

# **Lightrays, Shocks, Strings, and Conformal Colliders**

Alexander Zhiboedov, CERN

Strings 2019, Brussels

based on the joint work with M. Kologlu, P. Kravchuk, D. Simmons-Duffin

(related work with: A. Belitsky, X. Camanho, J. Edelstein, J. Henn, S. Hohenegger, Z. Komargodski, G. Korchemsky, M. Kulaxizi, J. Maldacena, A. Parnachev, E. Sokatchev, K. Yan)

# Introduction

Consider a unitary QFT in  $d > 2$ . Assume a stress tensor

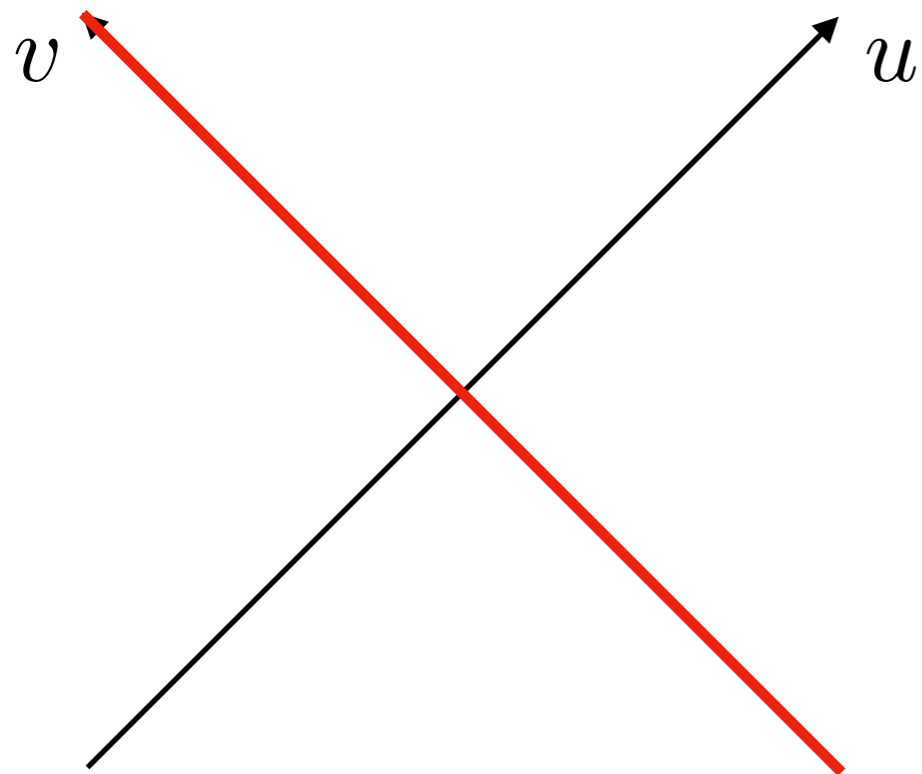
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# Introduction

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$$\partial_\mu T^{\mu\nu} = 0$$

$$ds^2 = -dudv + d\vec{y}^2 \quad \vec{y} \in \mathbb{R}^{d-2}$$



The ANEC operator (energy density):

$$\mathcal{E}(\vec{y}) = \int_{-\infty}^{\infty} dv T_{vv}(0, v, \vec{y}) \geq 0$$

[Faulkner, Leigh, Parrikar, Wang 16']

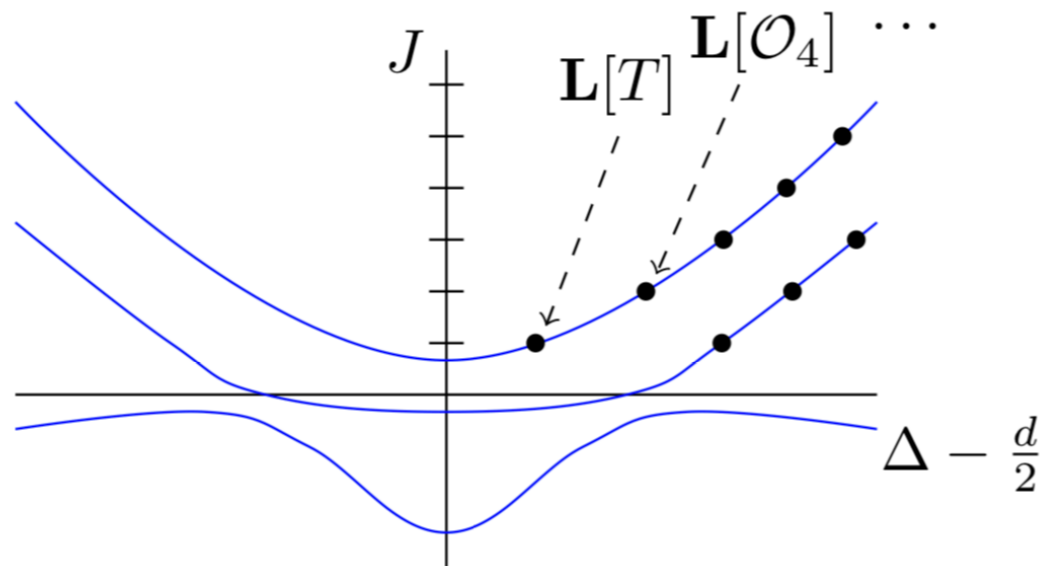
[Hartman, Kundu, Tajdini 16']

# ANECology

[Review talk by T. Hartman, Strings 2018]  
 [Review talk by D. Simmons-Duffin, Strings 2018]

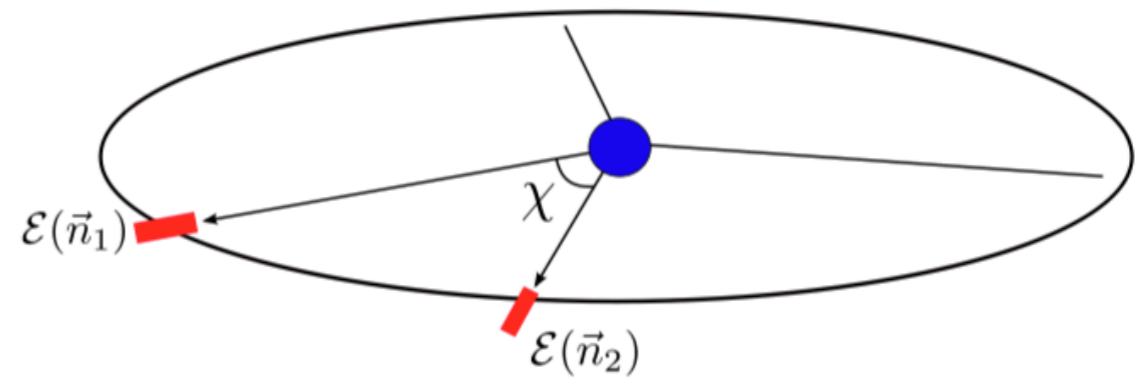
The ANEC operator has many appearances and applications.

**light-ray operators (lightrays)**



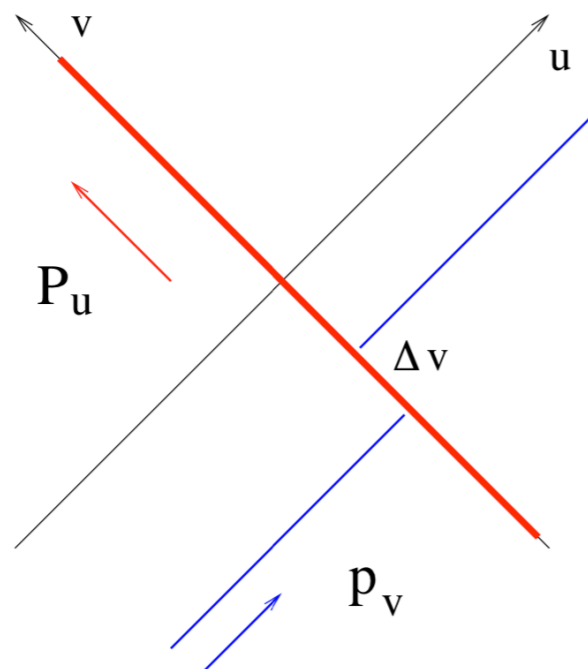
[Kravchuk, Simmons-Duffin '18]

**event shapes**



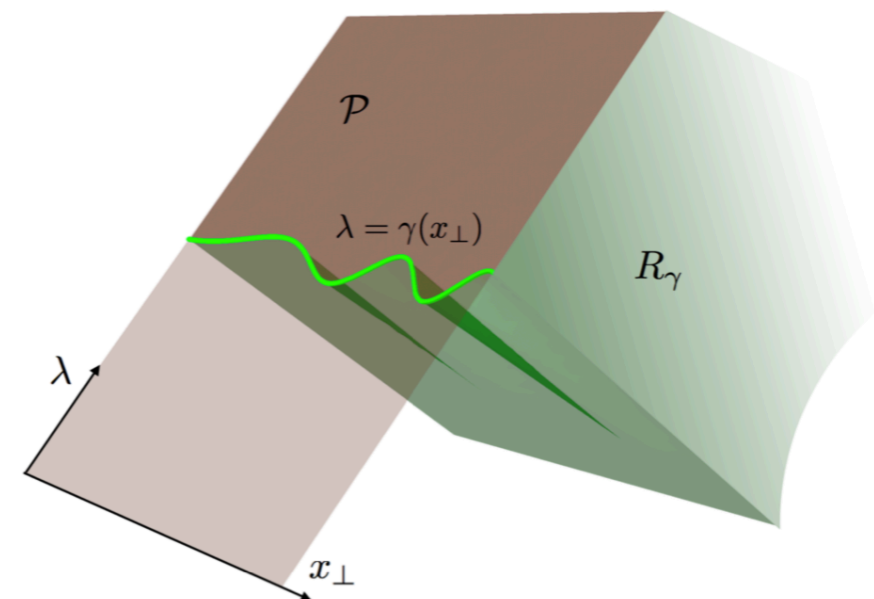
[Hofman, Maldacena '08]

**gravitational shocks**



[Afkhani-Jeddi, Hartman, Kundu, Tajdini '17]

**QIT**



[Casini, Testé, Torroba '18]

# ANECology

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**1-point:**  $\langle \Psi' | \mathcal{E}(\vec{y}) | \Psi \rangle$

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in a unitary  $d > 2$  CFT.

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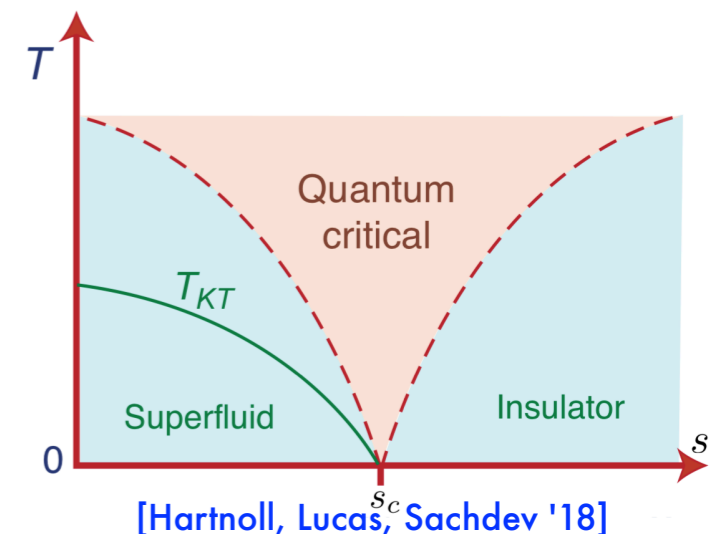
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**2-point\*:**  $\langle \Psi' | \mathcal{E}(\vec{y}_1) \mathcal{E}(\vec{y}_2) | \Psi \rangle$   $|\Psi\rangle = \mathcal{O}|\Omega\rangle$

in a unitary  $d > 2$  CFT.

\*

This is just a particular example of a generic class of observables that involve light-ray operators in Lorentzian CFTs.



## **Part I:           new lightray technology**

- convergence and commutativity
- local  $\times$  lightray OPE
- lightray  $\times$  lightray OPE

## **Part II:           applications**

- Deriving AdS gravity from CFT
- Conformal collider physics



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# Commutativity of ANECs

**Q:** Do ANEC operators commute?

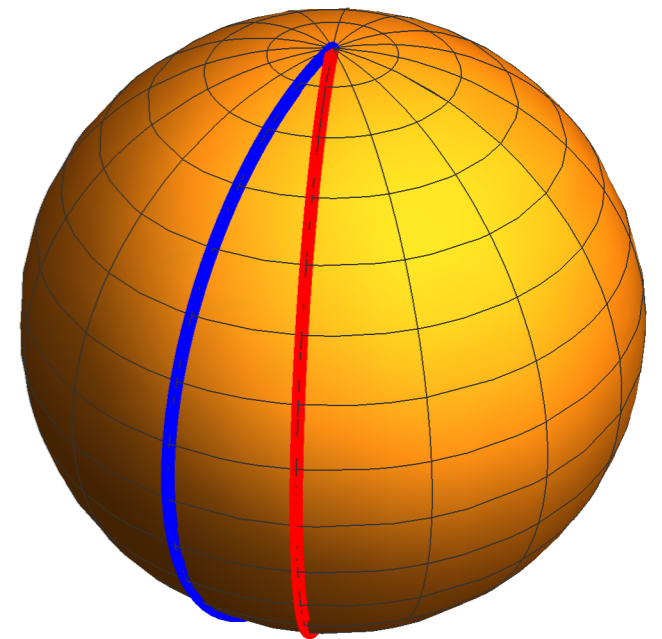
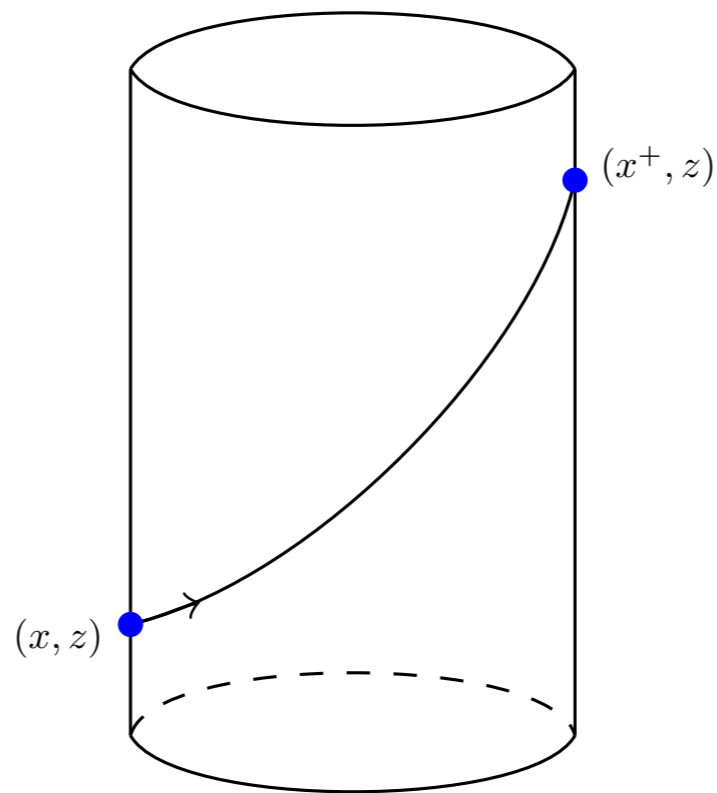
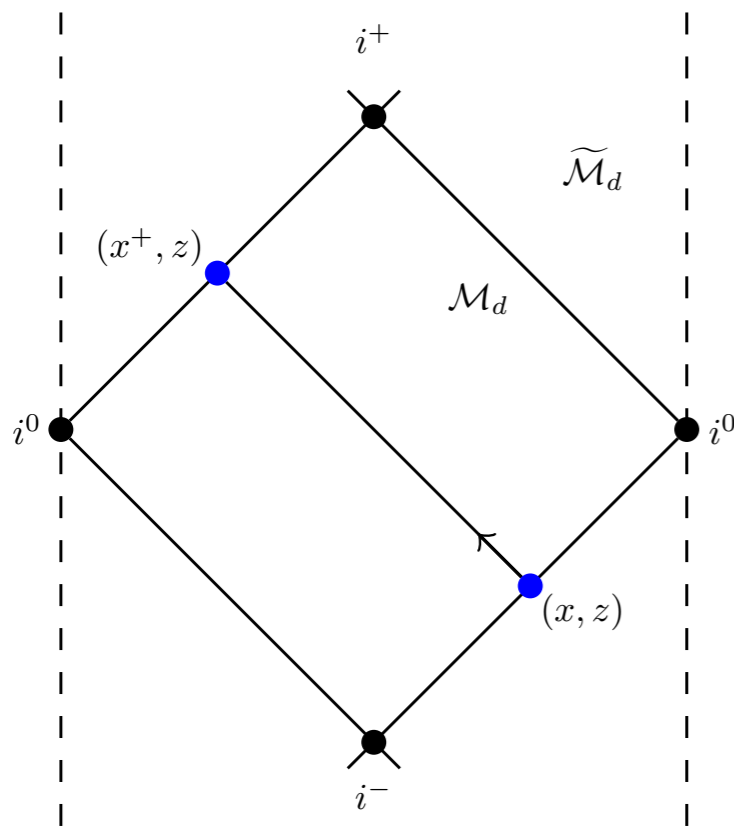
$$[\mathcal{E}(\vec{y}_1), \mathcal{E}(\vec{y}_2)] \stackrel{?}{=} 0 \quad \mathcal{E}(\vec{y}) = \int_{-\infty}^{\infty} dv T_{vv}(0, v, \vec{y})$$

