

# Orientifold Singularities and Duality

Ben Heidenreich (Harvard)

*with Iñaki García Etxebarria (MPI Munich)  
and Timm Wrane (Stanford SITP)*

1210.7799, 1307.1701  
and forthcoming

# Review ( $\mathcal{N} = 4$ )

$$N \text{ D3s} \quad O3$$

● + ×

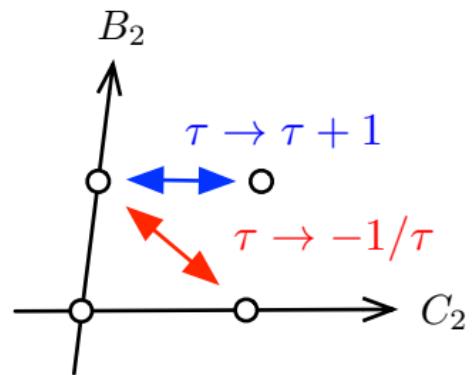
**Montonen-Olive  
Duality**

$$O3^+ : USp(2k)$$

$$O3^- : SO(2k) \quad SO(2k+1)$$

AdS/CFT description:  
(Witten '98)

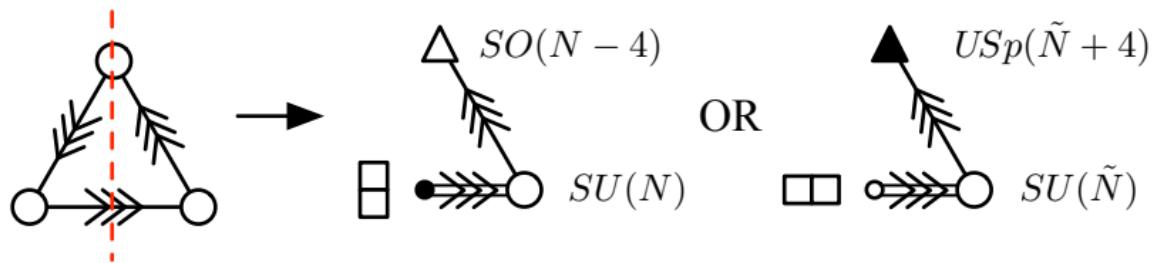
$$H^3(S^5/\mathbb{Z}_2, \tilde{\mathbb{Z}}) \cong \mathbb{Z}_2$$



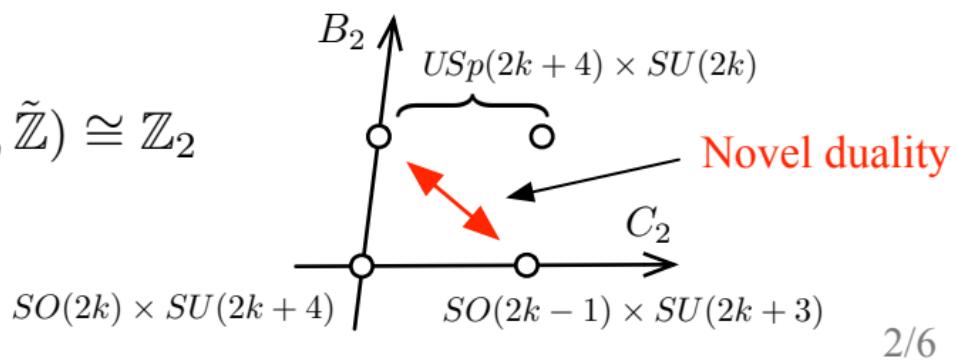
# Orbifolds ( $\mathcal{N} = 1$ )

(BH, García-Etxebarria,  
Wrase '12, '13)

$$\mathbb{C}^3 / \mathbb{Z}_3 : z^i \rightarrow e^{2\pi i / 3} z^i \quad \sigma : z^i \rightarrow -z^i$$

