New gravity duals for higher-dimensional superconformal theories

Alessandro Tomasiello

based on

1309.2949 with F.Apruzzi, M. Fazzi, D. Rosa 1404.0711 with D. Gaiotto 1406.0852 with F.Apruzzi, M. Fazzi, A. Passias, D. Rosa









Several reasons to be interested in CFTs in d > 4.

Several reasons to be interested in CFTs in d > 4.

• Harder to define.

e.g. $Tr(F_{\mu\nu})^2$ relevant in d>4. Similar problem to $\sqrt{-g}R$ in d>2

Several reasons to be interested in CFTs in d > 4.

Harder to define.

e.g. $Tr(F_{\mu\nu})^2$ relevant in d>4. Similar problem to $\sqrt{-g}R$ in d>2

- String theory:
- $\mathcal{N} = (2,0)$ theory on M5-branes
- theories arising at singularities
- intersecting branes

[Witten '96; Seiberg, Witten '96; (Blum,) Intriligator '97; Hanany, Zaffaroni '97; Brunner, Karch '97...]

Several reasons to be interested in CFTs in d > 4.

Harder to define.

e.g. $Tr(F_{\mu\nu})^2$ relevant in d>4. Similar problem to $\sqrt{-g}R$ in d>2

- String theory:
- $\mathcal{N} = (2,0)$ theory on M5-branes
 - theories arising at singularities
 - intersecting branes
- Mothers of interesting theories in $d \le 4$

[Witten '96; Seiberg, Witten '96; (Blum,) Intriligator '97; Hanany, Zaffaroni '97; Brunner, Karch '97...]

Several reasons to be interested in CFTs in d > 4.

Harder to define.

e.g. $Tr(F_{\mu\nu})^2$ relevant in d>4. Similar problem to $\sqrt{-g}R$ in d>2

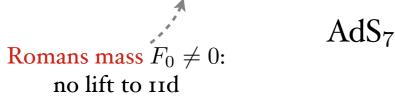
- String theory:
- $\mathcal{N} = (2,0)$ theory on M5-branes
- theories arising at singularities
- intersecting branes
- Mothers of interesting theories in $d \le 4$

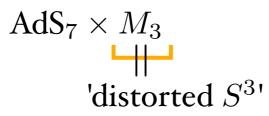
[Witten '96; Seiberg, Witten '96; (Blum,) Intriligator '97; Hanany, Zaffaroni '97; Brunner, Karch '97...]

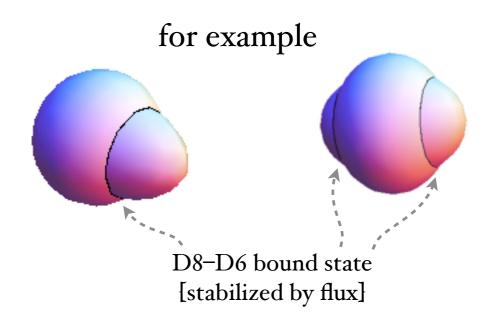
In this talk, we will see some holographic classification results for superconformal theories in d=5,6:

- A classification of AdS₇ BPS solutions in type II sugra.
 - in 11d, only $AdS_7 \times S^4/\Gamma$

- A classification of AdS₇ BPS solutions in type II sugra.
 - in 11d, only $AdS_7 \times S^4/\Gamma$
 - but in massive IIA, many new solutions!

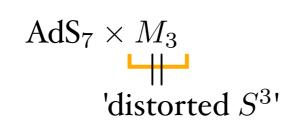


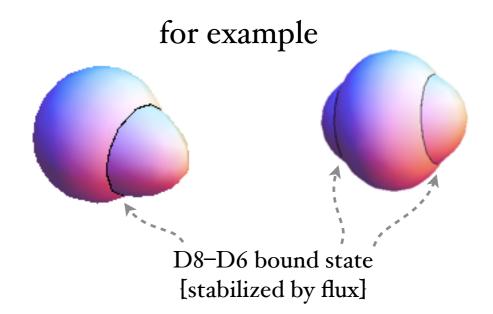




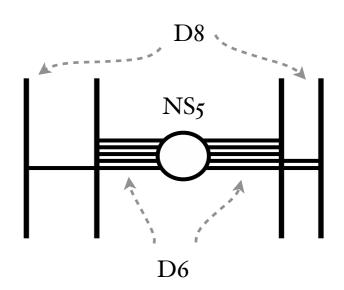
- A classification of AdS₇ BPS solutions in type II sugra.
 - in 11d, only $AdS_7 \times S^4/\Gamma$
 - but in massive IIA, many new solutions!

Romans mass
$$F_0 \neq 0$$
:
no lift to 11d

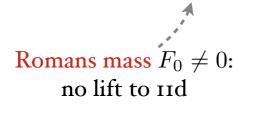


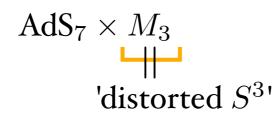


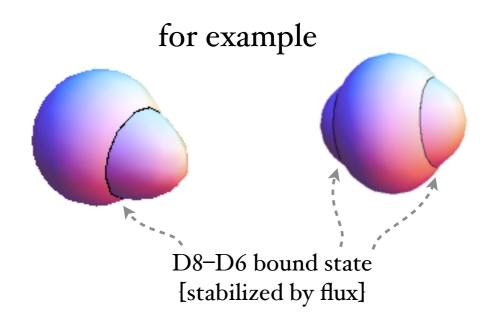
- Their $\mathcal{N} = (1,0)$ CFT₆ duals.
 - near-horizon limits of brane systems
 - quiver descriptions on tensor branch
 - via T-duality: 'Hitchin pole' extension of F-theory classification in [Heckman, Morrison, Vafa '13]



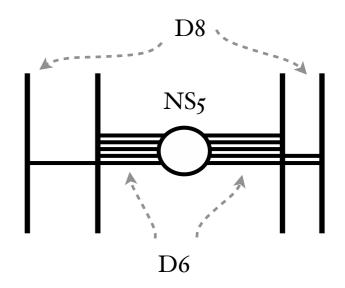
- A classification of AdS₇ BPS solutions in type II sugra.
 - in 11d, only $AdS_7 \times S^4/\Gamma$
 - but in massive IIA, many new solutions!







- Their $\mathcal{N} = (1,0)$ CFT₆ duals.
 - near-horizon limits of brane systems
 - quiver descriptions on tensor branch
 - via T-duality: 'Hitchin pole' extension of F-theory classification in [Heckman, Morrison, Vafa '13]



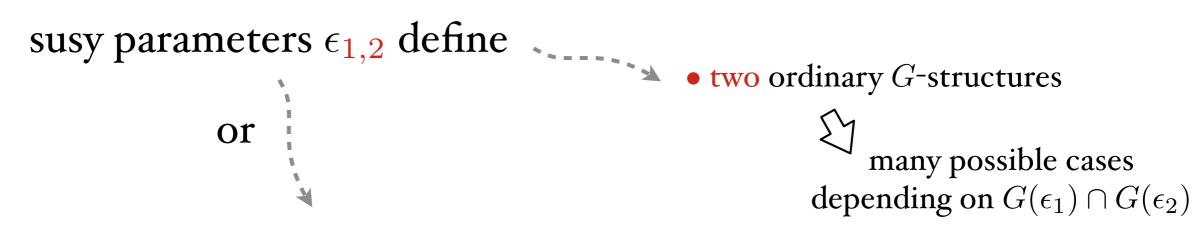
• A similar (but less complete) classification of AdS₆ solutions.