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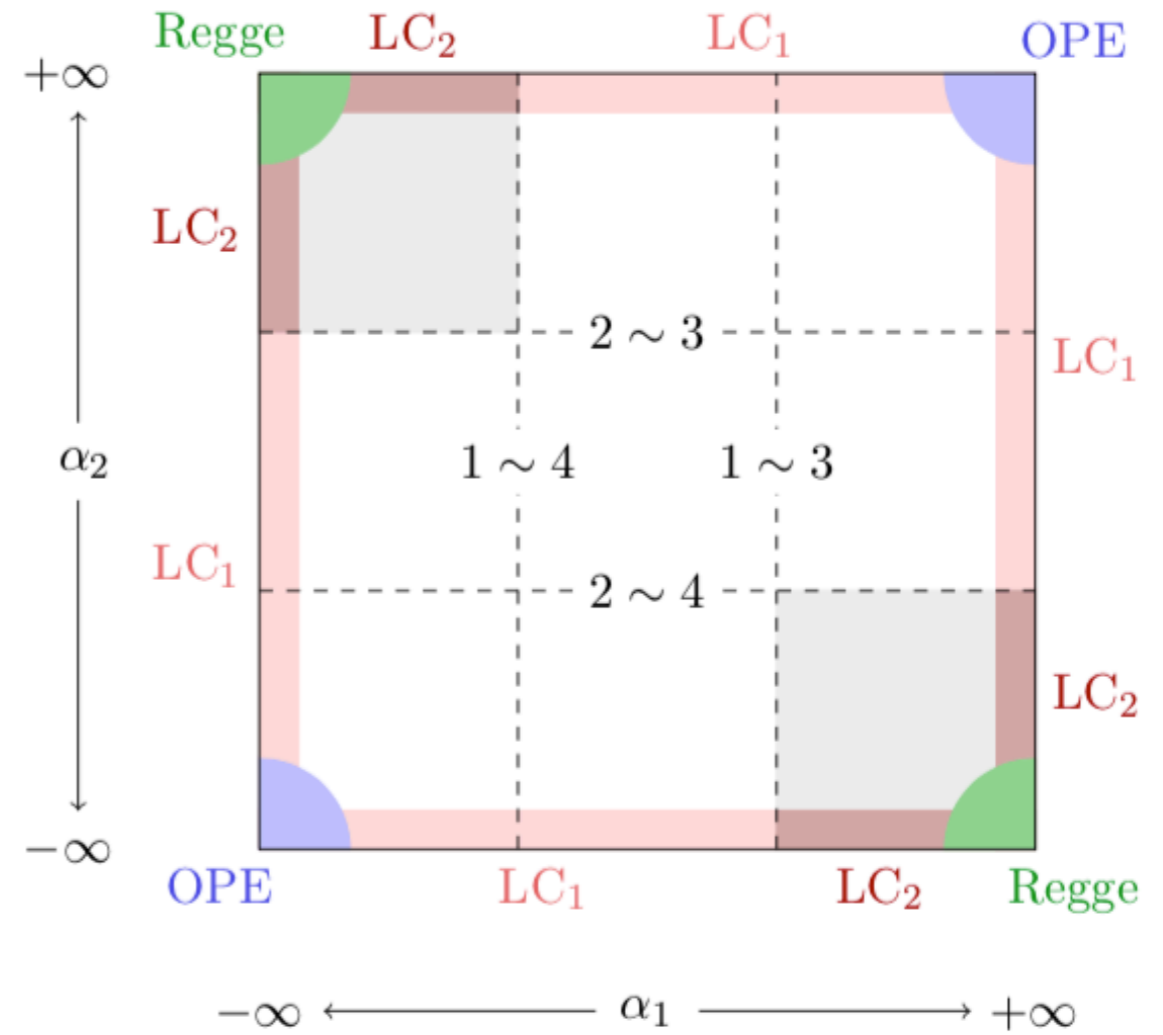
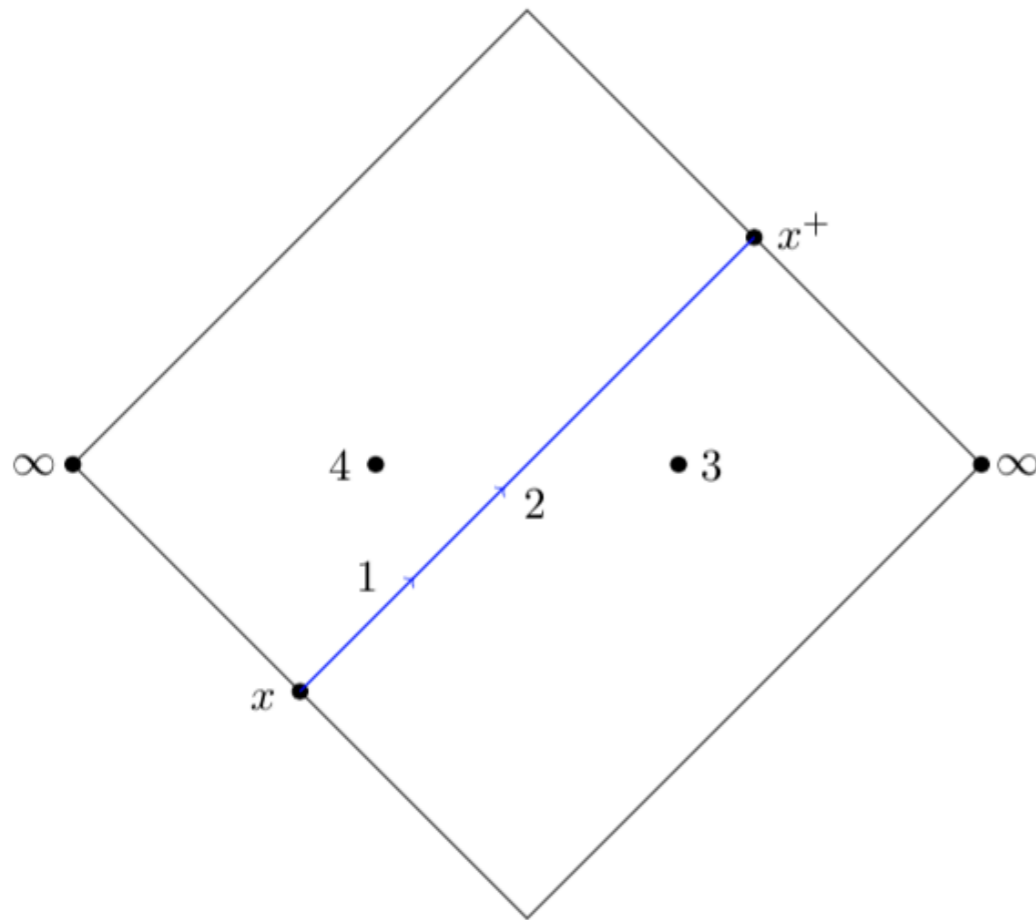
$$[\mathcal{E}(\vec{y}_1), \mathcal{E}(\vec{y}_2)] \stackrel{?}{=} 0 \quad \mathcal{E}(\vec{y}) = \int_{-\infty}^{\infty} dv T_{vv}(0, v, \vec{y})$$

They are not space-like separated at the endpoints.

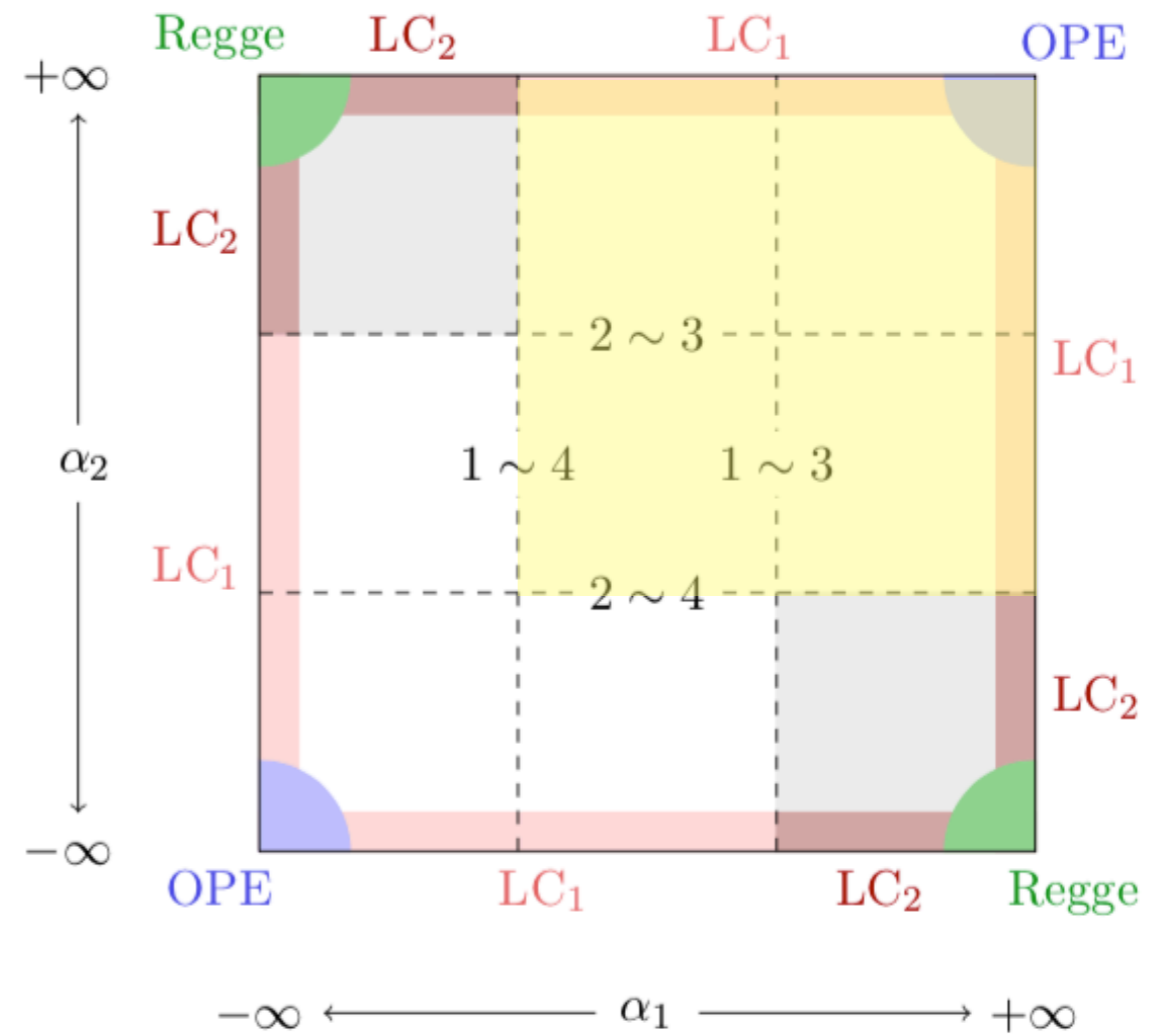
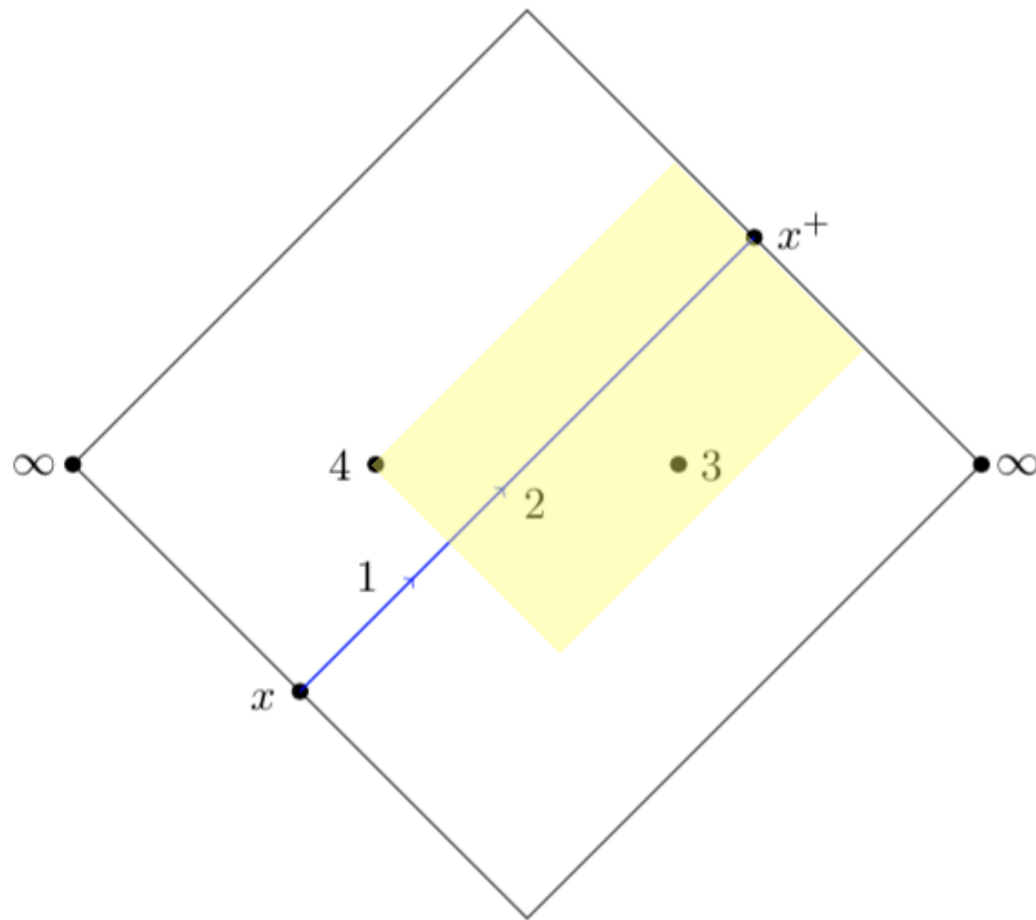


