Novel BPS Wilson Loops in Quiver Chern-Simons-matter theories

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- ► The VEV of a circular half-BPS Wilson loop can be computed exactly using localization at finite 't Hooft coupling and finite N [Pestun, 07].
- ► This VEV is a nontrivial function of the coupling constant, interpolating between weak coupling results from perturbative field theory and strong coupling results (in Large N limit) from string theory side [Berestein etal, 98][Drukker, Gross, Ooguri 99].

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ABJM theory

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- ▶ This theory is low energy effective theory of N M2-branes put at $\mathbf{C}_4/\mathbf{Z}_k$.
- ▶ It is holographically dual to M-theory on $AdS_4 * S^7/Z_k$ or type IIA string theory on $AdS_4 \times CP^3$.

▶ BPS Wilson loop in ABJM theory was constructed in [Drukker, Plefka, Young (DPY), 08][Chen, JW, 08] [Rey, Suyama, Yamaguchi(RSY), 08].



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- Such Wilson loop is 1/6 BPS when it is along a line or a circle. It is closely related to 1/2- (1/3-)BPS Wilson loop in generic $\mathcal{N}=2(3)$ Chern-Simons-matter (CSM) theories in [Gaiotto, Yin (GY), 07].

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- ► To provide a matrix model calculation for the VEV of 1/6 BPS circular Wilson loop was the original motivation for Kapustin, Willett and Yaakov to develop the localization in 3d CSM theories.

[Marino, lecture notes, 11]



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- Such loop was finally constructed by *Drukker and Trancanelli* (*DT*) in 2009 by including the fermions in the construction and build a super-connection.
- ► This construct was elegantly explained by *K. Lee and S. Lee in 2010* via the *Brout-Englert-Higgs* mechanism.

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- ▶ 2/5-BPS DT-type Wilson loops in $\mathcal{N}=5$ CSM theories ([Hosomichi, Lee³, Park, 0806], [ABJ, 08]) were found by K. Lee and S. Lee.
- ▶ 1/2-BPS DT-type Wilson loops in $\mathcal{N}=4$ CSM theories[HLLLP, 0805][for $\mathcal{N}=4$ orbifold ABJM theory, Benna etal, 08] were constructed in [Ouyang, JW, Zhang, 1506][Cooke, Drukker, Trancanelli, 1506].

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- ► The previous results may tend to let people feel that DT type Wilson loops are very rare and their existence requires that the theory have a quite large number of supersymmetries.
- DT type Wilson loops also seem to preserve more supersymmetries than the GY type Wilson loops when they are along the same contour.
- ► Taken home message of this talk is that both these two speculations are *incorrect*.

$\mathcal{N}=2$ quiver CSM theories - vector multiplets

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- Let us pick two adjacent nodes in the quiver diagram and the corresponding gauge group are $U(N_1)$ and $U(N_2)$. The Chern-Simons levels are k_1 and k_2 , respectively.

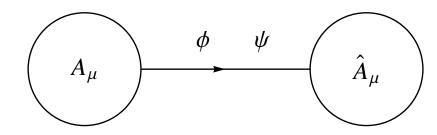
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- Let us pick two adjacent nodes in the quiver diagram and the corresponding gauge group are $U(N_1)$ and $U(N_2)$. The Chern-Simons levels are k_1 and k_2 , respectively.
- ▶ The vector multiplet for gauge group $U(N_1)$ include A_{μ}, σ, χ, D and the last three fields are the auxiliary fields. Similarly for gauge group $SU(N_2)$ we have the vector multiplet $\hat{A}_{\mu}, \hat{\chi}, \hat{\sigma}, \hat{D}$.

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$\mathcal{N}=2$ quiver CSM theories - chiral multiplets

▶ The chiral multiplet in the bifunamental representation of $U(N_1) \times U(N_2)$ includes the scalar ϕ , the spinor ψ and the auxiliary field F.