Plan

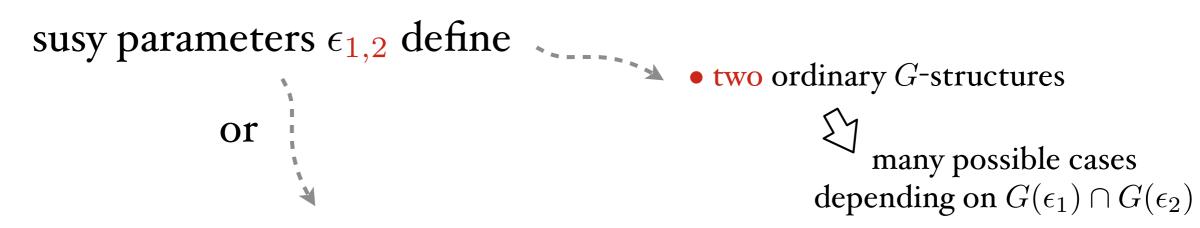
- I. Methods: Pure spinors
 - 2. Classification of AdS₇ solutions
 - 3. CFT₆ duals
 - 4. AdS₆ solutions

susy parameters $\epsilon_{1,2}$ define \bullet two ordinary G-structures

many possible cases depending on $G(\epsilon_1) \cap G(\epsilon_2)$



 \bullet one $G\mbox{-structure}$ on $T\oplus T^*$ 'generalized tangent bundle': vectors \oplus 1-forms

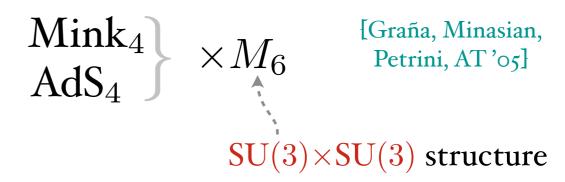


ullet one $G ext{-structure}$ on $T\oplus T^*$ 'generalized tangent bundle': vectors \oplus 1-forms

forms obeying algebraic constraints: often 'pure spinors'

nicer equations; easier classifications

$$\left. \begin{array}{c} \operatorname{Mink_4} \\ \operatorname{AdS_4} \end{array} \right\} \times M_6 \qquad \begin{array}{c} \left[\operatorname{Gra ilde{n}a,\,Minasian,\,Minasian,\,Petrini,\,AT\,'o5}\right] \end{array}$$



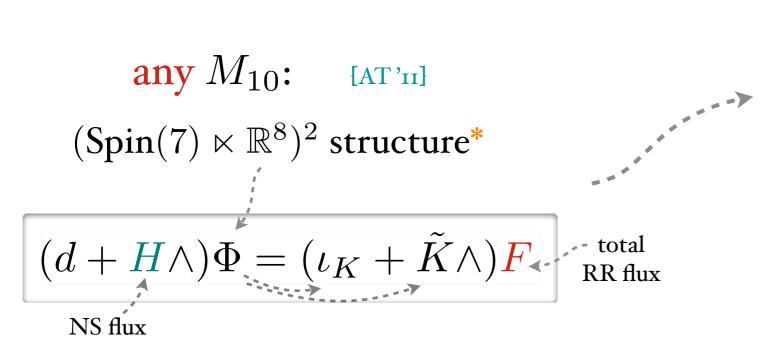
[Hitchin's "generalized complex geometry"]

any M_{10} : [AT'II]

$$(d + H \wedge)\Phi = (\iota_K + \tilde{K} \wedge)F$$

$$\begin{array}{c} \text{Mink}_4 \\ \text{AdS}_4 \end{array} \times M_6 \quad \begin{array}{c} \text{[Graña, Minasian, Petrini, AT'o5]} \\ \text{SU(3)} \times \text{SU(3)} \text{ structure} \end{array}$$

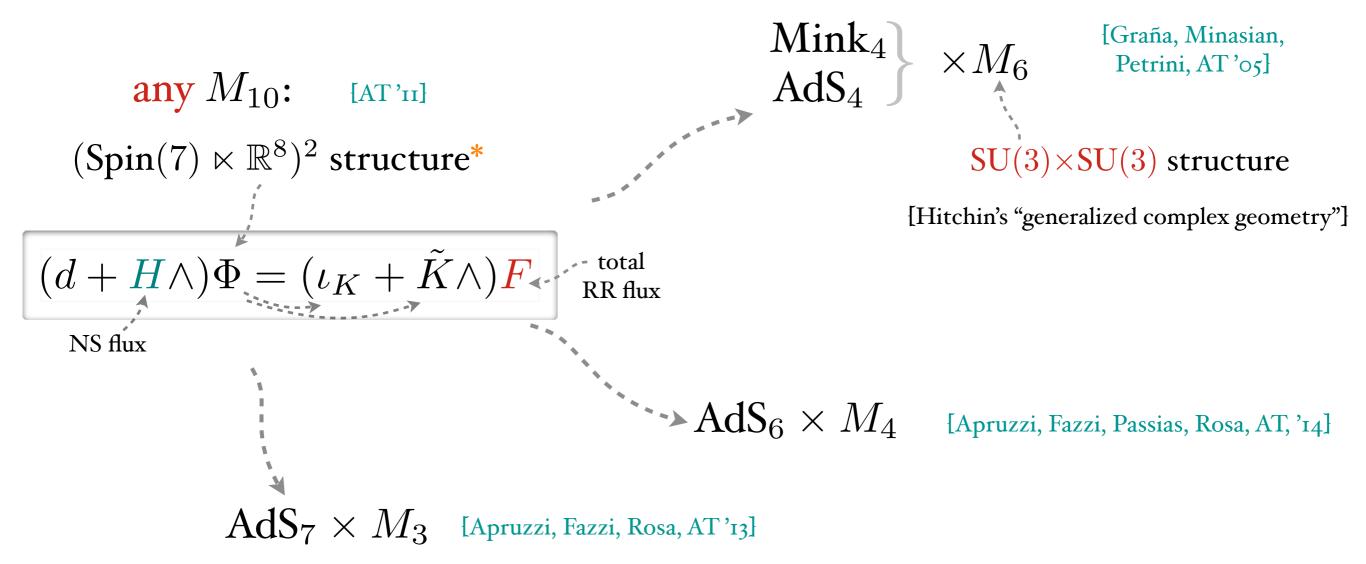
[Hitchin's "generalized complex geometry"]



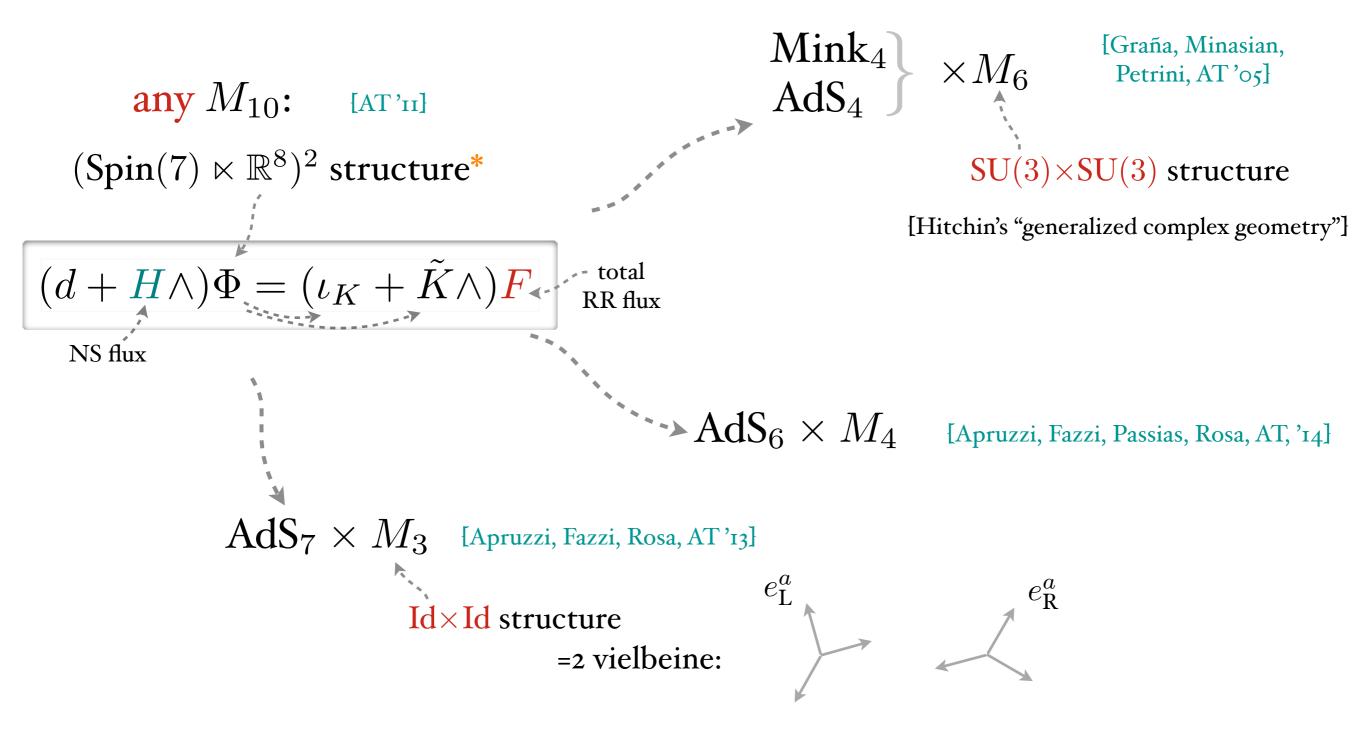
$$\begin{array}{c} \text{Mink}_4 \\ \text{AdS}_4 \end{array} \times \begin{array}{c} M_6 \\ \text{Petrini, AT '05} \end{array}$$