$\mathbf{L}[T](x, z_1)\mathbf{L}[T](x, z_2)$   
**light transform**

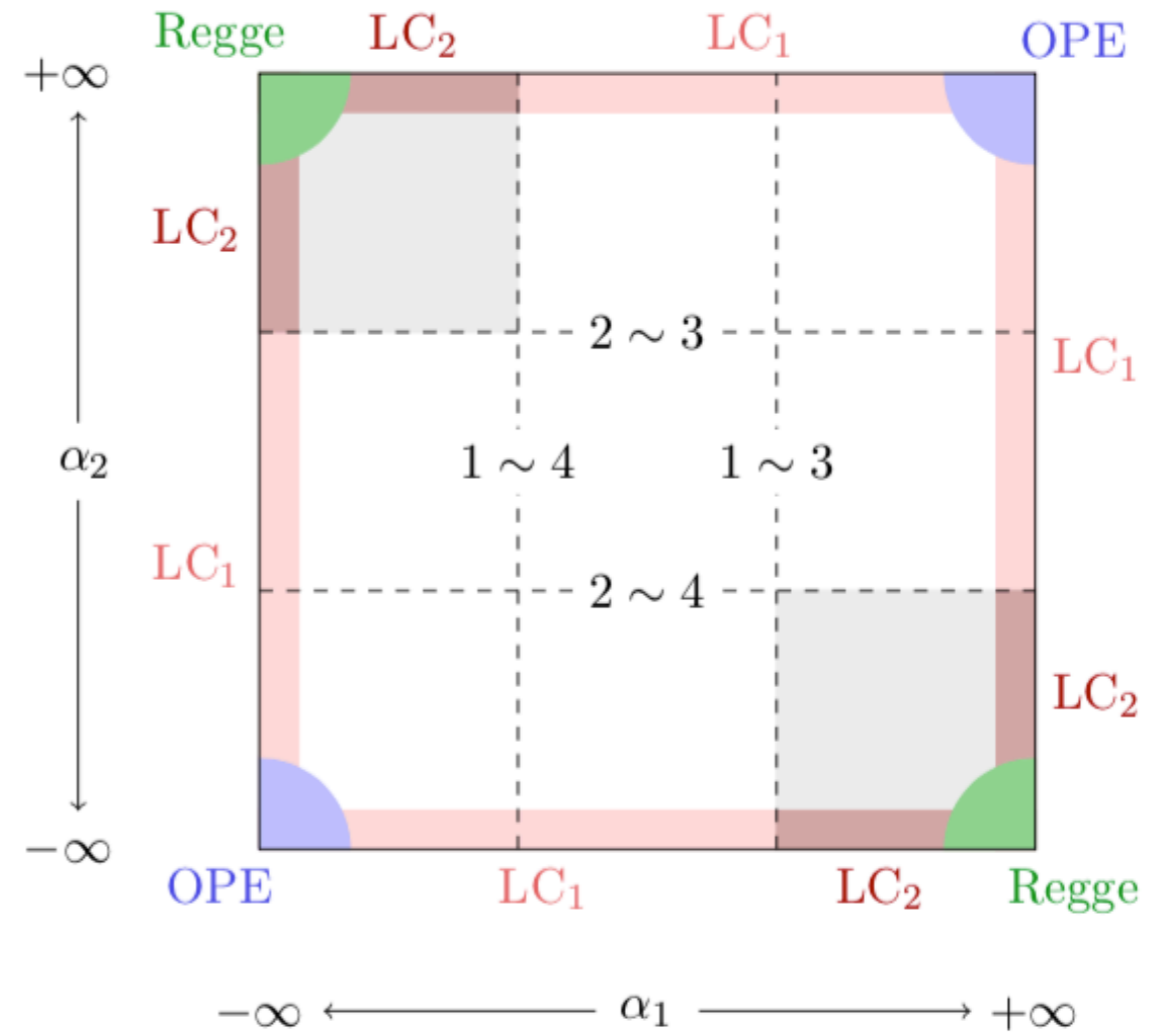
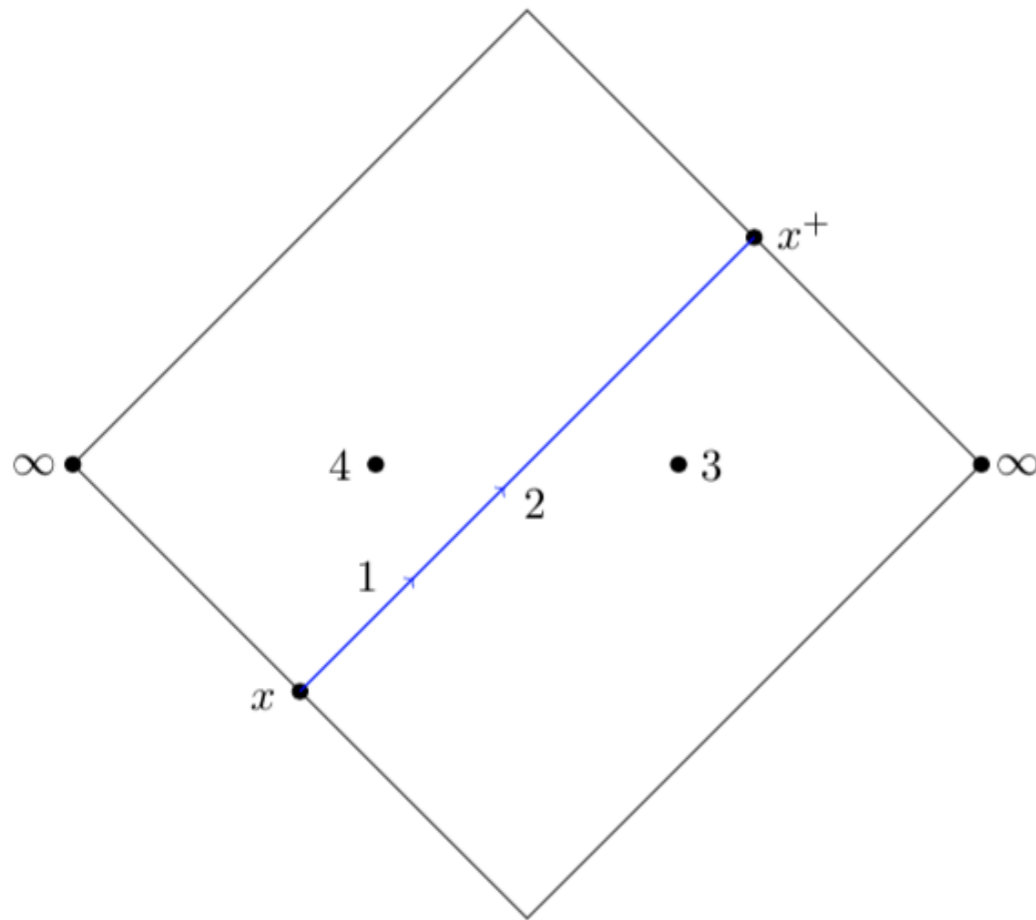
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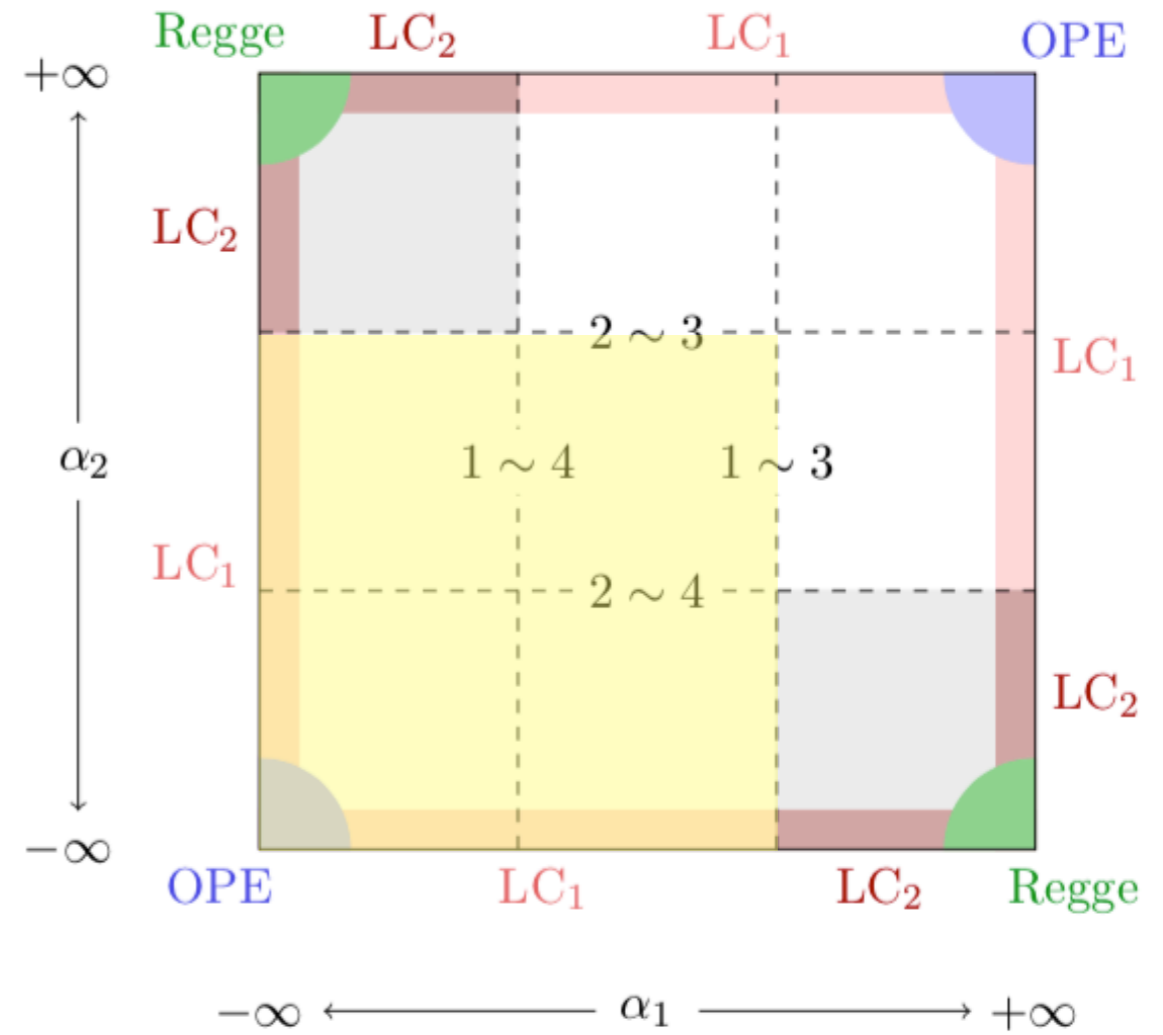
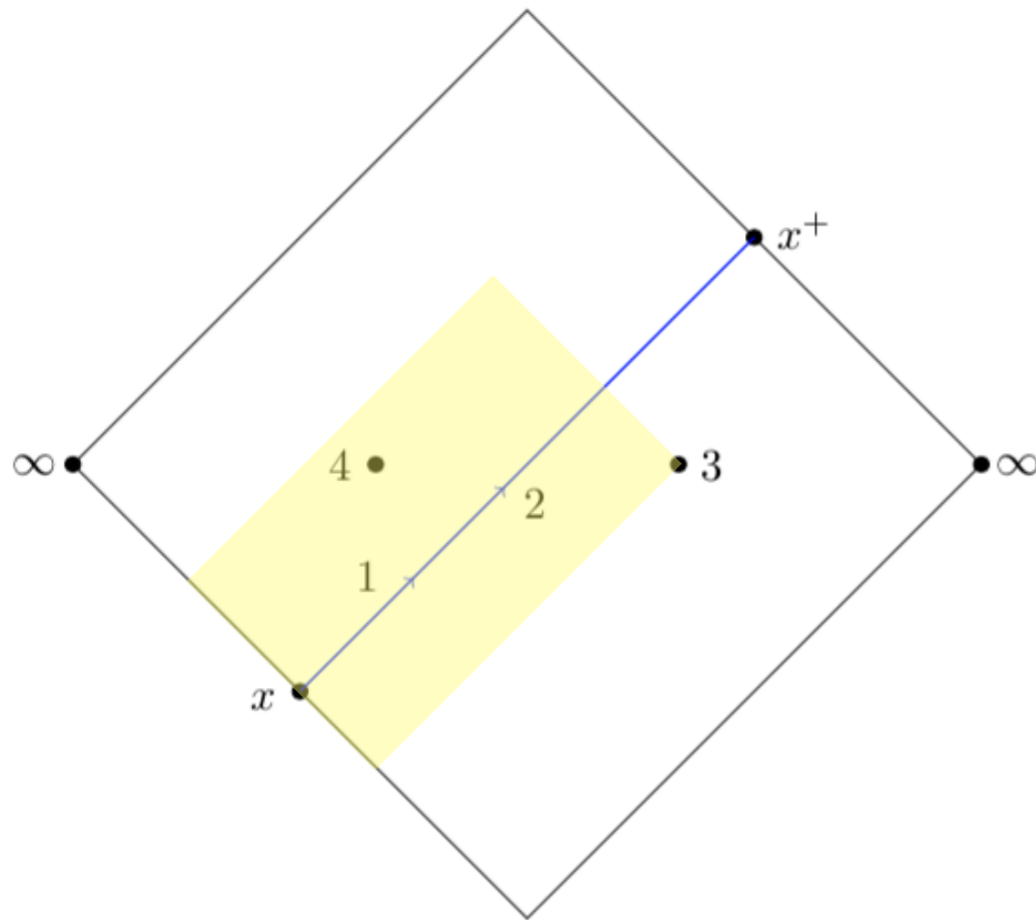
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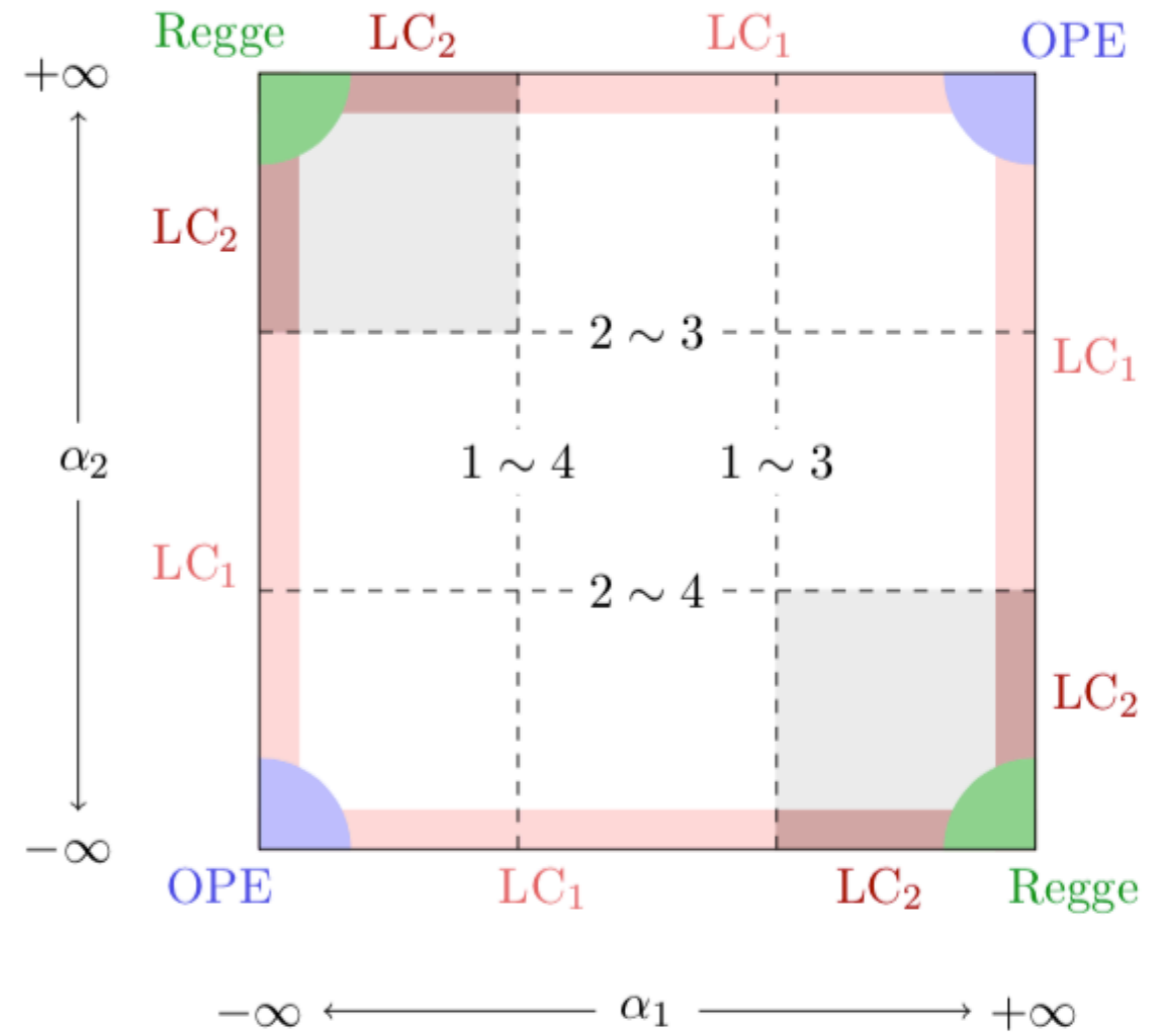
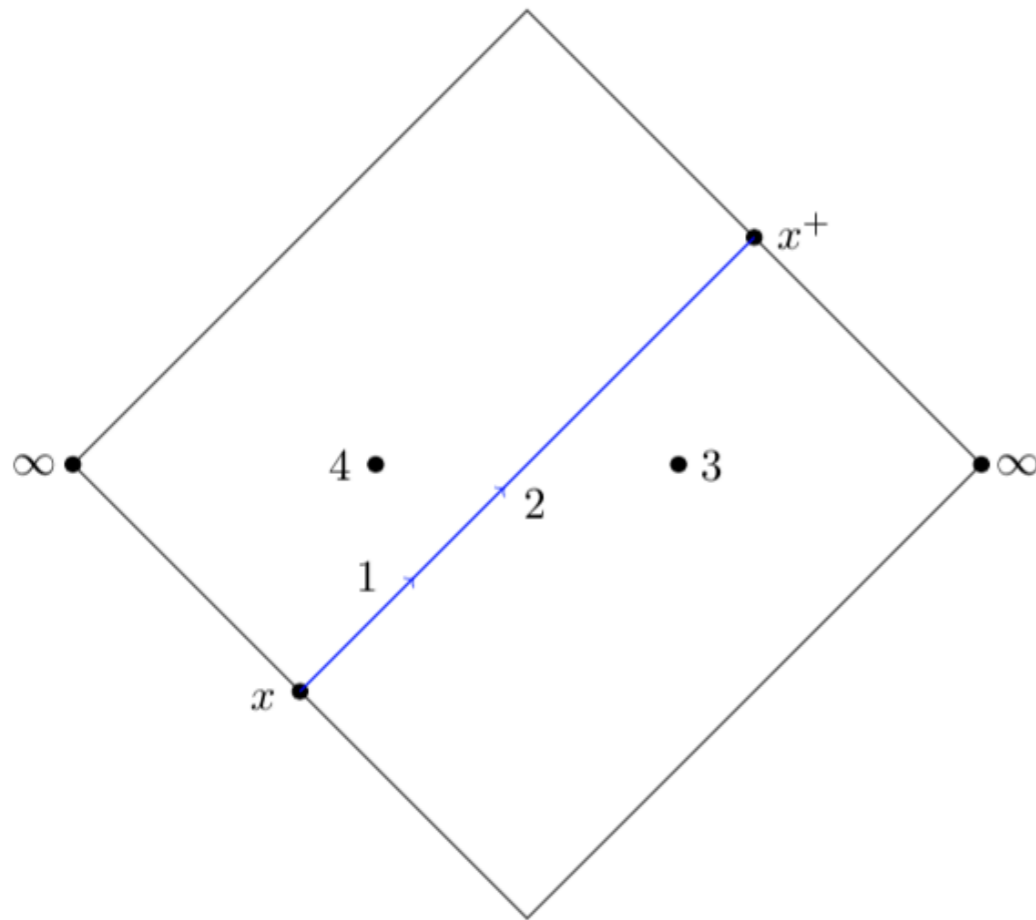
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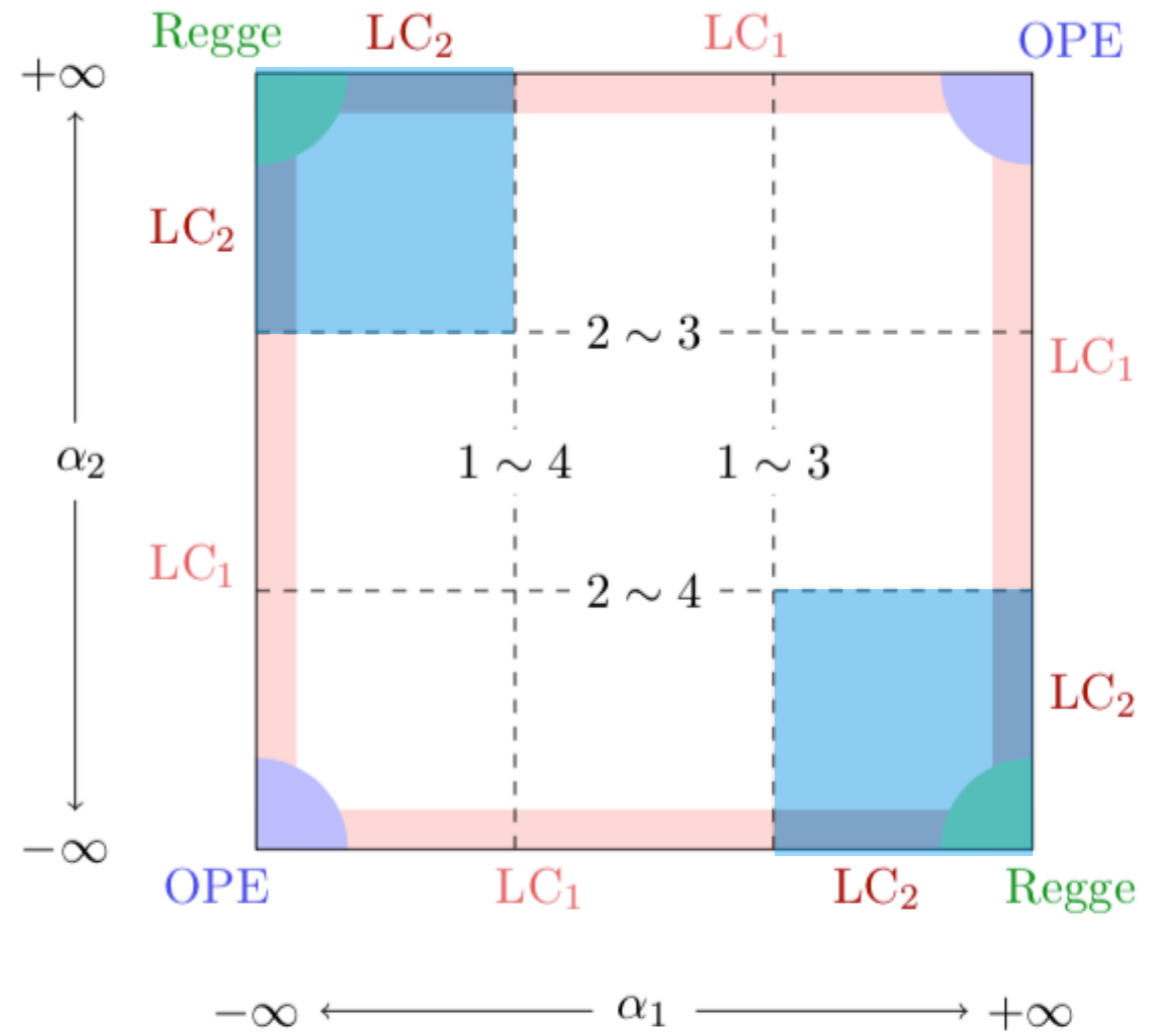
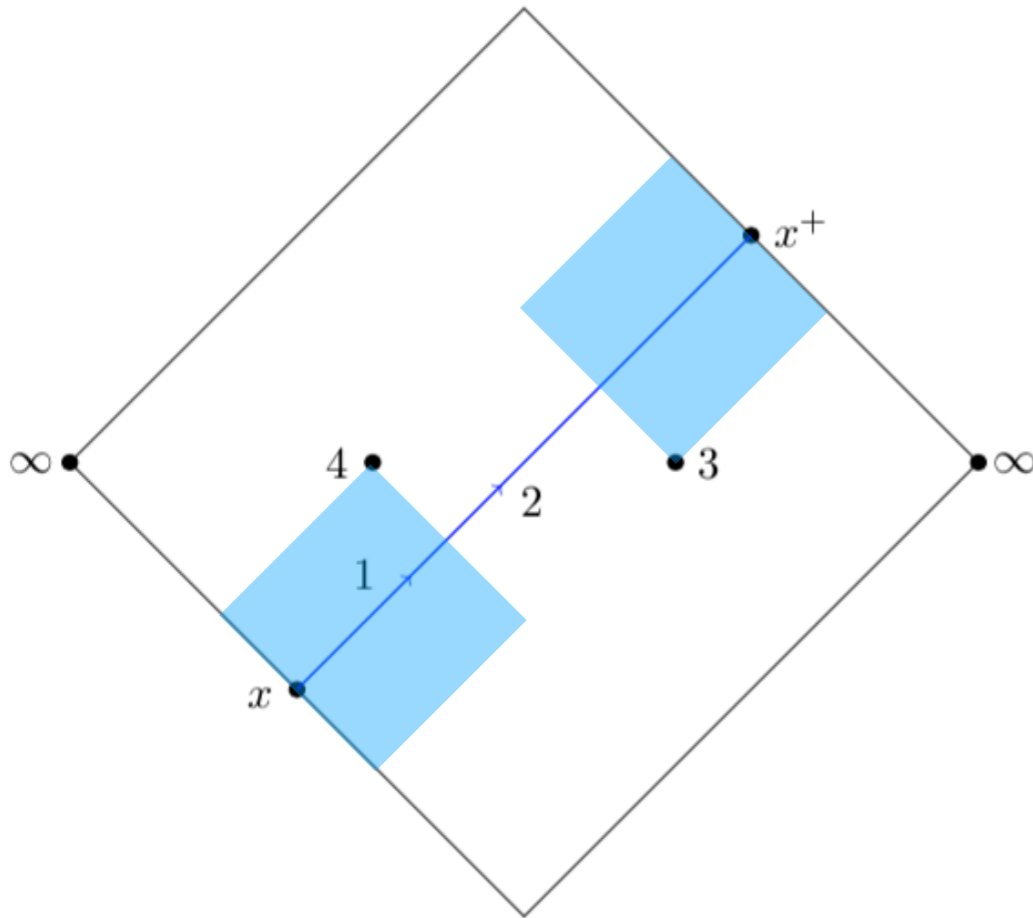