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Supersymmetry transformation

▶ For the vector multiplet part, we only need the off-shell supersymmetry transformation of $A_{\mu}, \sigma, \hat{A}_{\mu}, \hat{\sigma}$ is,

$$\delta A_{\mu} = \frac{1}{2} (\bar{\chi} \gamma_{\mu} \theta + \bar{\theta} \gamma_{\mu} \chi), \quad \delta \sigma = -\frac{i}{2} (\bar{\chi} \theta + \bar{\theta} \chi),
\delta \hat{A}_{\mu} = \frac{1}{2} (\bar{\hat{\chi}} \gamma_{\mu} \theta + \bar{\theta} \gamma_{\mu} \hat{\chi}), \quad \delta \hat{\sigma} = -\frac{i}{2} (\bar{\hat{\chi}} \theta + \bar{\theta} \hat{\chi}). \quad (1)$$

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$$\delta \hat{A}_{\mu} = \frac{1}{2} (\bar{\chi} \gamma_{\mu} \theta + \bar{\theta} \gamma_{\mu} \hat{\chi}), \quad \delta \hat{\sigma} = -\frac{i}{2} (\bar{\chi} \theta + \bar{\theta} \hat{\chi}). \quad (1)$$

 \blacktriangleright For the matter part we only need the off-shell supersymmetry transformation of ϕ and ψ

$$\delta\phi = i\bar{\theta}\psi, \quad \delta\bar{\phi} = i\bar{\psi}\theta,$$

$$\delta\psi = (-\gamma^{\mu}D_{\mu}\phi - \sigma\phi + \phi\hat{\sigma})\theta + i\bar{\theta}F,$$

$$\delta\bar{\psi} = \bar{\theta}(\gamma^{\mu}D_{\mu}\bar{\phi} + \hat{\sigma}\bar{\phi} - \bar{\phi}\sigma) - i\theta\bar{F},$$
(2)

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GY type BPS Wilson loops

In Minkowski spacetime, one can construct a GY type 1/2 BPS Wilson loop along an infinite straight line $x^\mu=\tau\delta_0^\mu$ as

$$W_{\text{GY}} = \mathcal{P} \exp \left(-i \int d\tau L_{\text{GY}}(\tau)\right),$$

$$L_{\text{GY}} = \begin{pmatrix} A_{\mu} \dot{x}^{\mu} + \sigma |\dot{x}| \\ \hat{A}_{\mu} \dot{x}^{\mu} + \hat{\sigma} |\dot{x}| \end{pmatrix}. \tag{3}$$

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 (3)

The preserved SUSY can be denoted as

$$\gamma_0 \theta = i\theta, \quad \bar{\theta}\gamma_0 = i\bar{\theta}.$$
 (4)

DT-type BPS Wilson loops - I

▶ We can also construct the DT type Wilson loop along a line,

$$W_{\rm DT} = \mathcal{P} \exp \left(-i \int d\tau L_{\rm DT}(\tau)\right),$$

$$L_{\rm DT} = \begin{pmatrix} \mathcal{A} & \bar{f}_1 \\ f_2 & \hat{\mathcal{A}} \end{pmatrix},$$

$$\mathcal{A} = A_{\mu} \dot{x}^{\mu} + \sigma |\dot{x}| + m\phi \bar{\phi} |\dot{x}|, \quad \bar{f}_1 = \bar{\zeta}\psi |\dot{x}|,$$

$$\hat{\mathcal{A}} = \hat{A}_{\mu} \dot{x}^{\mu} + \hat{\sigma} |\dot{x}| + n\bar{\phi}\phi |\dot{x}|, \quad f_2 = \bar{\psi}\eta |\dot{x}|.$$
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► To make it preserve the SUSY in (4) at least classically, it is enough to require that [K. Lee, S. Lee, 2010]

$$\delta L_{\rm DT} = \partial_{\tau} G + i[L_{\rm DT}, G], \tag{6}$$

for some Grassmann odd matrix

$$G = \begin{pmatrix} \bar{g}_1 \\ g_2 \end{pmatrix}. \tag{7}$$

DT-type Wilson loops - II

▶ We find that the necessary and sufficient conditions for the existence of such \bar{g}_1 and g_2 are

$$\bar{\zeta}^{\alpha} = \bar{\alpha}(1, i), \quad \eta_{\alpha} = (1, -i)\beta,$$

$$m = n = 2i\bar{\alpha}\beta.$$
(8)

Such DT type Wilson loop is 1/2 BPS, and the preserved SUSY is the same as (4). Note that there are two free complex parameters $\bar{\alpha}$ and β in the Wilson loop, and they can be any complex constants. When $\bar{\alpha}=\beta=0$, it becomes the GY type Wilson loop.