[Hitchin's "generalized complex geometry"]

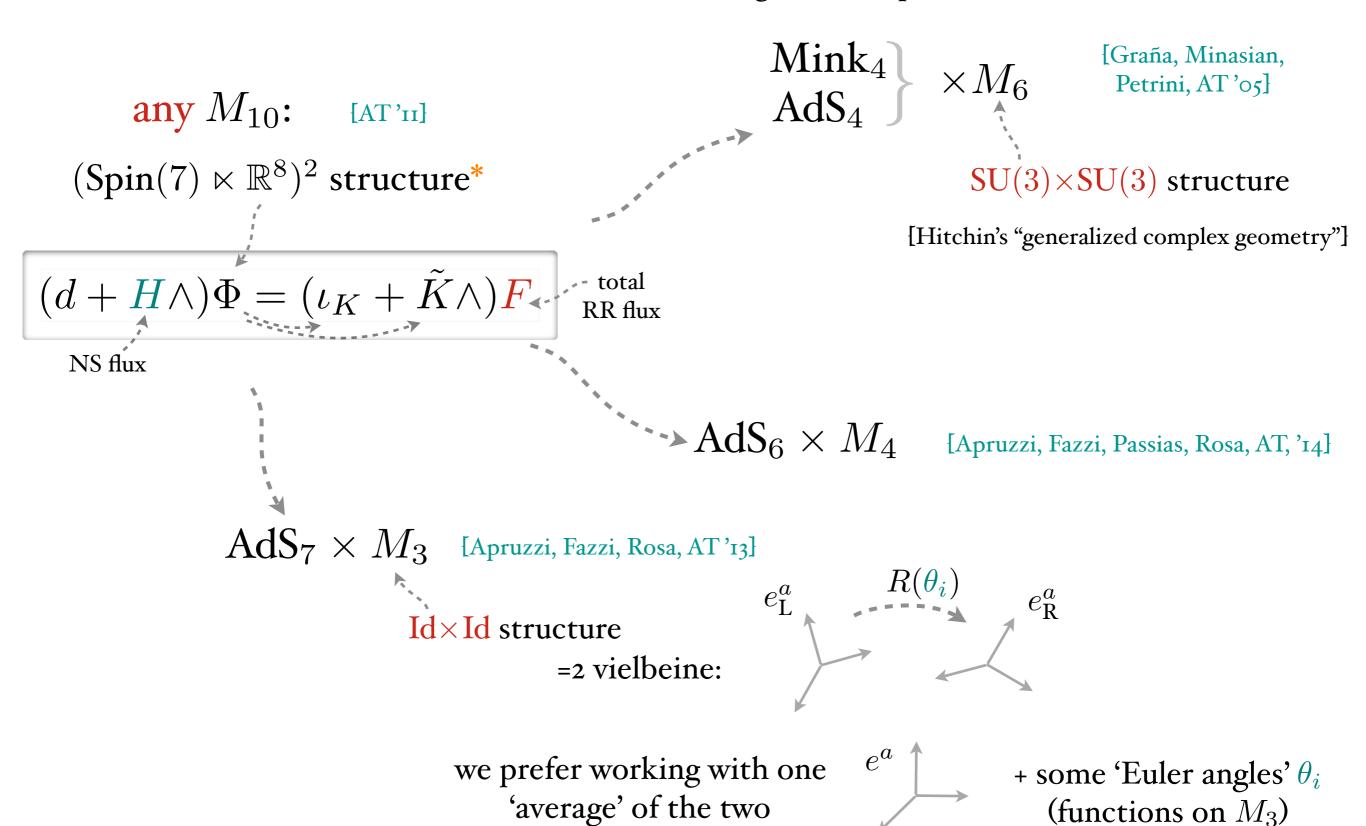
^{*}simplifying the story a bit...



^{*}simplifying the story a bit...



^{*}simplifying the story a bit...



*simplifying the story a bit...

[Apruzzi, Fazzi, Rosa, AT '13]

[Apruzzi, Fazzi, Rosa, AT '13]

IIB: the system contains

zero-form equations on θ_i

[Apruzzi, Fazzi, Rosa, AT'13]

IIB: the system contains

zero-form equations on $\theta_i \longrightarrow no$ solutions!

but: see later about F-theory

[Apruzzi, Fazzi, Rosa, AT'13]

IIB: the system contains

zero-form equations on $\theta_i \longrightarrow no$ solutions!

but: see later about F-theory

IIA: the system contains one-form equations

 $e^a \sim \text{functions}(\theta_i) d(\theta_i)$

[Apruzzi, Fazzi, Rosa, AT '13]

the system contains IIB:

zero-form equations on $\theta_i \longrightarrow no$ solutions!

but: see later about F-theory

the system contains IIA: one-form equations

one-form equations $e^a \sim \mathrm{functions}(\theta_i) \, d(\theta_i) \, \Rightarrow \begin{array}{c} \mathrm{local\ form} \\ \mathrm{of\ the\ metric:} \end{array} \qquad ds^2 \sim dr^2 + v^2(r) ds_{S^2}^2$ This S^2 realizes

the SU(2) R-symmetry of a (1,0) 6d theory.

[Apruzzi, Fazzi, Rosa, AT '13]

the system contains IIB:

zero-form equations on $\theta_i \longrightarrow no$ solutions!

but: see later about F-theory

the system contains IIA: one-form equations

one-form equations $e^a \sim \mathrm{functions}(\theta_i) \, d(\theta_i) \, \Rightarrow \begin{array}{c} \mathrm{local\ form} \\ \mathrm{of\ the\ metric:} \end{array} \qquad ds^2 \sim dr^2 + v^2(r) ds_{S^2}^2 \end{array}$ This S^2 realizes

no Ansatz necessary

the SU(2) R-symmetry of a (1,0) 6d theory.

[Apruzzi, Fazzi, Rosa, AT '13]

the system contains IIB:

zero-form equations on $\theta_i \longrightarrow no$ solutions!

but: see later about F-theory

the system contains IIA: one-form equations

one-form equations $e^a \sim \mathrm{functions}(\theta_i) \, d(\theta_i) \, \Rightarrow \begin{array}{c} \mathrm{local\ form} \\ \mathrm{of\ the\ metric:} \end{array} \qquad ds^2 \sim dr^2 + v^2(r) ds_{S^2}^2 \end{array}$ This S^2 realizes

no Ansatz necessary

the SU(2) R-symmetry of a (1,0) 6d theory.

The rest of the system also determines the fluxes Bianchi id's automatically satisfied

[Apruzzi, Fazzi, Rosa, AT'13]

the system contains IIB:

zero-form equations on $\theta_i \longrightarrow no$ solutions!

but: see later about F-theory

the system contains IIA: one-form equations

one-form equations $e^a \sim \operatorname{functions}(\theta_i) \, d(\theta_i) \, \Rightarrow \begin{array}{c} \operatorname{local\ form} \\ \operatorname{of\ the\ metric:} \end{array} \qquad ds^2 \sim dr^2 + v^2(r) ds_{S^2}^2$

no Ansatz necessary

This S^2 realizes the SU(2) R-symmetry of a (1,0) 6d theory.