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**Rindler positivity  
+asymptotic light-cone expansion**

# Commutativity of light-ray operators

More generally, a necessary condition for a product to be well-defined and commutative

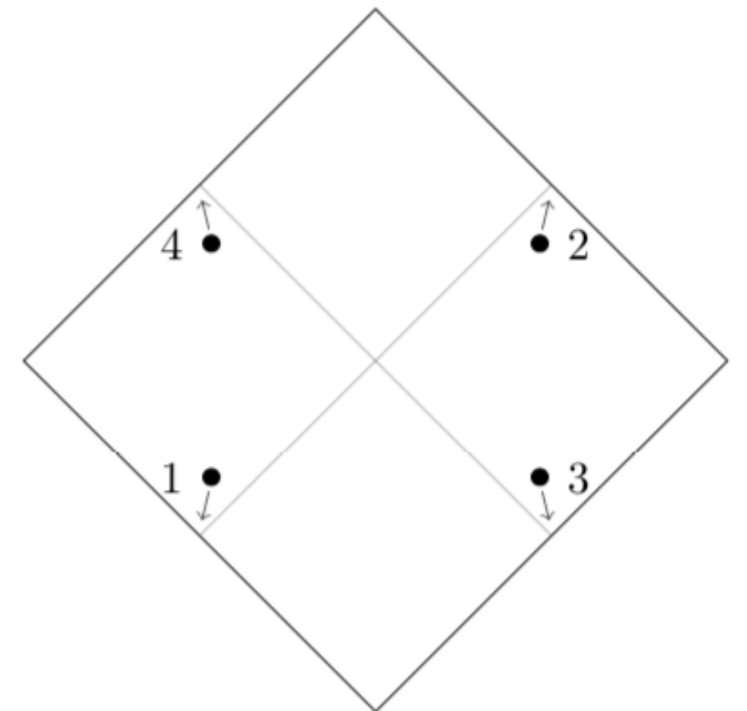
$$\langle \Omega | \mathcal{O}_4 \mathbf{L}[\mathcal{O}_{J_1}](x, z_1) \mathbf{L}[\mathcal{O}_{J_2}](x, z_2) \mathcal{O}_3 | \Omega \rangle$$

$$J_1 + J_2 > 1 + J_0$$

Here  $J_0$  is the Regge intercept

$$\frac{\langle ABAB \rangle}{\langle AA \rangle \langle BB \rangle} = 1 - f_{AA\mathcal{O}}(J_0) f_{BB\mathcal{O}}(J_0) e^{t(J_0-1)}$$

$$\mathcal{A}(s, t) \sim s^{J_0}$$



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**Reason:**

$$J_0 < 3$$

$$J_1 + J_2 > 1 + J_0$$

**Nonperturbatively:**

$$J_0 \leq 1$$

[Caron-Huot 17']

**Planar:**

$$J_0^{\text{planar}} \leq 2$$

[Maldacena, Shenker, Stanford 15']

Conversely, a non-vanishing commutator leads to a Regge pole at

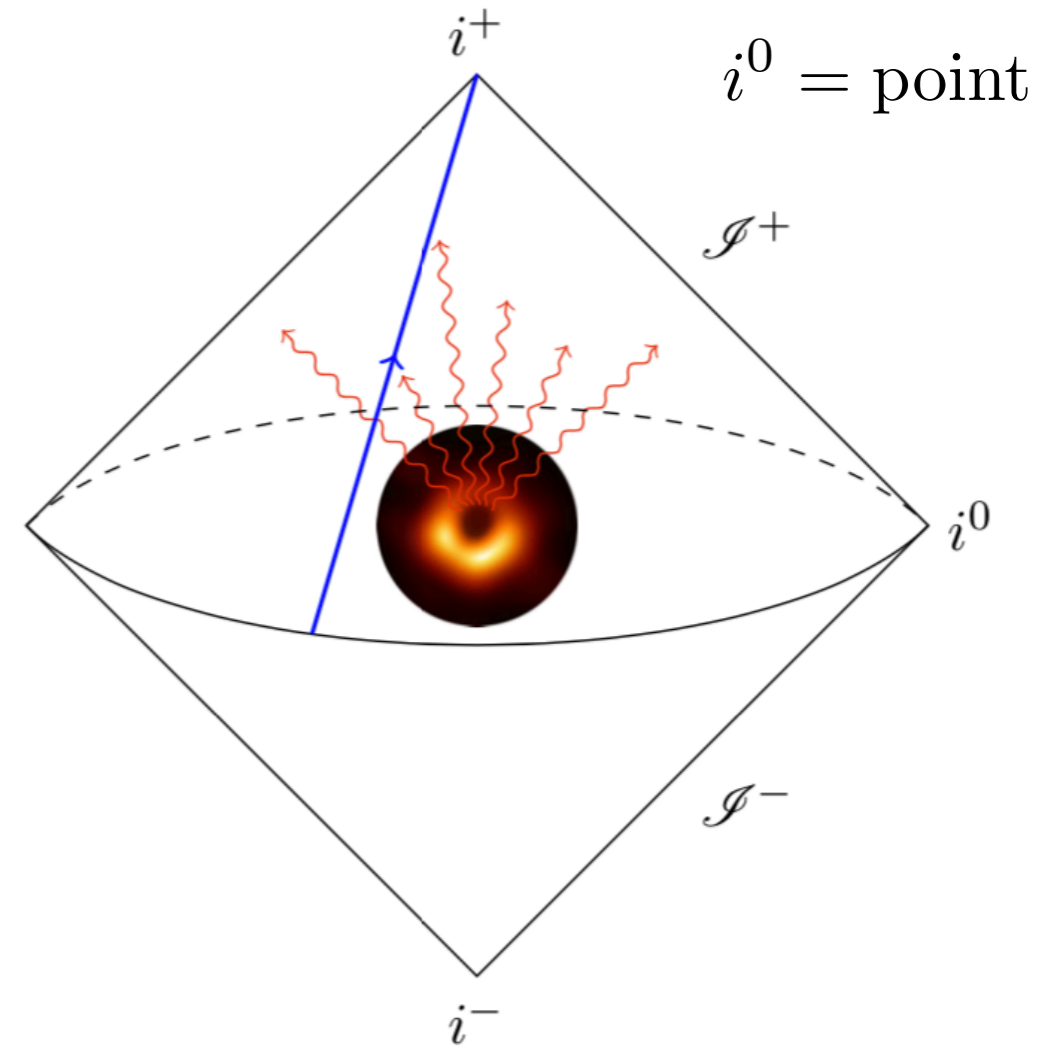
$$J_0 = 3$$

# Event Shapes

A convenient frame:

$$[P^\mu, \mathbf{L}[\mathcal{O}](\infty, z)] = 0$$

$$|\phi(p)\rangle = \int d^d x e^{ip \cdot x} \phi(x) |\Omega\rangle$$



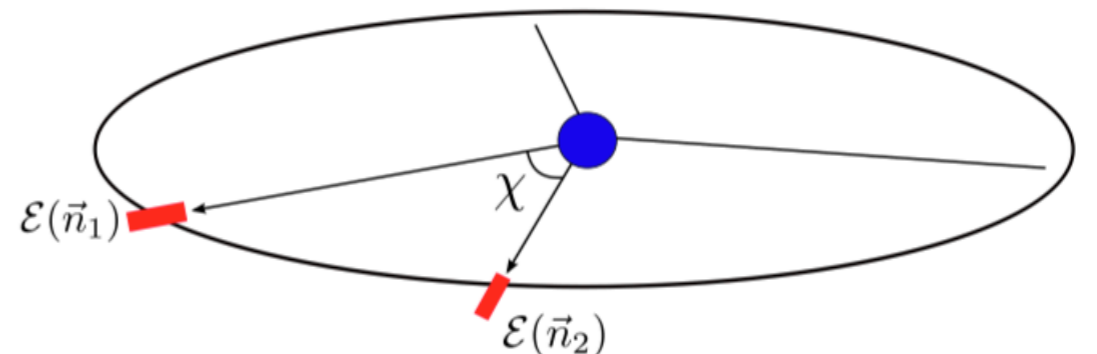
Event shapes:

$$\langle \phi_1(p) | \mathbf{L}[\mathcal{O}_1](\infty, z_1) \cdots \mathbf{L}[\mathcal{O}_n](\infty, z_n) | \phi_2(p) \rangle$$

(integrated Wightman functions)

$$z = (1, \vec{n})$$

$$z_1 \cdot z_2 = -1 + \cos \chi$$



lighttray = detector

## **Two-point event shapes**

Consider a commutative and convergent event shape.