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Generalizations

▶ There could be other matters couple to these two gauge fields. They will change the on-shell values of σ and $\hat{\sigma}$ in the Wilson loops we will construct. The structure of these Wilson loops will not be changed.

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Generalizations

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- \blacktriangleright We also constructed half-BPS circular Wilson loops for $\mathcal{N}=2$ superconformal quiver Chern-Simons theory in Euclidean space.
- The case with multi matter fields in the bifundamental and anti-bifundamental representations were also considered. The DT type Wilson loops can be divided into four classes.

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▶ In ABJM theory, there are four scalars ϕ_I and four fermions ψ_I in the bifundamental representation.

- ▶ In ABJM theory, there are four scalars ϕ_I and four fermions ψ_I in the bifundamental representation.
- ▶ A general GY type Wilson loop along the timelike infinite straight line $x^{\mu} = \tau \delta^{\mu}_{0}$ takes the form

$$W_{\rm GY} = \mathcal{P} \exp\left(-i \int d\tau L_{\rm GY}(\tau)\right),$$

$$L_{\rm GY} = \begin{pmatrix} \mathcal{A}_{\rm GY} \\ \hat{\mathcal{A}}_{\rm GY} \end{pmatrix},$$

$$\mathcal{A}_{\rm GY} = A_{\mu}\dot{x}^{\mu} + \frac{2\pi}{k} R^{I}{}_{J}\phi_{I}\bar{\phi}^{J}|\dot{x}|,$$

$$\hat{\mathcal{A}}_{\rm GY} = \hat{A}_{\mu}\dot{x}^{\mu} + \frac{2\pi}{k} S_{I}{}^{J}\bar{\phi}^{I}\phi_{J}|\dot{x}|.$$
(9)

▶ Up to some SU(4) transformation, the only GY-type Wilson line preserving Ponincare supercharges are the ones with $R^I_{\ J} = S_J^{\ I} = {\rm diag}(-1,-1,1,1).$ They are 1/6-BPS preserving the supersymmetries

$$\gamma_0 \theta^{12} = i\theta^{12}, \quad \gamma_0 \theta^{34} = -i\theta^{34},
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▶ This is just the Wilson loop that was constructed in [DPY][Chen JW][RSY]. Here we show that this is the only form of GY type 1/6 BPS Wilson loops up to some SU(4) transformation. Especially, we find that we do not need to require that $R^I_{\ J}$ or $S_I^{\ J}$ is a hermitian matrix a priori, and we show that it is the result of supersymmetry.

▶ We turn to constructing a DT type Wilson loop along a straight line that preserves at least the supersymmetries (10). A general DT type Wilson loop is

$$W_{\rm DT} = \mathcal{P} \exp \left(-i \int d\tau L_{\rm DT}(\tau)\right),$$

$$L_{\rm DT} = \begin{pmatrix} \mathcal{A} & \bar{f}_1 \\ f_2 & \hat{\mathcal{A}} \end{pmatrix},$$

$$\mathcal{A} = \mathcal{A}_{\rm GY} + \frac{2\pi}{k} M^I{}_J \phi_I \bar{\phi}^J |\dot{x}|,$$

$$\hat{\mathcal{A}} = \hat{\mathcal{A}}_{\rm GY} + \frac{2\pi}{k} N_I{}^J \bar{\phi}^I \phi_J |\dot{x}|,$$

$$\bar{f}_1 = \sqrt{\frac{2\pi}{k}} \bar{\zeta}_I \psi^I |\dot{x}|, f_2 = \sqrt{\frac{2\pi}{k}} \bar{\psi}_I \eta^I |\dot{x}|.$$
(12)