The rest of the system also determines the fluxes Bianchi id's automatically satisfied

> When the dust settles: we have a local solution provided we solve a system of 3 ODEs

warping

 $AdS_7 \times M_4$ in 11d sugra:

cone over M_4 should have reduced holonomy

 $AdS_7 \times M_4$ in 11d sugra:

cone over M_4 should have reduced holonomy

We can reduce $AdS_7 \times S^4$ to IIA:

 $AdS_7 \times M_4$ in 11d sugra:

cone over M_4 should have reduced holonomy

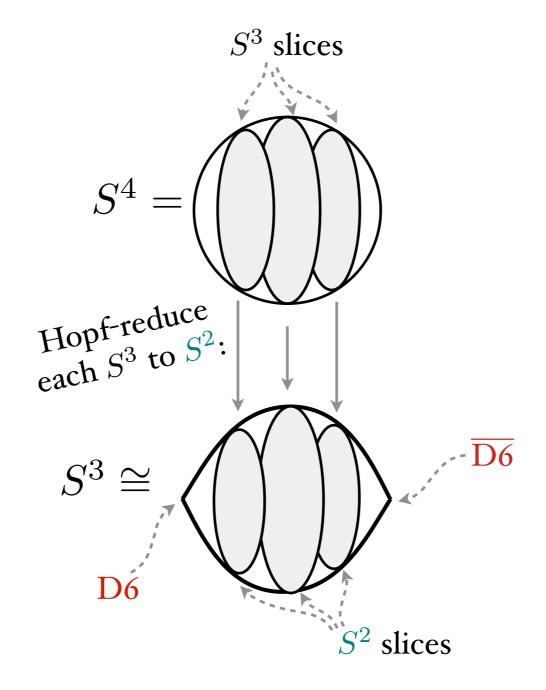
We can reduce $AdS_7 \times S^4$ to IIA:

$$S^3$$
 slices $S^4 = \bigcirc$

 $AdS_7 \times M_4$ in 11d sugra:

cone over M_4 should have reduced holonomy

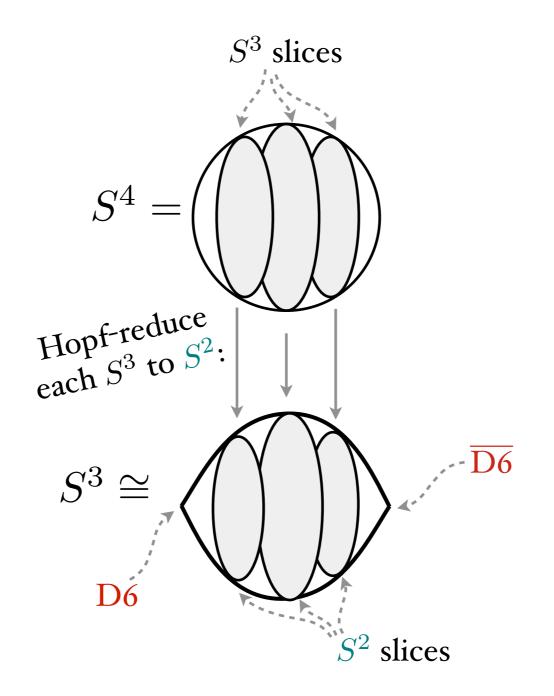
We can reduce $AdS_7 \times S^4$ to IIA:



 $AdS_7 \times M_4$ in 11d sugra:

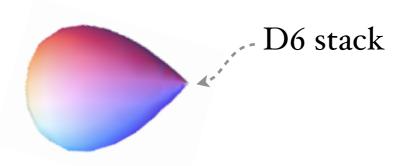
cone over M_4 should have reduced holonomy

We can reduce $AdS_7 \times S^4$ to IIA:

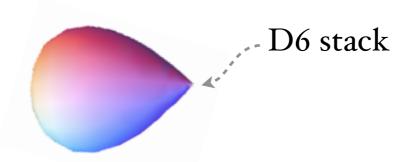


agrees with results in previous slide

we can make one of the poles regular:

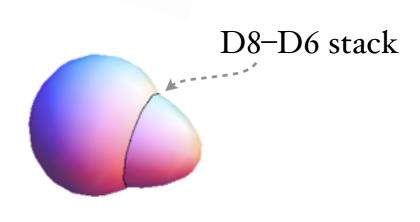


we can make one of the poles regular:

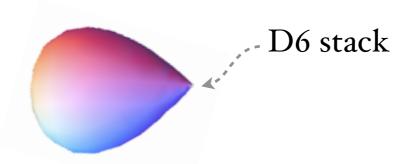


or both,
if we include D8's:
actually, 'magnetized' D8's

D8-D6 bound states

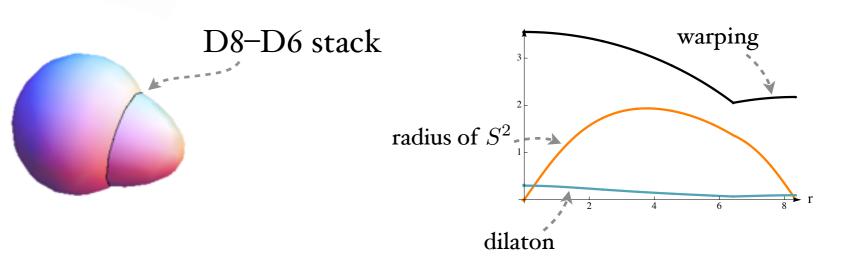


we can make one of the poles regular:

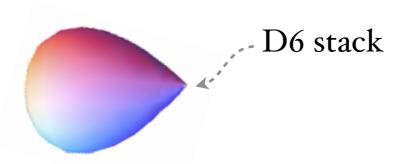


or both,
if we include D8's:
actually, 'magnetized' D8's

D8-D6 bound states



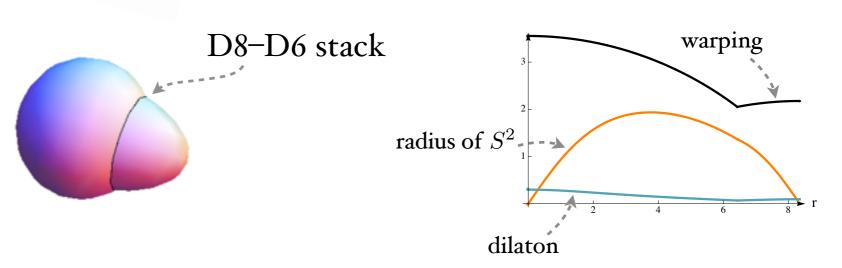
we can make one of the poles regular:



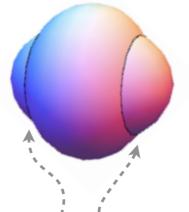
or both, if we include D8's:

actually, 'magnetized' D8's

D8-D6 bound states



or include several D8/D6 stacks:

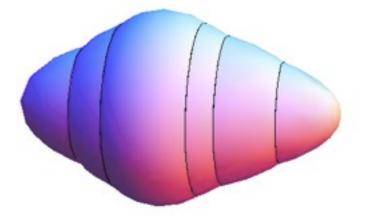


intuitively: D8's don't slip off because of electric attraction

stacks with opposite D6 charge

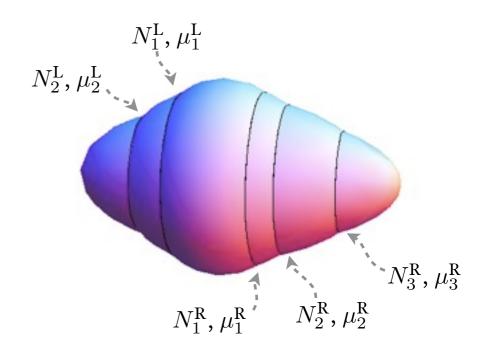
Most general solution is characterized by

[Apruzzi, Fazzi, Rosa, AT '13; Gaiotto, AT '14]



ullet numbers N_i of D8's, and their D6 charges μ_i

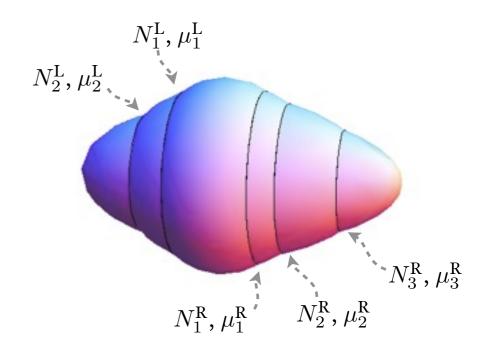
[D8's with same D6 charge stay together.]



ullet numbers N_i of D8's, and their D6 charges μ_i

[D8's with same D6 charge stay together.]

• flux integer $N \equiv \frac{1}{4\pi^2} \int H$

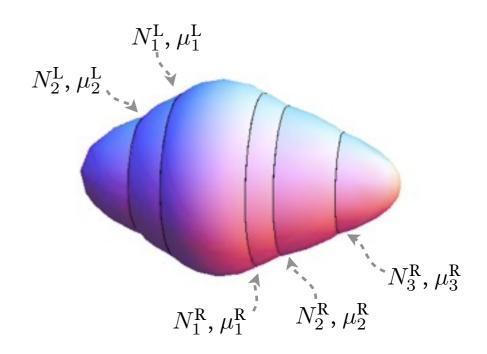


ullet numbers N_i of D8's, and their D6 charges μ_i

[D8's with same D6 charge stay together.]

