICATED MODELS ONCE SUSY IS BROKEN.

NOT A FREE LUNCH THOUGH !

# CONCLUSION

IT IS OF GREAT IMPORTANCE TO UNDERSTAND MODULI STABILIZATION IN THE NON-GEOMETRIC PHASE ?

SOME RATHER INTERESTING

QUESTIONS NEED TO BE SOLVED:

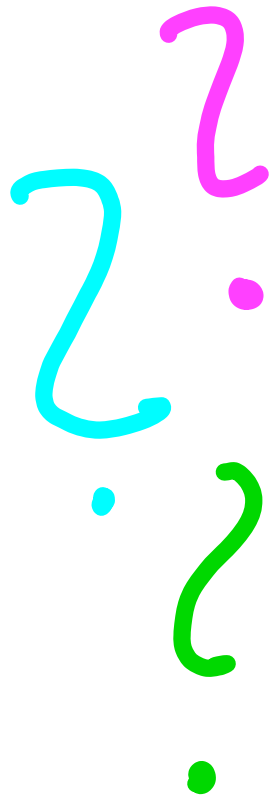
\* STRONG COUPLING SOLUTION :  
IS THERE A DUAL CFT ???

\* WEAK COUPLING SOLUTION :

INSTANTON CORRECTIONS TO  $W$ ,  
PERTURBATIVE CORRECTIONS TO  $K$

\* FLUXES IN CFT AND LANDAU-GINZBURG ?

\* IMPLICATIONS OF LIGHT MODULI FOR SWAMPLAND





AN EXCITING TRIP THROUGH THE  
NON-GEOMETRIC LANDSCAPE  
IS AHEAD OF US ! 😊