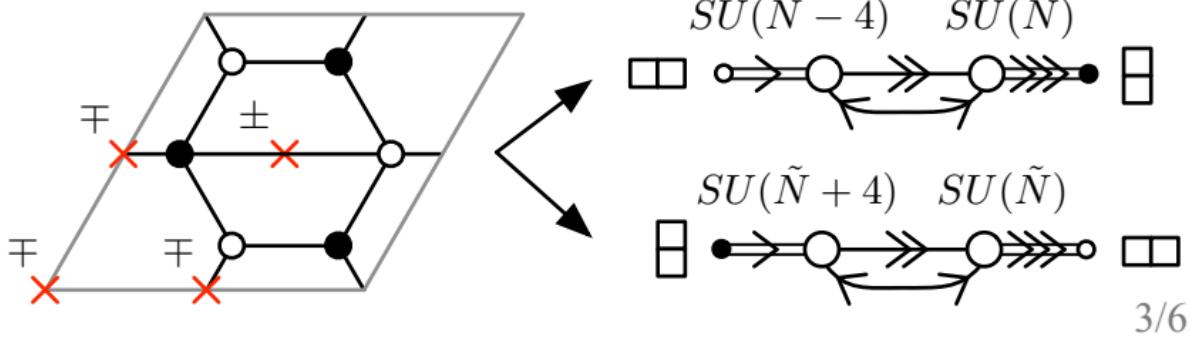
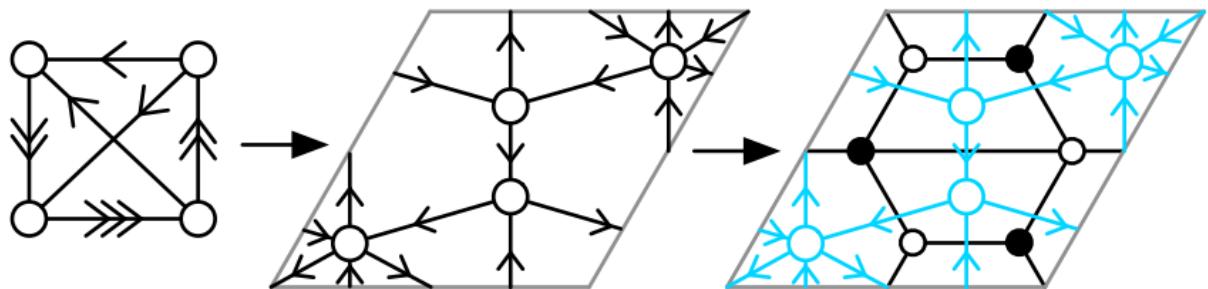


$$H^3(S^5 / \mathbb{Z}_6, \tilde{\mathbb{Z}}) \cong \mathbb{Z}_2$$



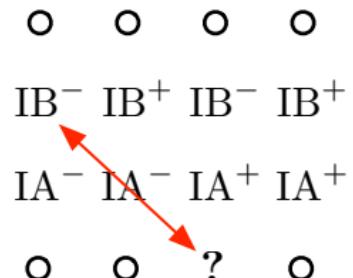
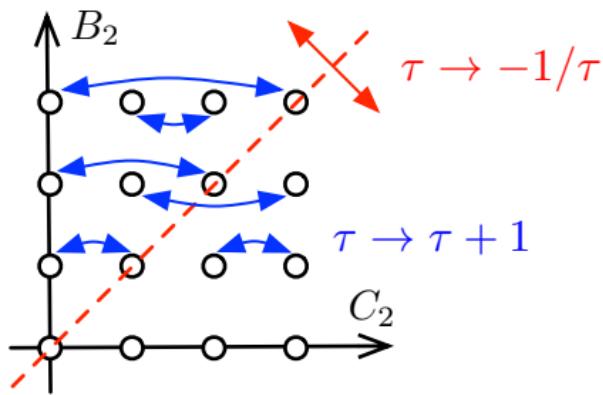
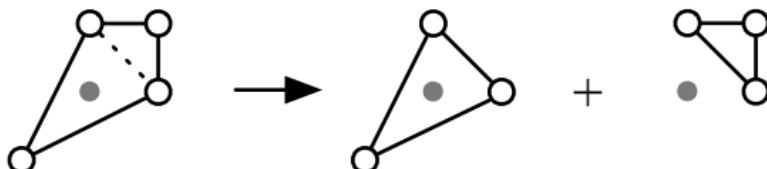
# Beyond Orbifolds

	$x$	$y$	$z$	$w$
$\mathbb{C}^*$	2	2	-1	-3
$\mathbb{Z}_2$	-	-	-	+



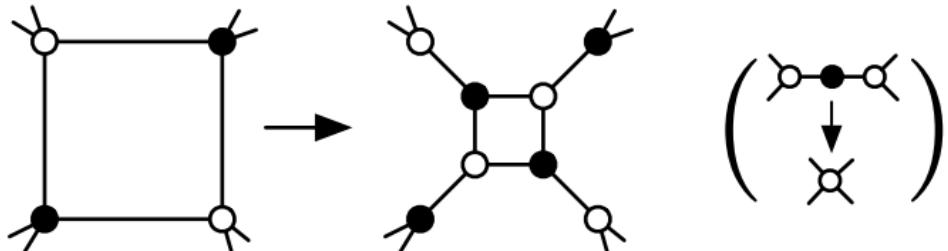
# $dP_1$ Discrete Torsion & Duality

$$H^3 \left( \frac{S^3 \times S^2}{\mathbb{Z}_2}, \tilde{\mathbb{Z}} \right) \cong \mathbb{Z}_2 \oplus \mathbb{Z}_2$$