• flux integer $N \equiv \frac{1}{4\pi^2} \int H$

subject to constraints:



• numbers N_i of D8's, and their D6 charges μ_i

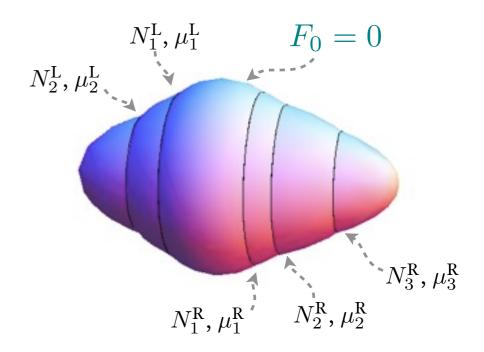
[D8's with same D6 charge stay together.]

• flux integer $N \equiv \frac{1}{4\pi^2} \int H$

subject to constraints:

 μ_i depend on gauge choice for B.

Place gauge transf. e.g. in region where $F_0 = 0$:



Most general solution is characterized by

[Apruzzi, Fazzi, Rosa, AT '13; Gaiotto, AT '14]

ullet numbers N_i of D8's, and their D6 charges μ_i

[D8's with same D6 charge stay together.]

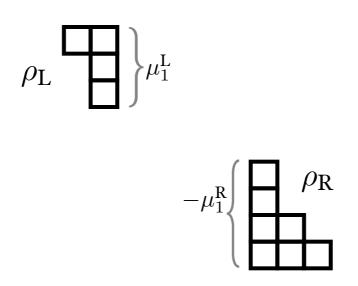
• flux integer $N \equiv \frac{1}{4\pi^2} \int H$

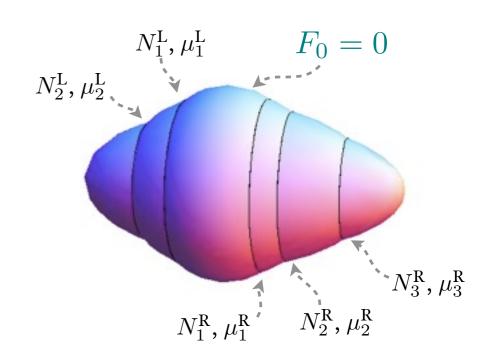
subject to constraints:

 μ_i depend on gauge choice for B.

Place gauge transf. e.g. in region where $F_0 = 0$:

 $\begin{array}{ll} \bullet \; \mu_i & \text{positive and growing for } F_0 > 0 \\ & \text{negative and growing for } F_0 < 0 \end{array}$





[Apruzzi, Fazzi, Rosa, AT '13; Gaiotto, AT '14]

ullet numbers N_i of D8's, and their D6 charges μ_i

[D8's with same D6 charge stay together.]

• flux integer $N \equiv \frac{1}{4\pi^2} \int H$

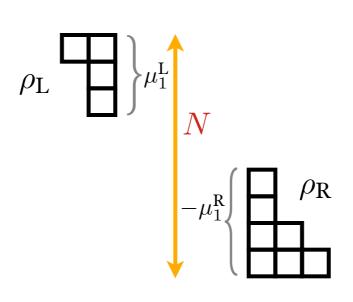
subject to constraints:

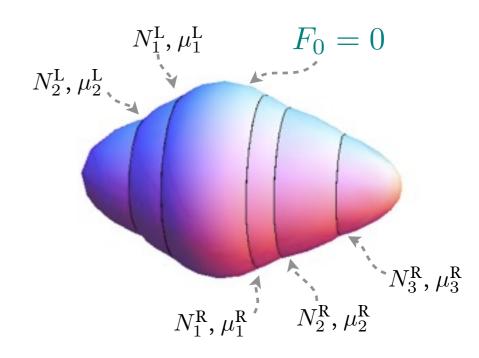
 μ_i depend on gauge choice for B.

Place gauge transf. e.g. in region where $F_0 = 0$:

 $\begin{array}{ll} \bullet \; \mu_i & \text{positive and growing for } F_0 > 0 \\ & \text{negative and growing for } F_0 < 0 \end{array}$

•
$$N \ge |\mu_1^{\rm L}| + |\mu_1^{\rm R}|$$
bordering
 $F_0 = 0$ region.





[Gaiotto, AT '14]

[Gaiotto, AT '14]

Often one finds a CFT dual using a brane configuration.

[Gaiotto, AT'14]

III. CFT₆ duals

Often one finds a CFT dual using a brane configuration.

For the $F_0 = 0$ solution this can be done:

Often one finds a CFT dual using a brane configuration.

For the $F_0 = 0$ solution this can be done:

AdS₇ ×
$$S^4/\mathbb{Z}_k$$

reduction
to IIA

AdS₇ × S^3

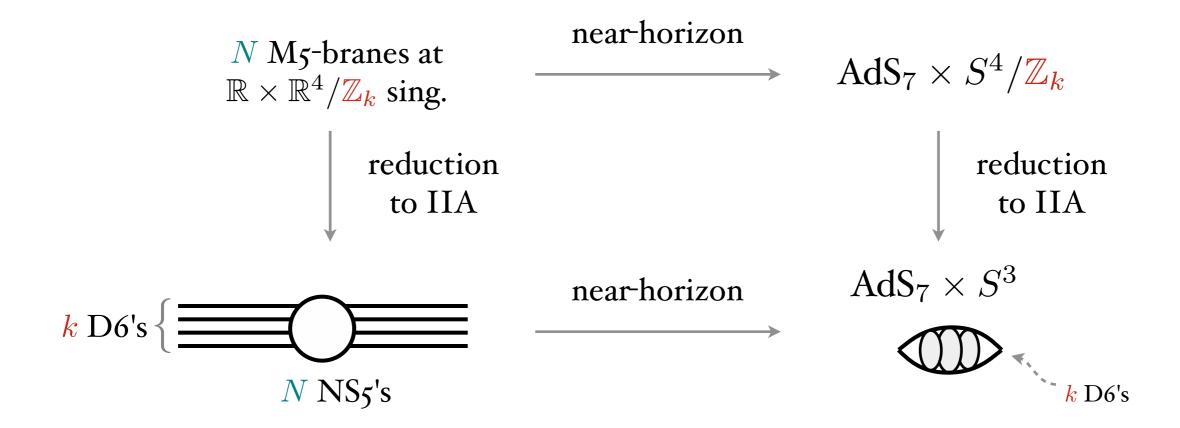
Often one finds a CFT dual using a brane configuration.

For the $F_0 = 0$ solution this can be done:

N M5-branes at $\mathbb{R} \times \mathbb{R}^4/\mathbb{Z}_k$ sing. AdS $_7 \times S^4/\mathbb{Z}_k$ reduction to IIA AdS $_7 \times S^3$

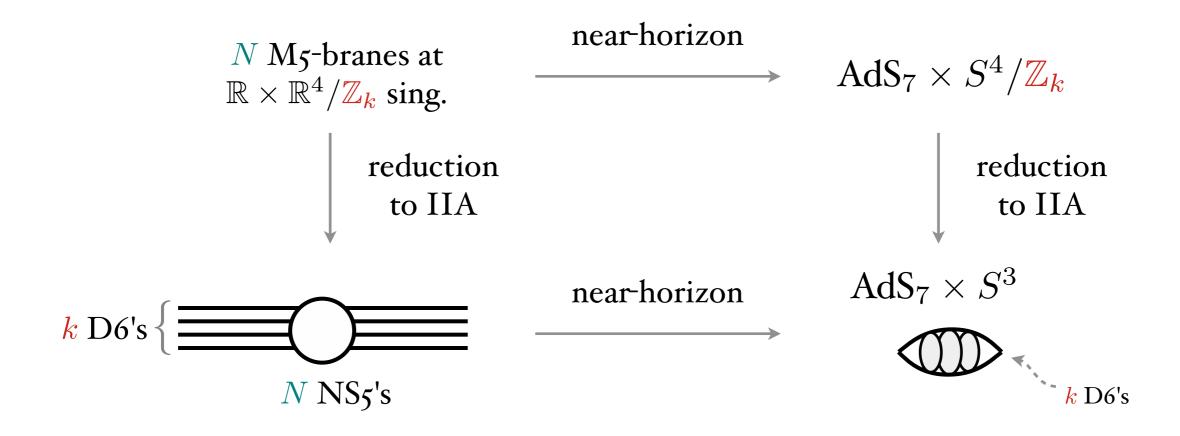
Often one finds a CFT dual using a brane configuration.