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For the two-point event shape

$$\langle \mathcal{O}_4(p) | \mathbf{L}[\mathcal{O}_1](\infty, z_1) \mathbf{L}[\mathcal{O}_2](\infty, z_2) | \mathcal{O}_3(p) \rangle$$

we can consider two types of OPE:

**t-channel:**      lightray – local  $\rightarrow$  lightray – local

**s-channel:**      lightray – lightray  $\rightarrow$  local – local



# Local-Lightray OPE

[Belin, Hofman, Mathys '19]  
[Kologlu, Kravchuk, Simmons-Duffin, AZ '19]

$$\langle \mathcal{O}_4(p) | \mathbf{L}[\mathcal{O}_1](\infty, z_1) \mathbf{L}[\mathcal{O}_2](\infty, z_2) | \mathcal{O}_3(p) \rangle$$

$$= \sum_{\mathcal{O}} \sum_{\Psi_{\mathcal{O}}} \langle \mathcal{O}_4(p) | \mathbf{L}[\mathcal{O}_1](\infty, z_1) | \Psi_{\mathcal{O}} \rangle \langle \Psi_{\mathcal{O}} | \mathbf{L}[\mathcal{O}_2](\infty, z_2) | \mathcal{O}_3(p) \rangle$$

$$\sum_{\Psi_{\mathcal{O}}} |\Psi_{\mathcal{O}}\rangle \langle \Psi_{\mathcal{O}}| = \mathcal{A}(\Delta)^{-1} \int_{p>0} \frac{d^d p}{(2\pi)^d} (-p^2)^{\frac{d}{2}-\Delta} |\mathcal{O}(p)\rangle \langle \mathcal{O}(p)|$$

$$= \sum_{\mathcal{O}, a, b} \lambda_{14\mathcal{O}, a} \lambda_{23\mathcal{O}, b} G_{\Delta_{\mathcal{O}}, \rho_{\mathcal{O}}}^{t, ab}(p, z_1, z_2)$$

These are the t-channel blocks

**Example:** For four scalars

$$G_{\Delta_{\mathcal{O}}, J_{\mathcal{O}}}^t(z_1, z_2, p) = \sum_{s=0}^J G_{\Delta_{\mathcal{O}}, J_{\mathcal{O}}}^t(s) C_s^{\left(\frac{d-3}{2}\right)}(\cos \chi)$$

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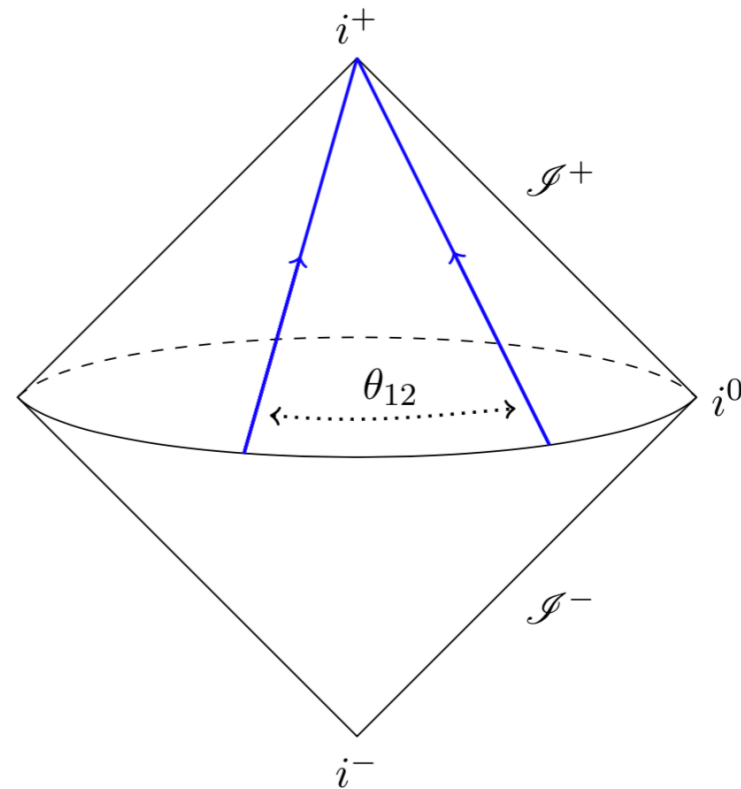
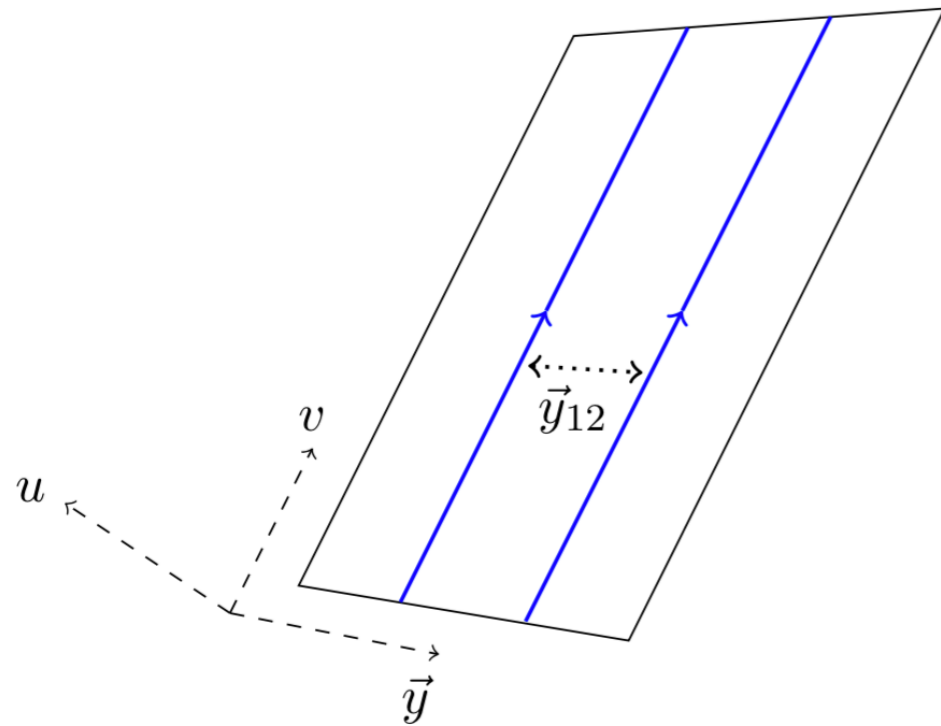
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involve  ${}_4F_3(\dots; 1)$

# Lightray-Lightray OPE

A light-ray operator is point-like in the transverse plane. It is natural to expand in small transverse separations.



$$\int_{-\infty}^{\infty} dv_1 \mathcal{O}_{1;v\dots v}(u=0, v_1, \vec{y}_1) \times \int_{-\infty}^{\infty} dv_2 \mathcal{O}_{2;v\dots v}(u=0, v_2, \vec{y}_2)$$

$$\stackrel{?}{=} \sum_i |\vec{y}_{12}|^{\delta_i - (\Delta_1 - 1) - (\Delta_2 - 1)} \mathbb{O}_i$$

# Lightray-Lightray OPE

Small angle:

- QCD [\[Konishi, Ukawa, Veneziano '79\]](#)
- planar  $\mathcal{N} = 4$  [\[Hofman, Maldacena, '08\]](#)

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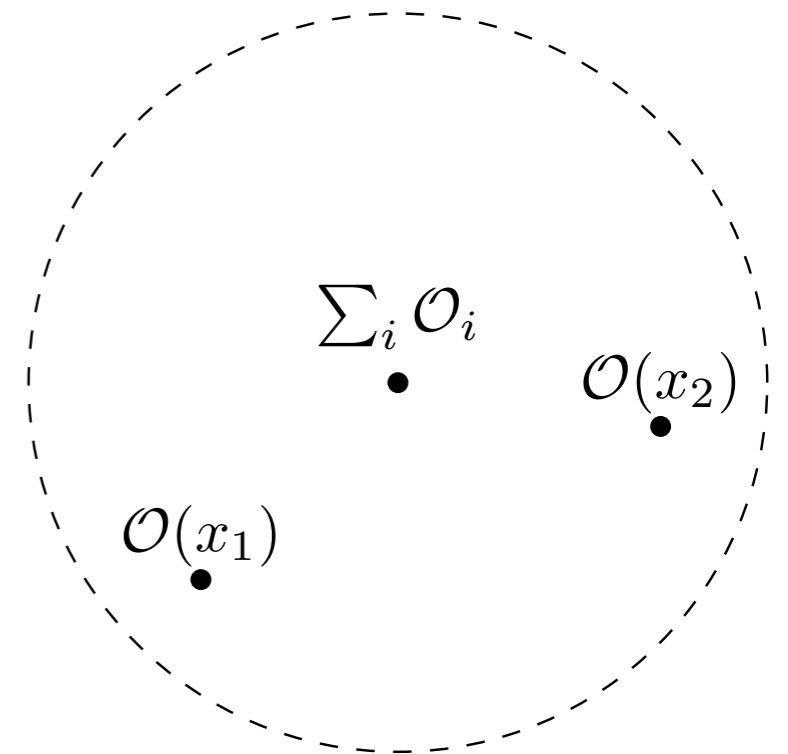
Can we develop a systematic expansion in a general CFT?

The usual argument does not apply

$$\mathcal{O}_1 \mathcal{O}_2 |\Omega\rangle = |\Psi\rangle = \sum_i |\mathcal{O}_i\rangle$$

$$|\mathcal{O}_i\rangle = \mathcal{O}_i |\Omega\rangle$$

No such argument for light-ray operators.

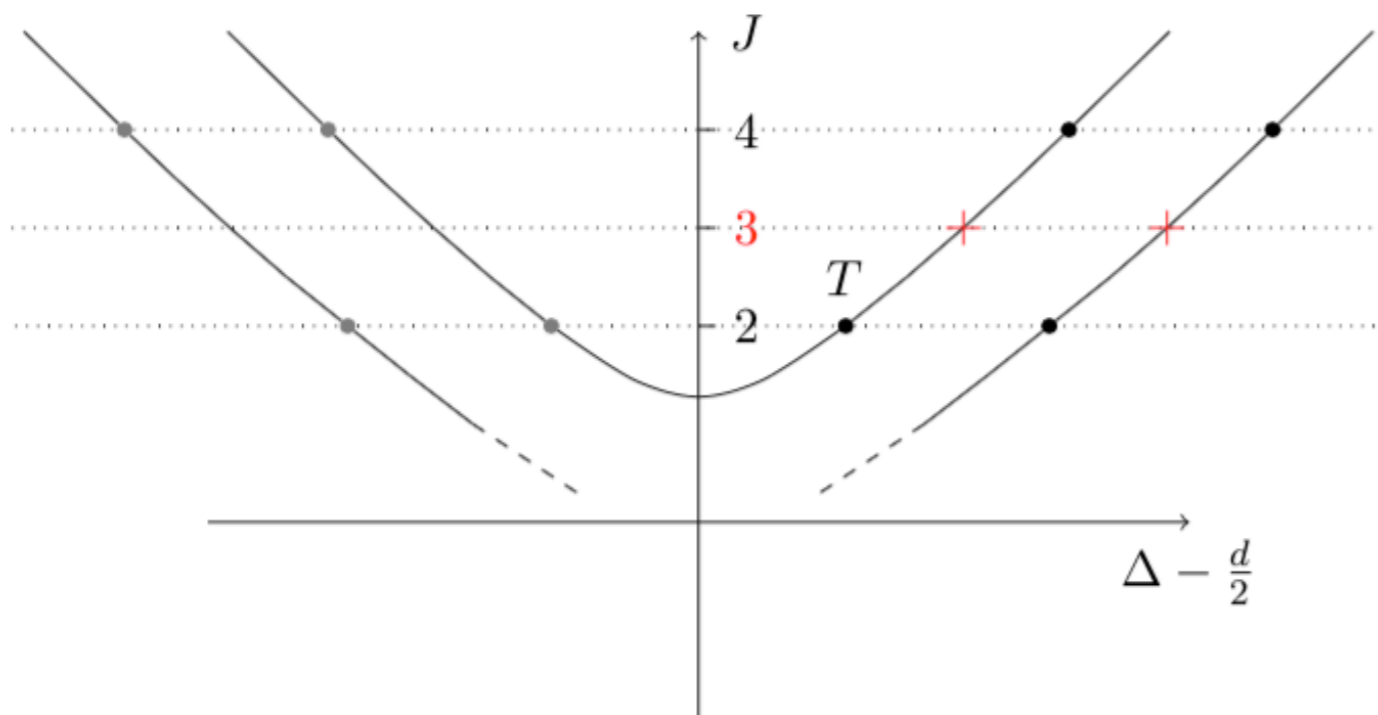


# ANEC OPE

**Claim:** The ANEC  $\times$  ANEC OPE in a unitary CFT is given by

$$\int dv_1 T_{vv}(0, v_1, \vec{y}_1) \times \int dv_2 T_{vv}(0, v_2, \vec{y}_2)$$

$$= \pi i \sum_{\lambda, a} \sum_i \mathcal{D}_{\Delta_i - 1, \lambda}^{(a), +}(\vec{y}_{12}, \partial_{\vec{y}_2}) \mathbb{O}_{i, J=3, \lambda, (a)}^+(\vec{y}_2)$$



$\lambda$  is the transverse spin  
SO(d-2) representation:

$$\bullet, \square, \square\square, \square\square\square, \square\square\square\square, \begin{array}{|c|c|} \hline \square & \square \\ \hline \square & \square \\ \hline \end{array}, \begin{array}{|c|c|} \hline \square & \square \\ \hline \square & \square \\ \hline \end{array}$$

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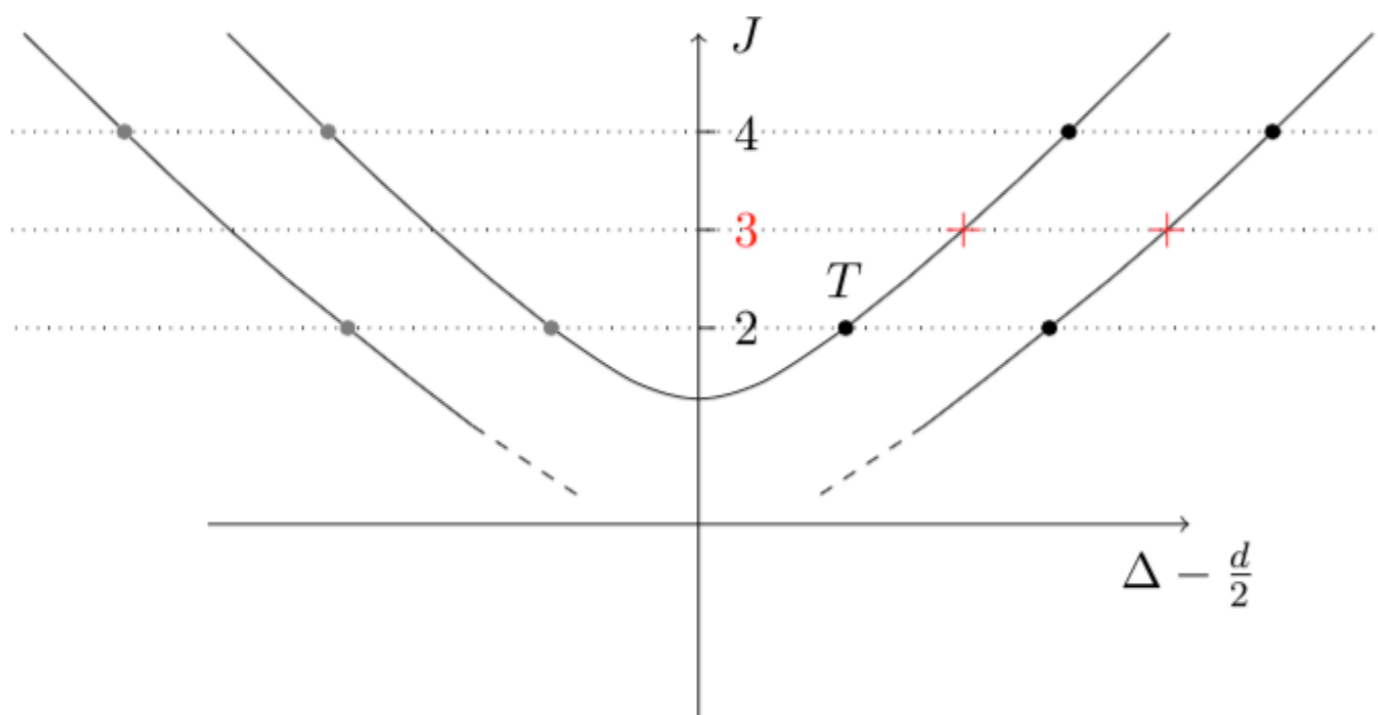
$$\int dv_1 T_{vv}(0, v_1, \vec{y}_1) \times \int dv_2 T_{vv}(0, v_2, \vec{y}_2)$$