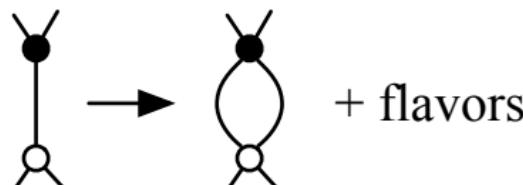
# New Involutions from Deconfinement

Seiberg  
Duality:

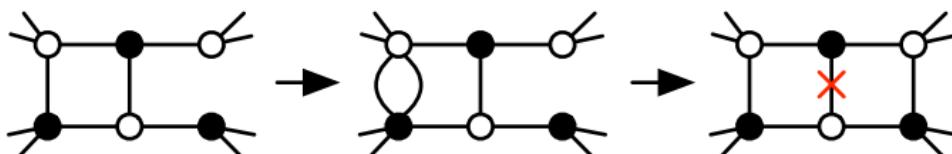


Deconfinement:

(Berkooz '95,  
Pouliot '95)

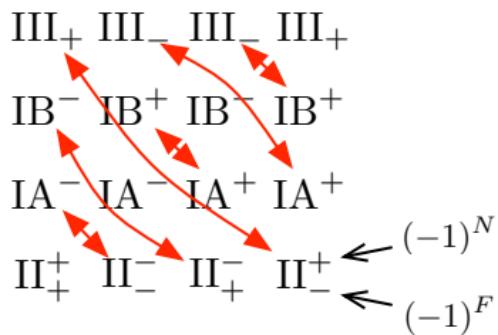
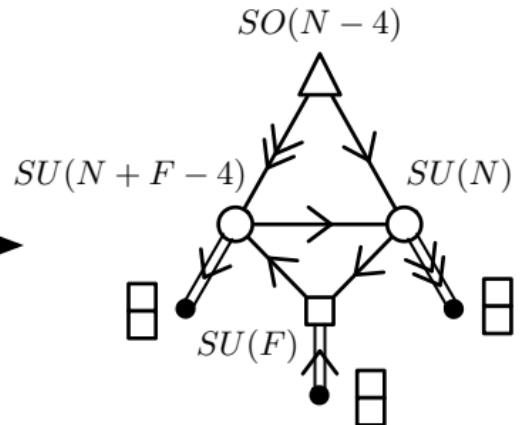
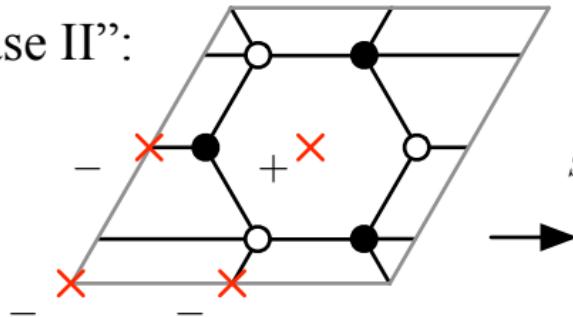


New Involution!



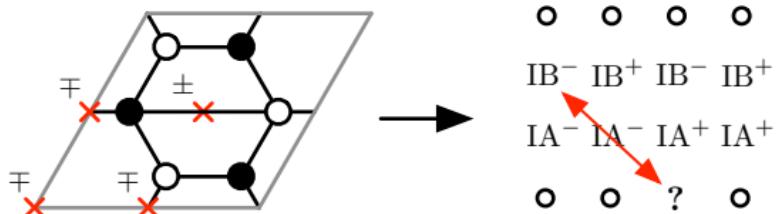
# New $dP_1$ Orientifolds

“Phase II”:

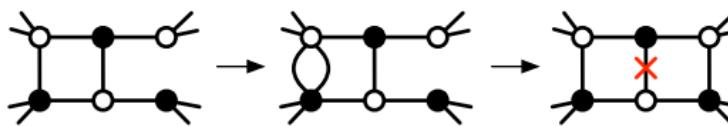


Anomalies, SCI,  
Low  $N$  examples  
match!

$SL(2, \mathbb{Z})$  covariance requires additional  $dP_1$  orientifolds



Constructed by deconfinement of parent theory



Verified by strong duality checks