For the $F_0 = 0$ solution this can be done:



Often one finds a CFT dual using a brane configuration.

For the $F_0 = 0$ solution this can be done:

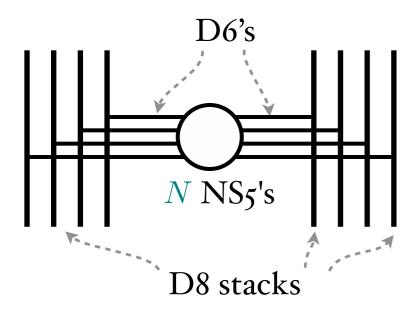


• (1,0) supersymmetry

CFT₆ with

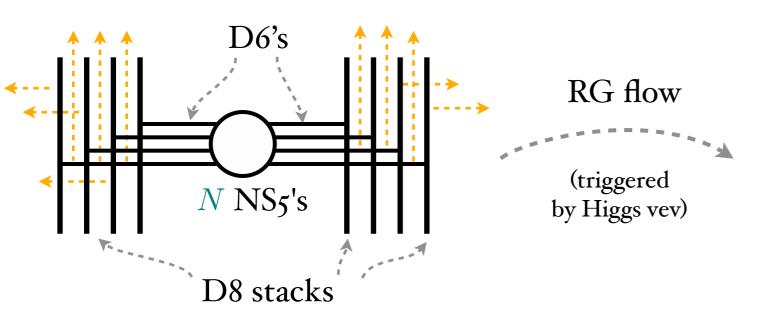
- N^3k^2 degrees of freedom
- $SU(k) \times SU(k)$ flavor symmetry

Adapting methods developed in [Gaiotto, Witten '08] for 3d theories



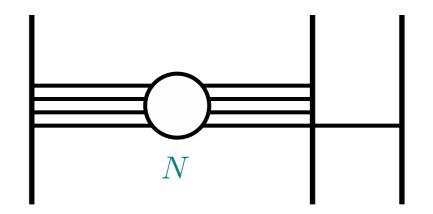
Each D6 on a separate D8: Dirichlet b.c. for fields on the D6.

Adapting methods developed in [Gaiotto, Witten '08] for 3d theories

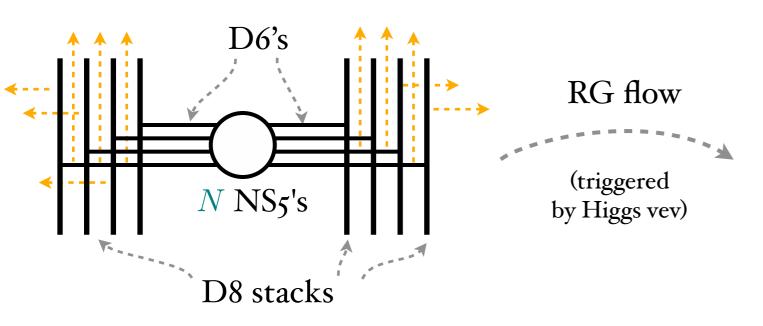


Each D6 on a separate D8: Dirichlet b.c. for fields on the D6.

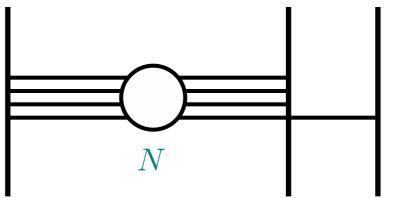
Adapting methods developed in [Gaiotto, Witten '08] for 3d theories



brane configurations studied long ago in [Hanany, Zaffaroni '97; Brunner, Karch '97]



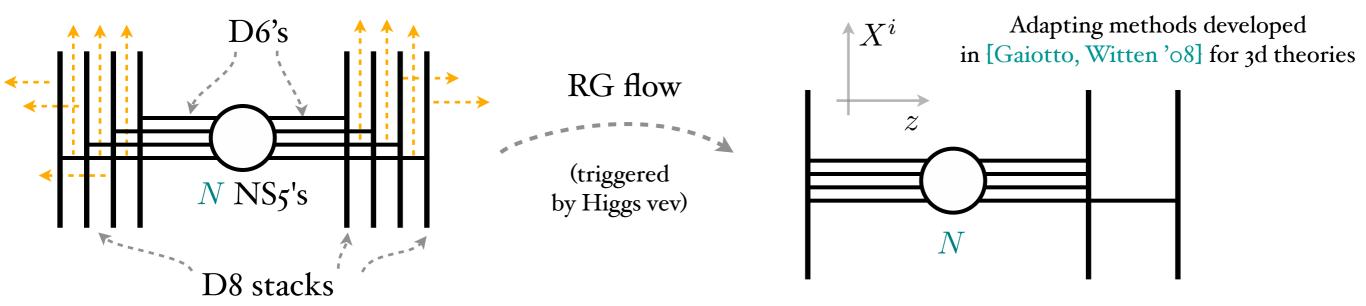
Adapting methods developed in [Gaiotto, Witten '08] for 3d theories



Each D6 on a separate D8: Dirichlet b.c. for fields on the D6.

brane configurations studied long ago in [Hanany, Zaffaroni '97; Brunner, Karch '97]

Would the D8 survive a near-horizon limit?



Each D6 on a separate D8: Dirichlet b.c. for fields on the D6.

brane configurations studied long ago in [Hanany, Zaffaroni '97; Brunner, Karch '97]

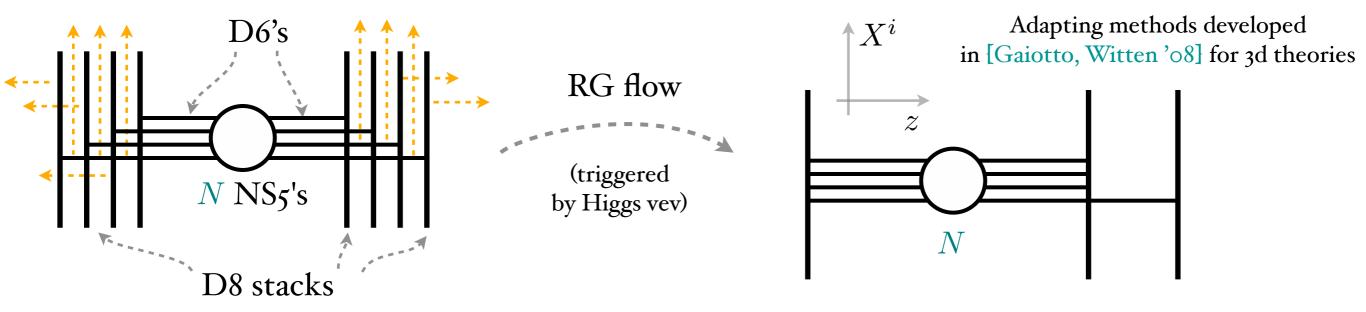
Would the D8 survive a near-horizon limit?

D8's can be thought of as Nahm poles for the D6's.

$$X^i \sim \frac{t_i}{z}$$

BPS equations on D6: Nahm equations

$$\partial_z X^1 = [X^2, X^3]$$
 etc.



Each D6 on a separate D8: Dirichlet b.c. for fields on the D6.

brane configurations studied long ago in [Hanany, Zaffaroni '97; Brunner, Karch '97]

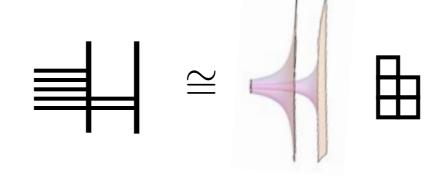
Would the D8 survive a near-horizon limit?

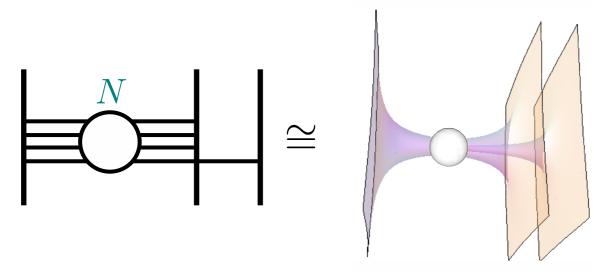
D8's can be thought of as Nahm poles for the D6's.