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spin selection rule:

$$J = J_1 + J_2 - 1$$

[Hofman, Maldacena 08']



$\lambda$  is the transverse spin  $SO(d-2)$  representation:

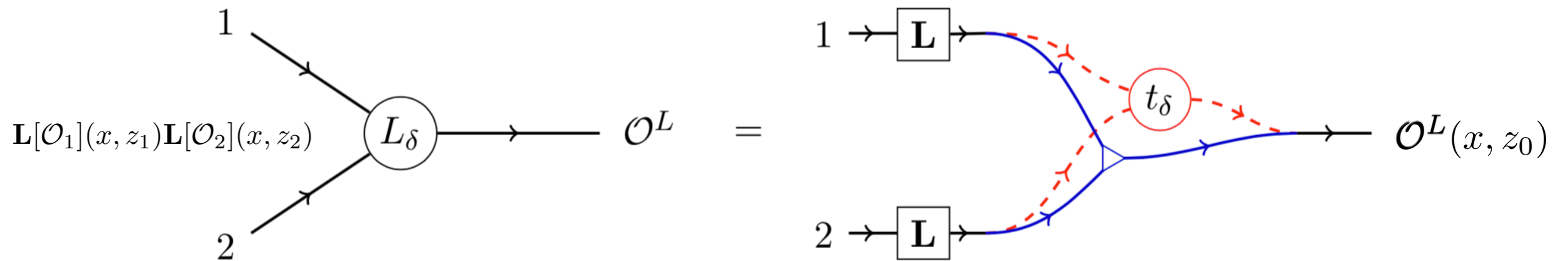
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# Lightray-Lightray OPE

Different strategy:

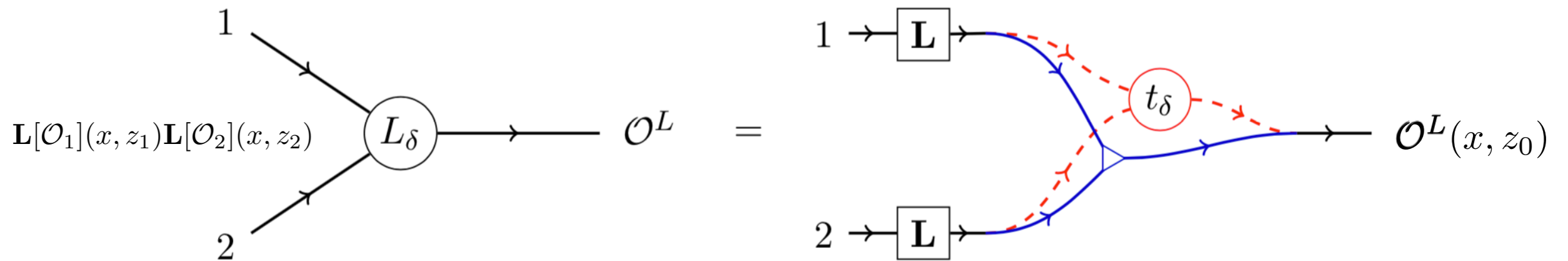
1. Decompose the product of light-ray operators into conformal irreps (harmonic analysis for the transverse conformal group  $SO(d-1, 1)$  )



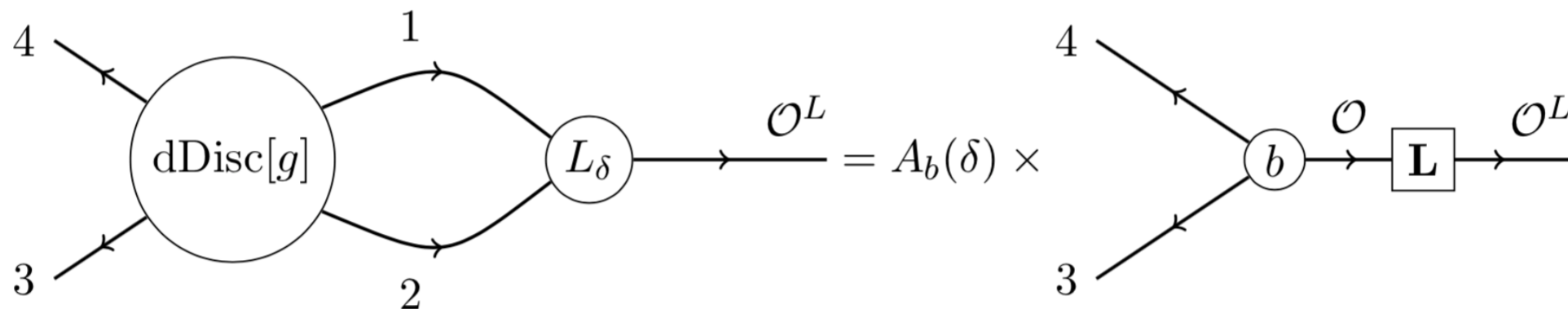
# Lightray-Lightray OPE

Different strategy:

1. Decompose the product of light-ray operators into conformal irreps (harmonic analysis for the transverse conformal group  $SO(d-1, 1)$ )



2. Compute a matrix element of a single irrep (in terms of an integral of a double commutator)



$$\mathbf{L}[\mathcal{O}]|\Omega\rangle = 0$$

$$\langle \mathcal{O}_1 \mathbf{L}[\mathcal{O}_2] \mathbf{L}[\mathcal{O}_3] \mathcal{O}_4 \rangle = \langle [\mathcal{O}_1, \mathbf{L}[\mathcal{O}_2]] [\mathbf{L}[\mathcal{O}_3], \mathcal{O}_4] \rangle$$

# Lightray-Lightray OPE

3. Relate to the Lorentzian inversion formula

$$A_b(\delta) = \left( \begin{array}{c} \text{dDisc}[g] \\ \text{L}_\delta \rightarrow \mathcal{O}^L \rightarrow \text{L} \leftarrow b \end{array} \right)$$

$$C_{ab}^+(\Delta, J) + C_{ab}^-(\Delta, J) = \left( \begin{array}{c} \text{dDisc}[g] \\ a \rightarrow \text{L} \rightarrow \mathcal{O}^L \rightarrow \text{L} \leftarrow b \end{array} \right)$$

$$A_b(\delta) \equiv \gamma^a (C_{ab}^+ + C_{ab}^-)$$

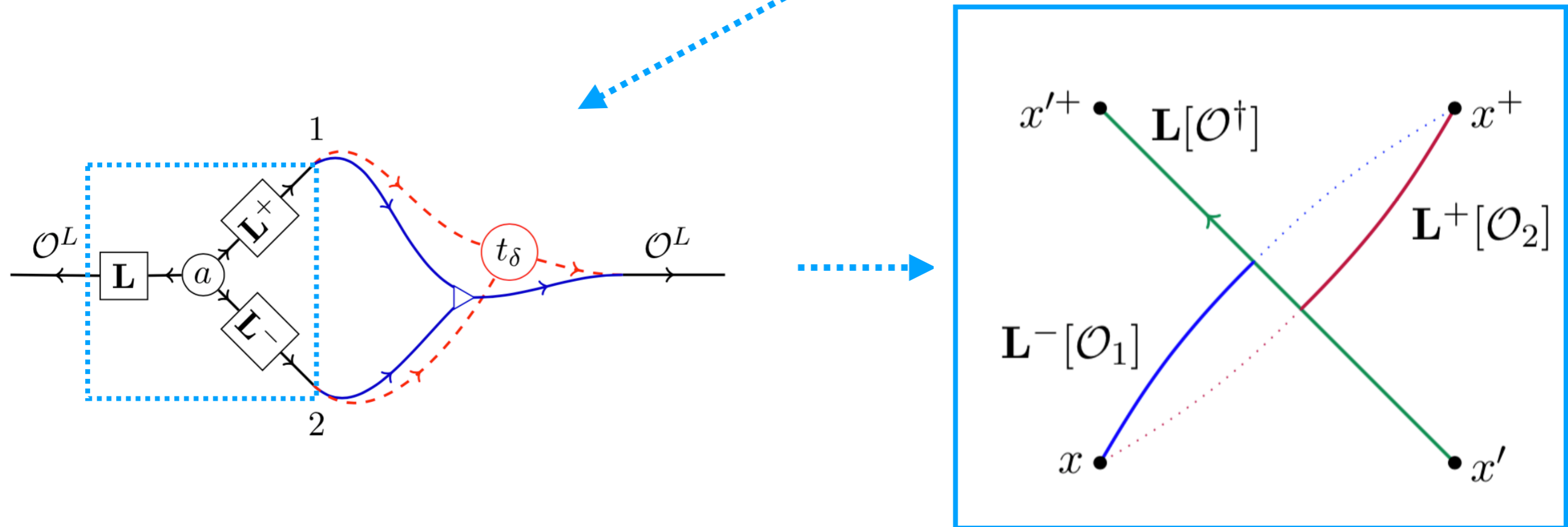
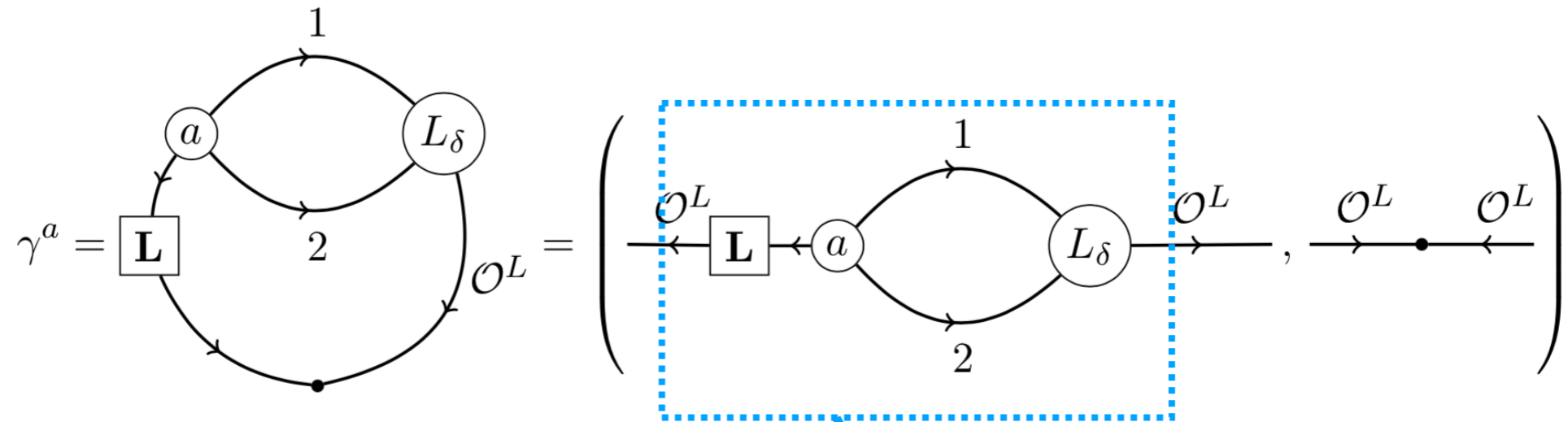
[Caron-Huot 17']

[Simmons-Duffin, Stanford, Witten 17']

[Kravchuk, Simmons-Duffin 18']

# Lightray-Lightray OPE

The relation is given by a bubble integral



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## **Part II:           applications**

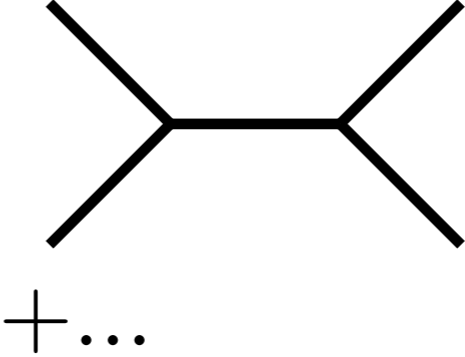
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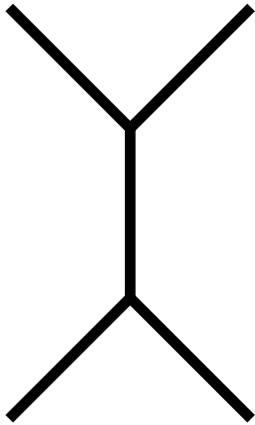
# Holographic CFTs

$$\frac{1}{l_{Pl}^{D-2}} \int d^D x \sqrt{-g} (R - 2\Lambda + \dots)$$

**AdS/CFT**



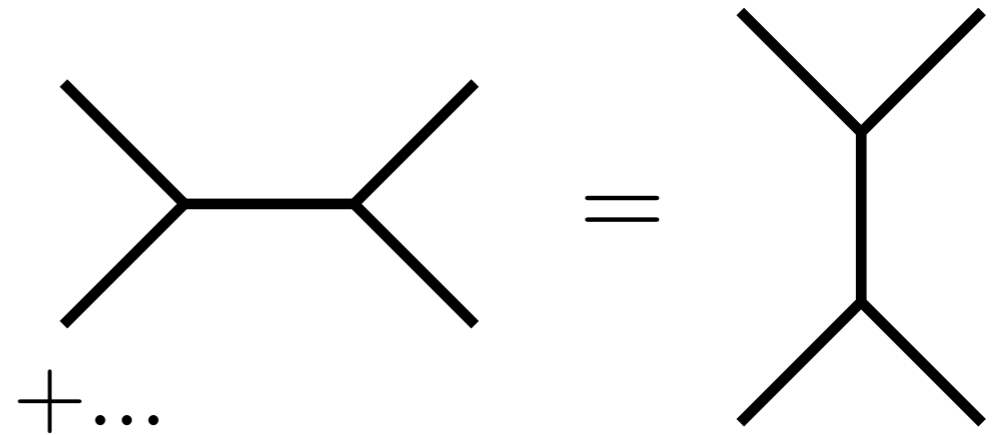
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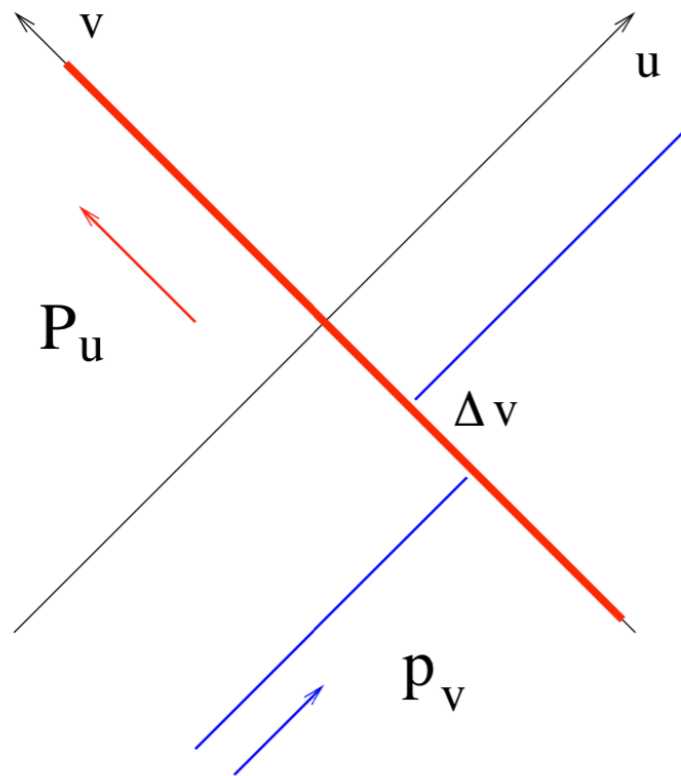
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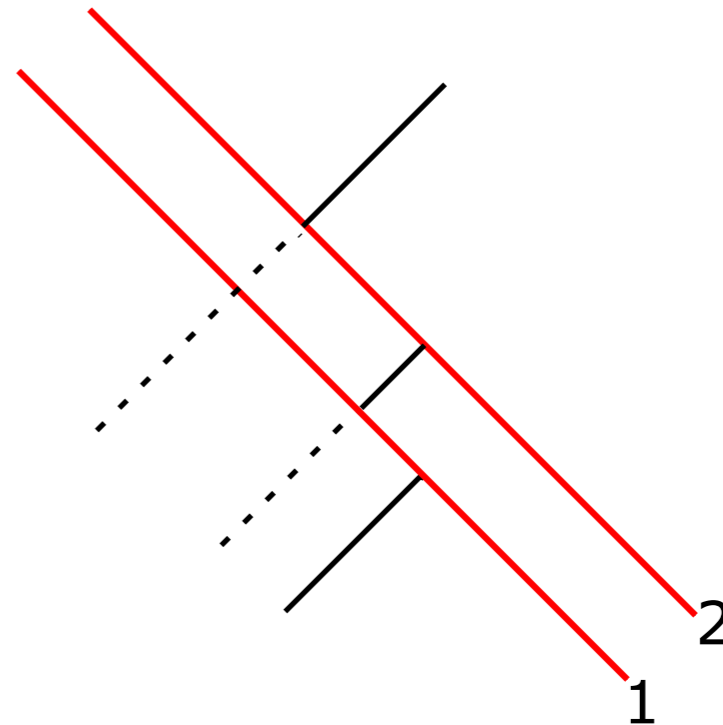
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**ANEC:**