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▶ The supersymmetry conditions give that

$$\bar{\zeta}_{1,2} = \bar{\alpha}_{1,2}\bar{\zeta}, \quad \bar{\zeta}^{\alpha} = (1,i),
\bar{\zeta}_{3,4} = \bar{\gamma}_{3,4}\bar{\mu}, \quad \bar{\mu}^{\alpha} = (1,-i),
\eta^{1,2} = \eta\beta^{1,2}, \quad \eta_{\alpha} = (1,-i),
\eta^{3,4} = \nu\delta^{3,4}, \quad \nu_{\alpha} = (1,i),$$
(13)

$$M^{I}_{J} = N_{J}^{I} = 2i \begin{pmatrix} \bar{\alpha}_{2}\beta^{2} & -\bar{\alpha}_{2}\beta^{1} \\ -\bar{\alpha}_{1}\beta^{2} & \bar{\alpha}_{1}\beta^{1} \\ & & \bar{\gamma}_{4}\delta^{4} & -\bar{\gamma}_{4}\delta^{3} \\ & & -\bar{\gamma}_{3}\delta^{4} & \bar{\gamma}_{3}\delta^{3} \end{pmatrix}.$$
(14)

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- Class I

$$\bar{\gamma}_{3,4} = \delta^{3,4} = 0. \tag{15}$$

Class II

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► Class III

$$\beta^{1,2} = \delta^{3,4} = 0. \tag{17}$$

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- ► Generically these Wilson loops preserving the same SUSY as GY type Wilson loops, i. e., they are 1/6-BPS.
- ► In class I and II, for special parameters in the constructions, the Wilson loops become the half-BPS ones found by Drukker and Trancanelli. Our novel DT type Wilson loops include 1/6-BPS GY type and half-BPS DT type ones as special cases.

DT type Wilson loops in $\mathcal{N}=3,4$ Chern-Simons-matter theories

▶ We found similar pattern in $\mathcal{N}=4$ CSM theories: generally the DT type BPS Wilson loop along a straight line/circle is 1/4 BPS, the same as GY type Wilson loops. For special parameters, supersymmetries preserved by the loops are enhanced to half-BPS.

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- ▶ For $\mathcal{N}=3$ CSM theories, the DT type BPS Wilson loop along a straight line/circle is 1/3-BPS. there is no supersymmetry enhancement here. This is consistent with the results from the dual M-theory side [Chen, JW, Zhu, 14].

Conclusion

 \blacktriangleright We constructed DT-type Wilson loops in general $\mathcal{N}=2$ quiver CSM theories.



Conclusion

- ▶ We constructed DT-type Wilson loops in general $\mathcal{N}=2$ quiver CSM theories.
- ▶ Along a straight line or a circle, the generic DT-type Wilson loops in ABJM theory are 1/6-BPS, which include 1/6-BPS GY-type Wilson loops and half-BPS DT-type Wilson loops as special case.

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Conclusion

- \blacktriangleright We constructed DT-type Wilson loops in general $\mathcal{N}=2$ quiver CSM theories.
- Along a straight line or a circle, the generic DT-type Wilson loops in ABJM theory are 1/6-BPS, which include 1/6-BPS GY-type Wilson loops and half-BPS DT-type Wilson loops as special case.
- ▶ Generically, these 1/6-BPS DT-type Wilson loops are not locally SU(3) invariant. This is different from the Wilson loops constructed in [Cardinali, Griguolo, Martelloni, Seminara, 12].

▶ Cooke, Drukker and Trancanelli argued that classically half-BPS DT-type Wilson loops in $\mathcal{N}=4$ CSM theories may not be truly BPS at the quantum level. Only special linear combinations of these loops will be BPS at the quantum level.



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- ► This idea was supported by recent three loop computations in [Bianchi, Griguolo, Leoni, Mauri, Penati, Seminara, 16] and truly half-BPS Wilson loops were also identified in this paper.

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- ► How to construct the holographical dual of the above BPS Wilson loops?



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Thanks for Your Attention!

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