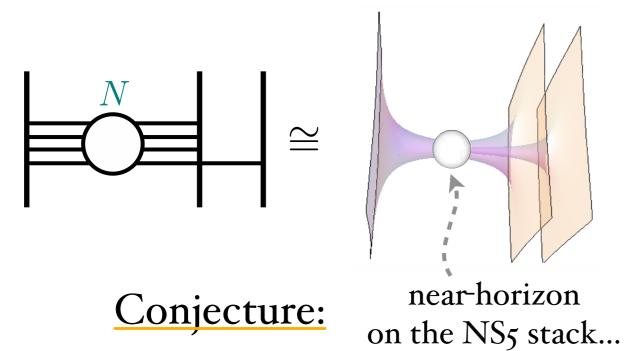
$$X^i \sim \frac{t_i}{z}$$
 su(2) subalgebra of su(k) \cong Young diagram

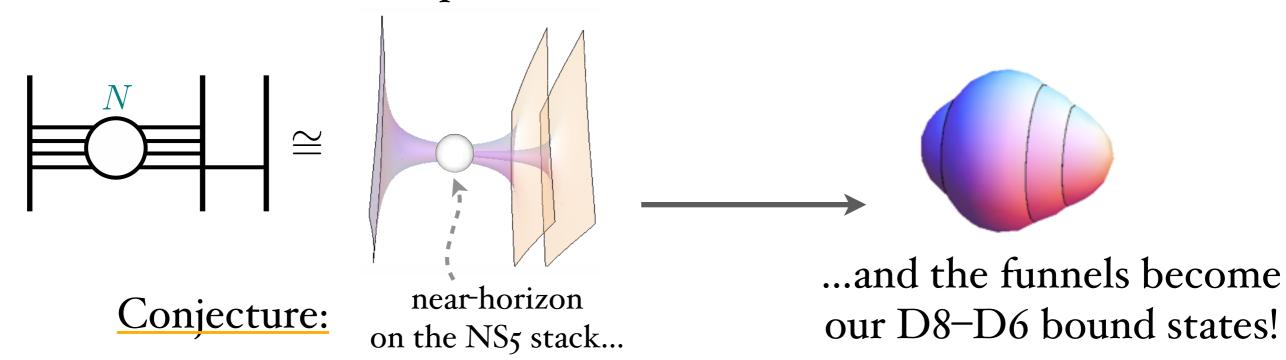
BPS equations on D6: Nahm equations

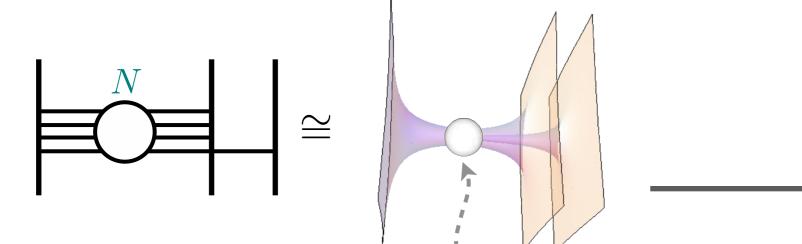
$$\partial_z X^1 = [X^2, X^3]$$
 etc.





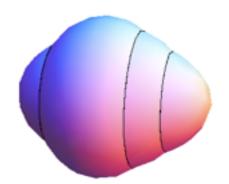












...and the funnels become our D8-D6 bound states!

More precisely:

D6's ending on a D8 ←

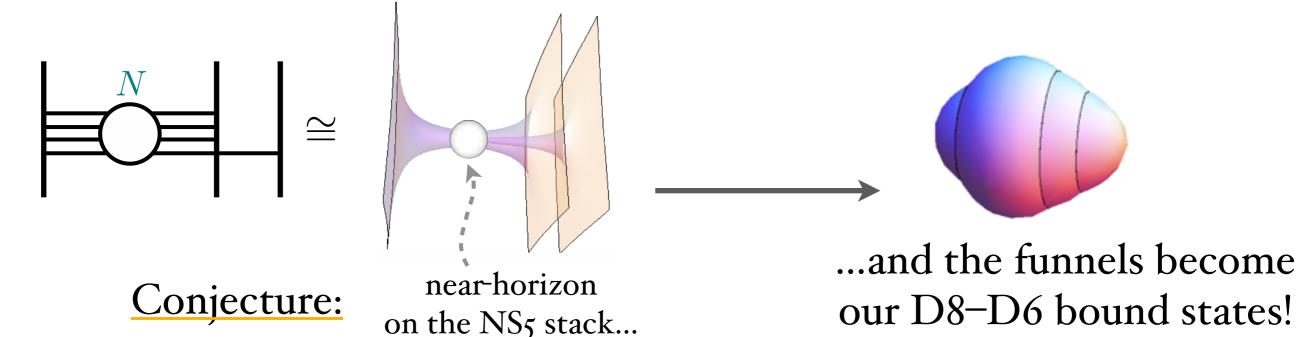
$$\longleftrightarrow$$

 $\mu \equiv D6$ charge of the D8

$$N =$$
NS5's



flux integer $\int_{M_3} H$



More precisely:

 $\mu \equiv D6$ charge of the D8

$$N =$$
NS5's

$$\longleftrightarrow$$

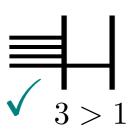
flux integer $\int_{M_3} H$

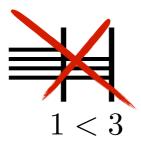
Indeed the brane pictures would generically lead to predict a CFT:

[Hanany, Zaffaroni '97; Brunner, Karch '97]

• nontrivial moduli spaces [singularities in the Higgs moduli space of massless theory]

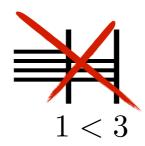
• ordering constraint in [Gaiotto, Witten '08]



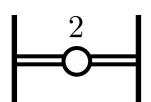


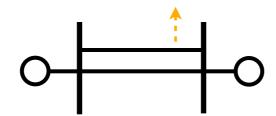
• ordering constraint in [Gaiotto, Witten '08]



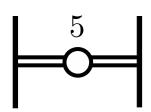


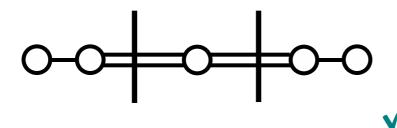
• separating the NS5's \longrightarrow tensor branch, effective quiver description:



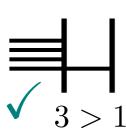


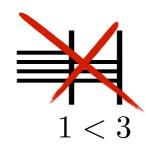
not a CFT: presence of free hypers





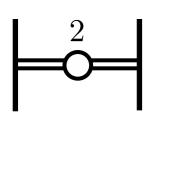
• ordering constraint in [Gaiotto, Witten '08]

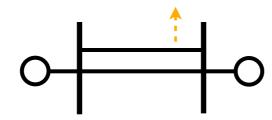




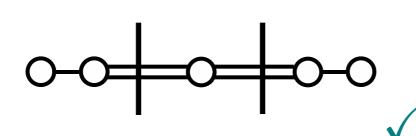


- μ_i monotonically increasing on both sides of $F_0 = 0$
- separating the NS5's \longrightarrow tensor branch, effective quiver description:





not a CFT: presence of free hypers

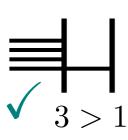


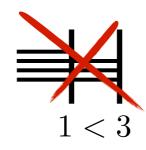
$$\bullet \ N \ge |\mu_1^{\rm L}| + |\mu_1^{\rm R}|$$

bordering $F_0 = 0$ region.

same constraints as for AdS7:

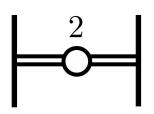
• ordering constraint in [Gaiotto, Witten '08]

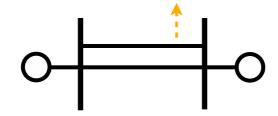




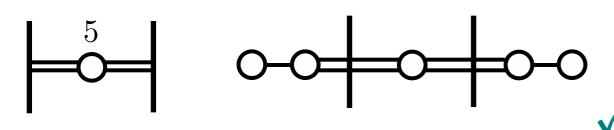


- μ_i monotonically increasing on both sides of $F_0 = 0$
- separating the NS5's \longrightarrow tensor branch, effective quiver description:





not a CFT: presence of free hypers



$$\bullet \ N \ge |\mu_1^{\rm L}| + |\mu_1^{\rm R}|$$

bordering $F_0 = 0$ region.

same constraints as for AdS7:

One-to-one correspondence with AdS7 solutions!