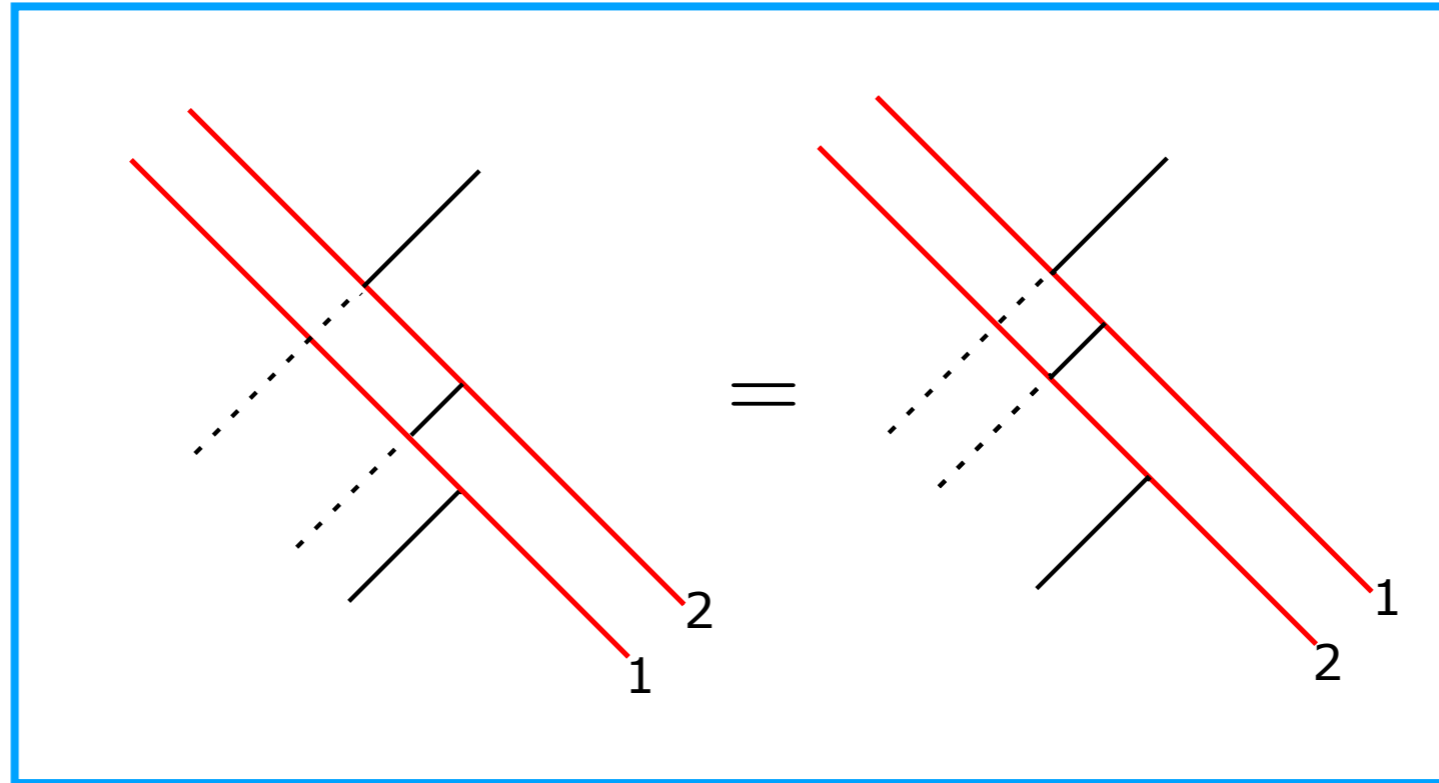
**two-point event shape:**



[Hofman, Maldacena, '08]

# AdS EFT: ANEC commutativity

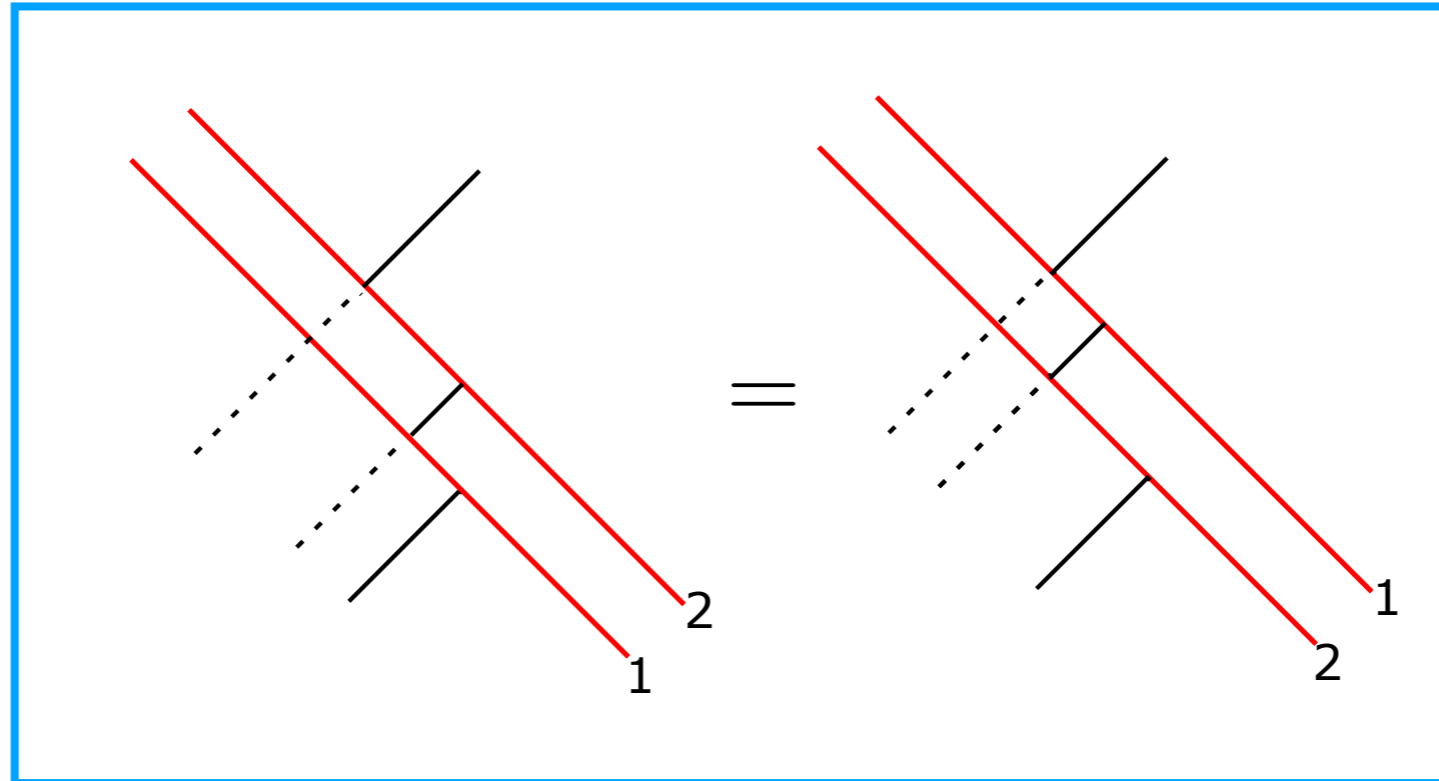
## ANEC commutativity





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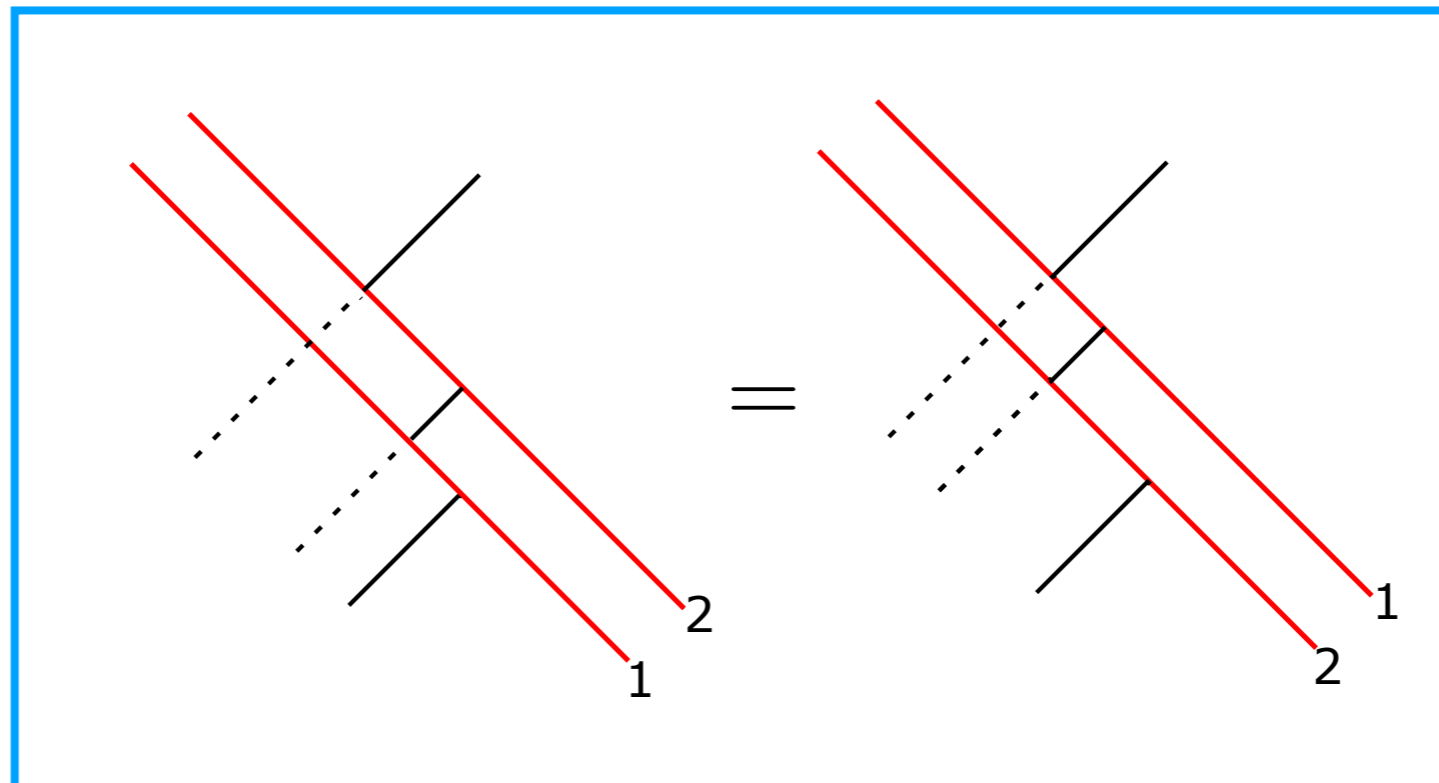
**Claim:** Any non-minimal graviton 3pt coupling violates ANEC commutativity

[Belin, Hofman, Mathys '19]

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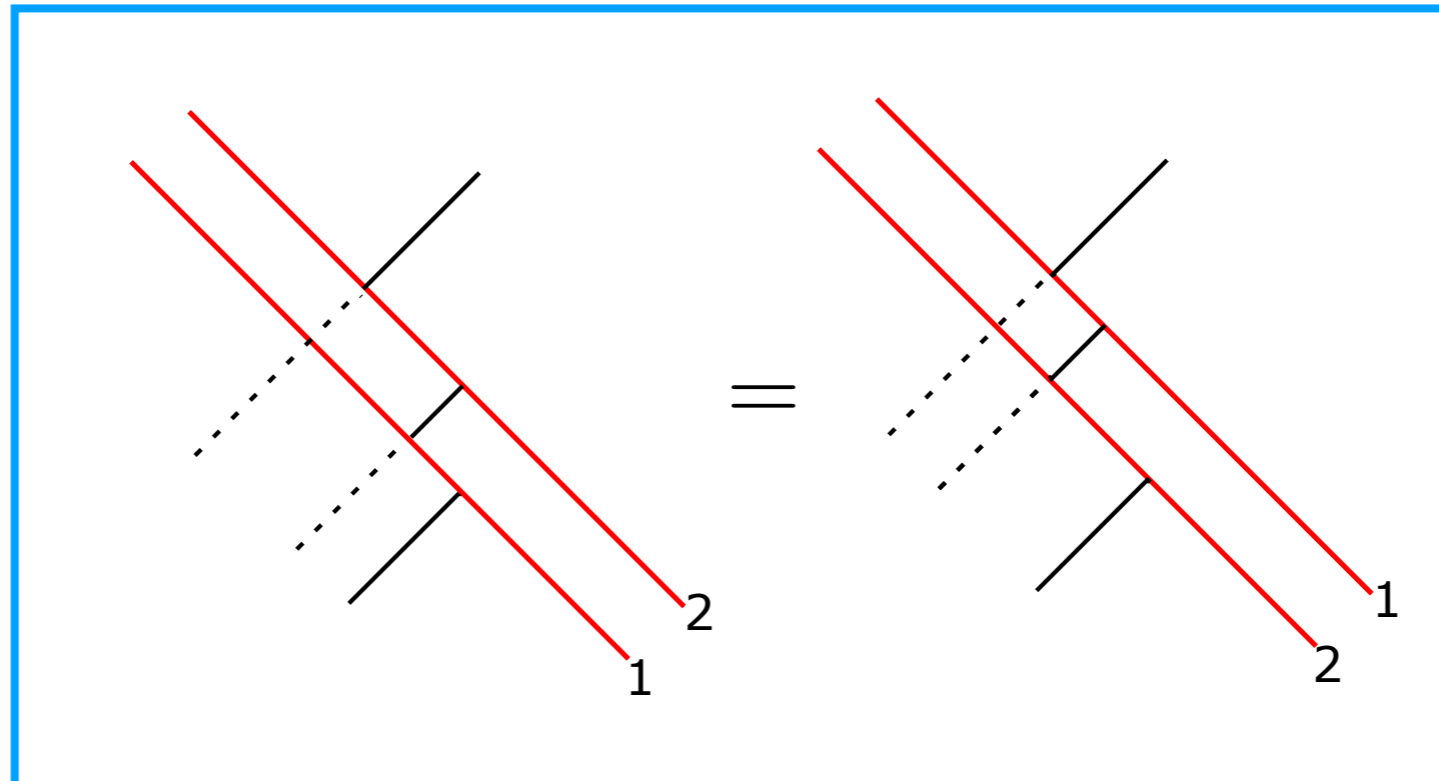
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**Stringy Equivalence Principle:** In every UV complete theory of quantum gravity AdS/flat/dS gravitational (and higher spin) shocks commute.  
(should be applicable to our Universe as well)

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$$\int dt \text{Disc}_t A(s, t) = 0$$