Coda: Comparison to F-theory

[wip. with del Zotto, Heckman, Vafa]; see also Vafa's talk

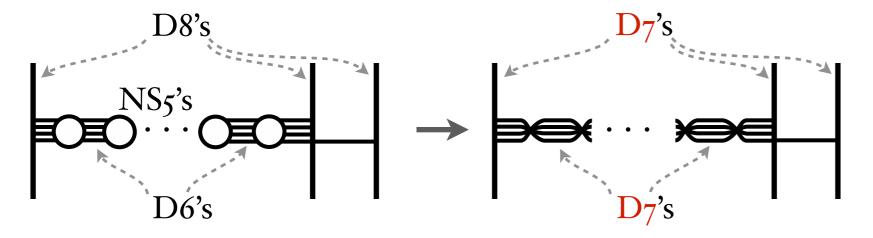
Many new (1,0) CFTs from chains of intersecting curves

[Heckman, Morrison, Vafa '13]

Many new (1,0) CFTs from chains of intersecting curves

[Heckman, Morrison, Vafa '13]

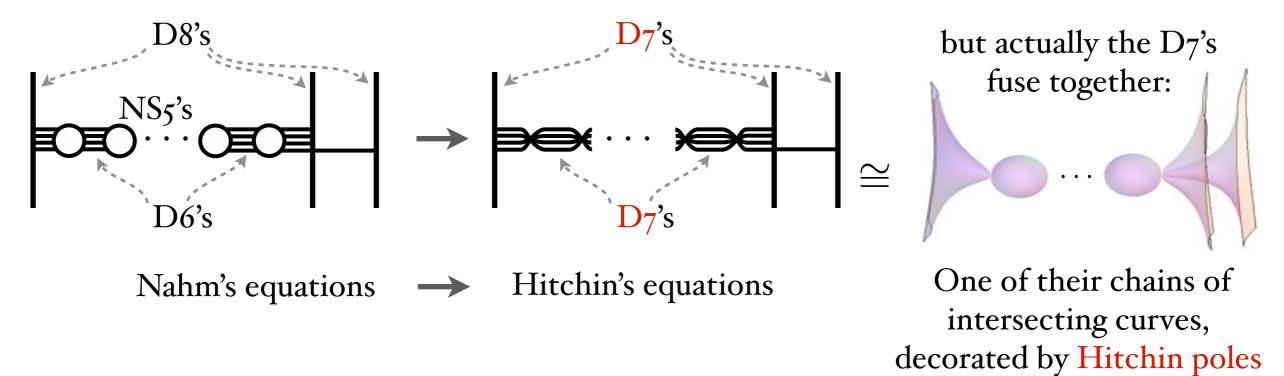
• one T-duality:



Many new (1,0) CFTs from chains of intersecting curves

[Heckman, Morrison, Vafa '13]

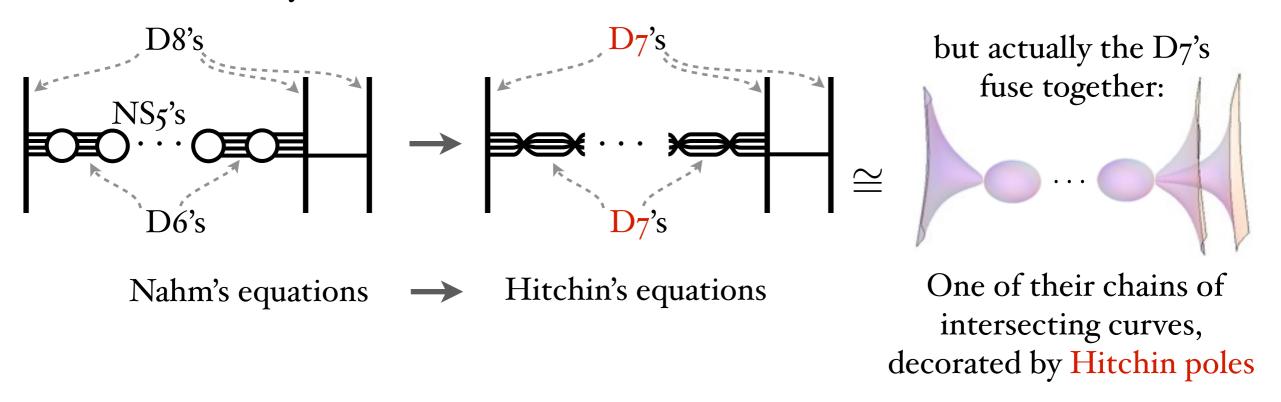
• one T-duality:



Many new (1,0) CFTs from chains of intersecting curves

[Heckman, Morrison, Vafa '13]

• one T-duality:



This suggests that one should add Hitchin poles to the chains of non-perturbative F-theory 7-branes as well.

• some chains with exceptional gauge groups also have gravity duals in M-theory

 some chains with exceptional gauge groups also have gravity duals in M-theory

e.g. a chain of curves with self-intersection 12; 1, 2, 2, 3, 1, 5, 1, 3, 2, 2, 1, 12; 1, 2, 2, . . . pattern repeated N times and gauge groups $\widetilde{SU(2) \times G_2 \times F_4 \times G_2 \times SU(2) \times E_8} \times SU(2) \times \dots$

"fractional M5's"

is dual to $AdS_7 \times S^4/\Gamma_{E_8}$

IV. AdS₆

[Apruzzi, Fazzi, Passias, Rosa, AT '13]

IV. AdS₆

[Apruzzi, Fazzi, Passias, Rosa, AT '13]

IIA:

- no solution for $F_0 = 0$
- one solution for $F_0 \neq 0$

near-horizon of D4's near D8-O8 wall [Brandhuber, Oz'99]

unique: [Passias '12]

[Apruzzi, Fazzi, Passias, Rosa, AT '13]

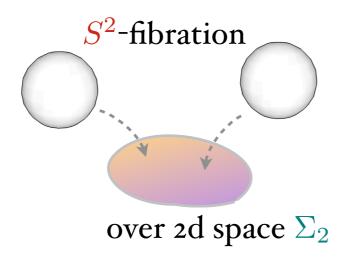
IIA:

- no solution for $F_0 = 0$
- one solution for $F_0 \neq 0$

near-horizon of D4's near D8-O8 wall [Brandhuber, Oz'99]

unique: [Passias '12]

IIB: again we determined the local form of the metric:



the S^2 realizes the SU(2) R-symmetry of a 5d theory.

we also determined all fluxes; they obey Bianchi automatically we have reduced the problem to 2 first-order PDEs on Σ_2 for warping and dilaton

we have reduced the problem to 2 first-order PDEs on Σ_2 for warping and dilaton

two known solutions:

abelian and non-abelian [non-compact!]
T-dual of D4-D8-O8

[Cvetic, Lu, Pope, Vazquez-Poritz '00; Lozano, Colgain, Sfetsos, Rodriguez-Gomez '12]

we have reduced the problem

to 2 first-order PDEs on Σ_2

for warping and dilaton

two known solutions:

abelian and non-abelian [non-compact!]
T-dual of D4-D8-O8

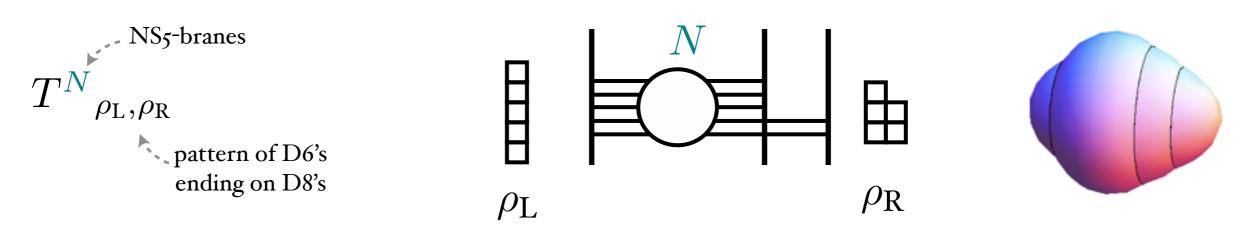
[Cvetic, Lu, Pope, Vazquez-Poritz '00; Lozano, Colgain, Sfetsos, Rodriguez-Gomez '12]

Expected solutions: near-horizon limits of (p,q)-webs (p,q)-fivebranes (p,q)-sevenbranes

e.g. [Aharony, Hanany '97; deWolfe, Hanany Iqbal, Katz '99; Benini, Benvenuti, Tachikawa '08; Bergman, Rodriguez-Gomez '12]

Conclusions

• Gravity duals for infinite family of (1,0) 6d CFTs



- with effective quiver description on 'tensor branch'
- Possible generalizations: include O6's, O8's
- Hints of more general story from F-theory
- Gravity duals for 5d CFTs?