**superconvergence**

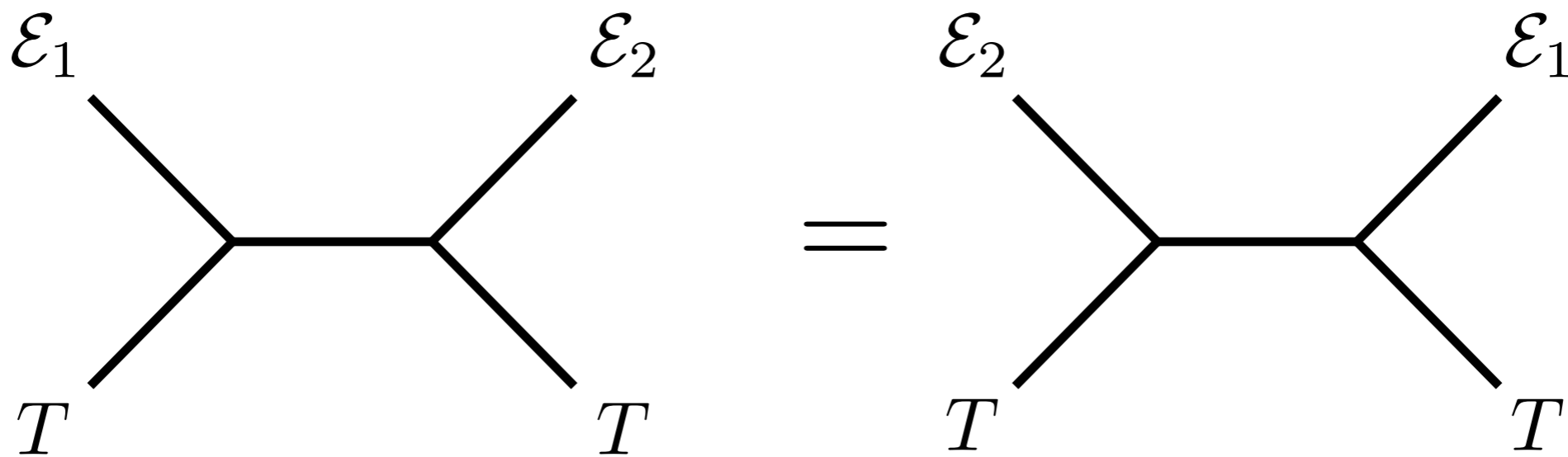
[Alfaro, Fubini, Rossetti, Furlan 66']

# AdS EFT: ANEC commutativity

$$[\mathbf{L}[T](x, z_1), \mathbf{L}[T](x, z_2)] = 0$$

Using the **t-channel OPE**:

$$\langle TTT \rangle = \langle TTT \rangle_R + t_2 \langle TTT \rangle_{R^2} + t_4 \langle TTT \rangle_{R^3}$$



$$(t_4 + 2t_2)^2 = \sum_{\phi} |\lambda_{TT\phi}|^2 \frac{15 \cdot 2^4 \pi^4 \Gamma(\Delta_{\phi} - 1) \Gamma(\Delta_{\phi})}{C_T \Gamma(4 - \frac{\Delta_{\phi}}{2})^2 \Gamma(2 + \frac{\Delta_{\phi}}{2})^6} + \text{non-scalar},$$

$$(t_4 + 2t_2)^2 = - \sum_{\phi} |\lambda_{TT\phi}|^2 \frac{360^2 \pi^4 \Gamma(\Delta_{\phi} - 1) \Gamma(\Delta_{\phi})}{7 C_T \Gamma(4 - \frac{\Delta_{\phi}}{2})^2 \Gamma(2 + \frac{\Delta_{\phi}}{2})^6} + \text{non-scalar}$$

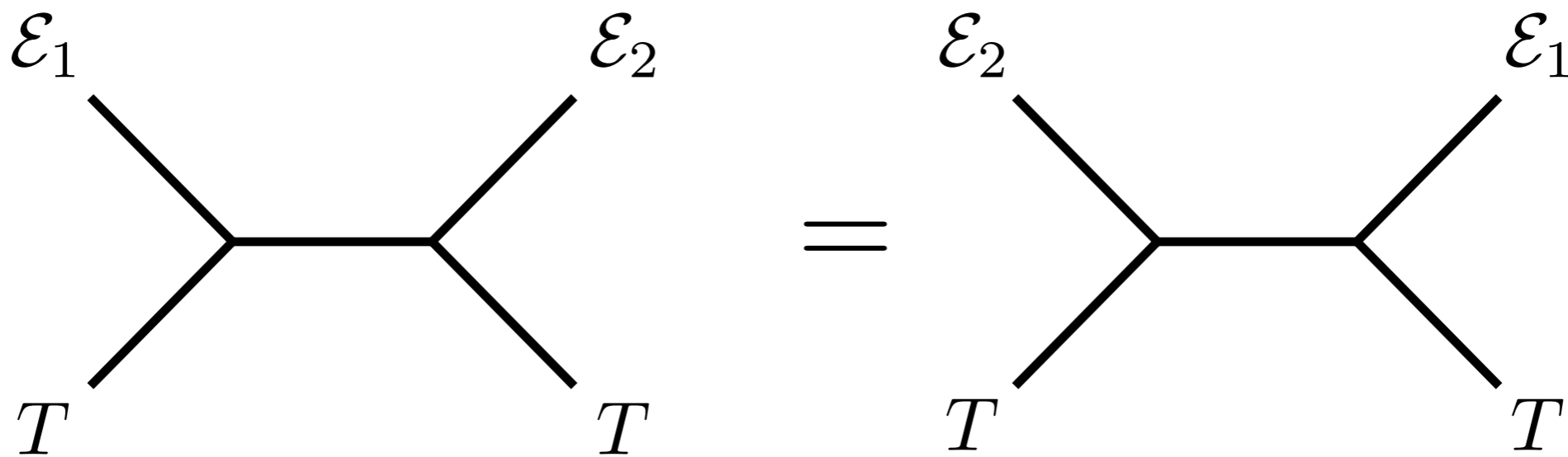
**Sum over single trace operators only! (at large N)**

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**Sum over single trace operators only! (at large N)**

**How do we bound these infinite sums?**

# AdS EFT: ANEC commutativity

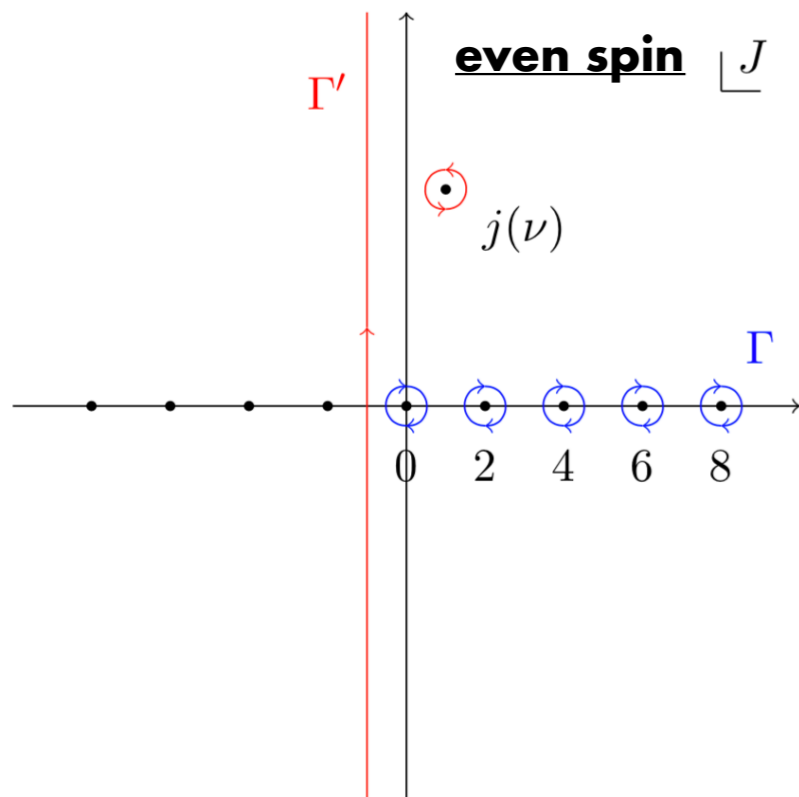
[Kologlu, Kravchuk, Simmons-Duffin, AZ, work in progress]

Using the **s-channel OPE** and conformal Regge theory:  
**(lightray-lightray)**

**ANEC commutativity**

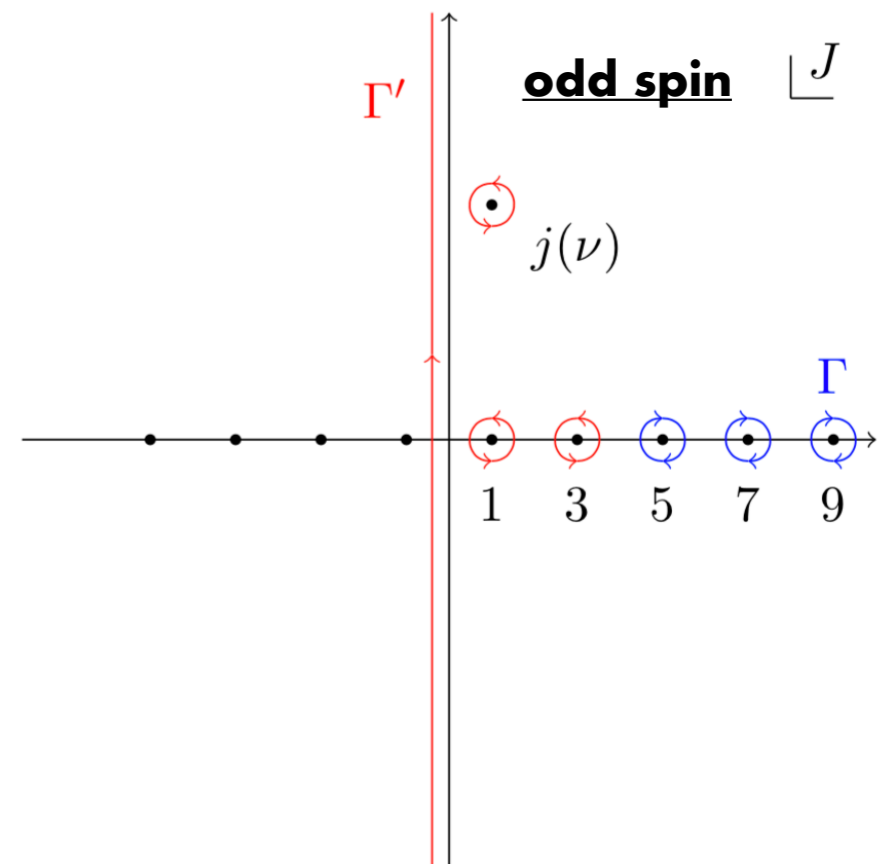
=

**absence of the J=3 Regge pole**



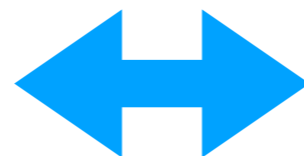
**Euclidean OPE**

vs



**analyticity in spin**

$$[\mathbf{L}[T](x, z_1), \mathbf{L}[T](x, z_2)] = 0$$



$$C_{ab}^-(\Delta, J = 3) = 0$$

# Toy Model

[Caron-Huot '17]

We next use the Froissart-Gribov formula:

**correlator**  $\mathcal{A}(s, t) = \sum_J a_J(s) \nu^J, \quad \nu = \frac{t-u}{2}$  **unitarity:**  $\text{Disc} \mathcal{A} \geq 0$

**CPW**  $a_J^\pm(s) = \int_0^\infty \frac{d\nu}{\nu} \nu^{-J} \text{Disc}_t \mathcal{A}(s, \nu) \pm \int_{-\infty}^0 \frac{d\nu}{-\nu} (-\nu)^{-J} \text{Disc}_u \mathcal{A}(s, \nu)$

$$a_{J=3}^-(s) = \alpha_{\text{GB}}^2(s) + \int_{\Delta_{\text{gap}}^2}^\infty \frac{d\nu}{\nu} \nu^{-3} \text{Disc}_t \mathcal{A}(s, \nu) - \int_{-\infty}^{-\Delta_{\text{gap}}^2} \frac{d\nu}{-\nu} (-\nu)^{-3} \text{Disc}_u \mathcal{A}(s, \nu) = 0$$

$$|\alpha_{\text{GB}}^2(s)| = \left| \int_{\Delta_{\text{gap}}^2}^\infty \frac{d\nu}{\nu} \nu^{-3} \text{Disc}_t \mathcal{A}(s, \nu) - \int_{-\infty}^{-\Delta_{\text{gap}}^2} \frac{d\nu}{-\nu} (-\nu)^{-3} \text{Disc}_u \mathcal{A}(s, \nu) \right| \leq a_{J=3}^+(s)$$

$$|\alpha_{GB}(s)|^2 \leq a_{J=3}^+(s)$$

# Toy Model

[Caron-Huot '17]

Reproducing the graviton pole requires:

$$a_{J=2}^+(s) : \lim_{s \rightarrow 0} \frac{C_{\phi\phi P}^2(s)}{2 - J(s)} = -\frac{1}{c_T} \frac{1}{s}$$



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**Pomeron pole:**

$$a_J^+(s) \sim \frac{C_{\phi\phi P}^2(s)}{J - J(s)} \quad \text{Disc}_t \mathcal{A}(s, \nu) \sim C_{\phi\phi P}^2(s) \nu^{J(s)}$$

**"No outliers":**

$$\text{Disc}_t \mathcal{A}(s, \nu) < c_0 C_{\phi\phi P}^2(s) \nu^{J(s)}$$

$$\nu > m_{gap}^2$$

$$c_0 = O(1)$$

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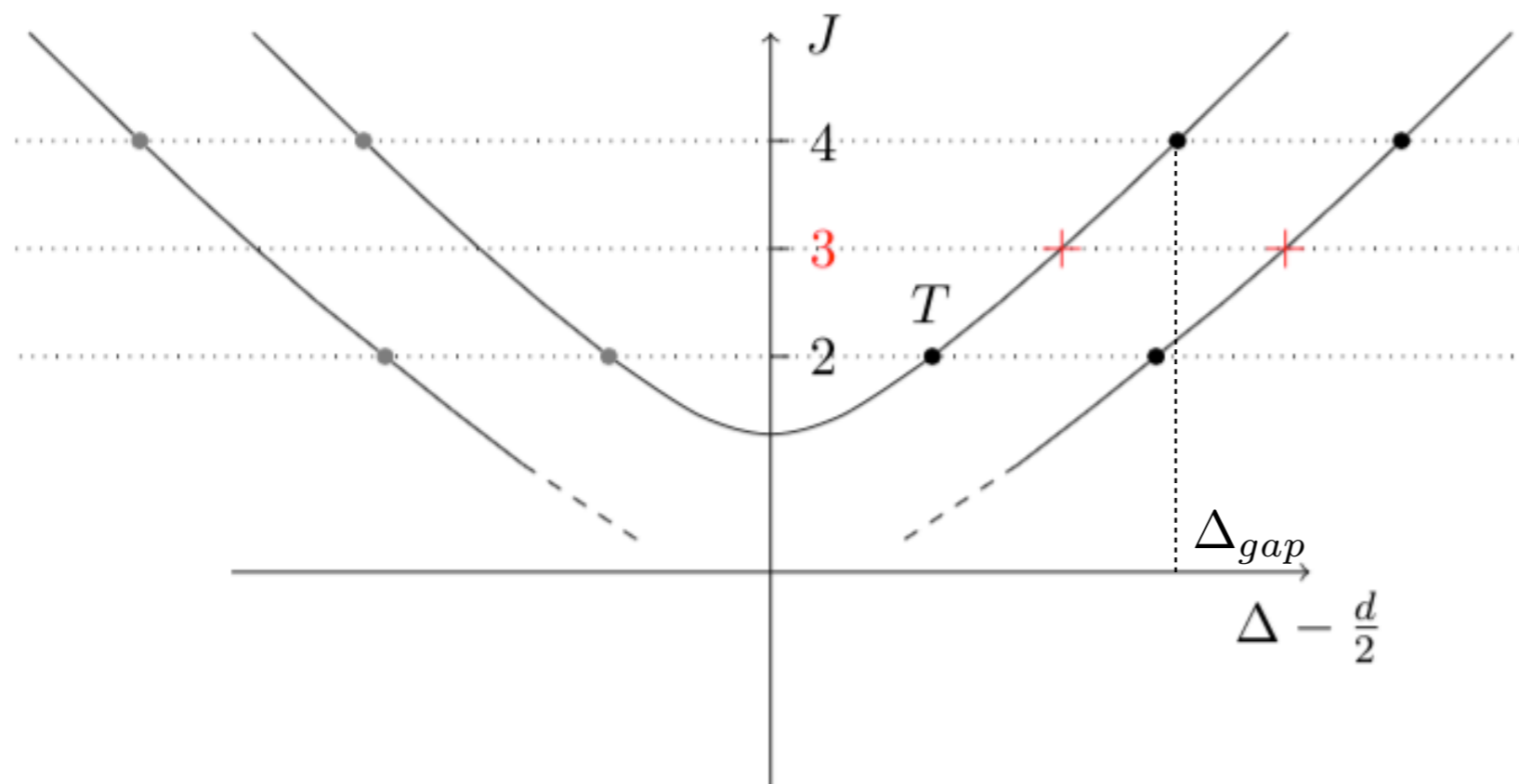
Assuming **no outliers** we get:

$$|\alpha_{GB}(s)|^2 \leq \frac{2c_0}{3 - J(s)} \frac{C_{\phi\phi P}^2(s)}{(\Delta_{gap}^2)^{3-J(s)}}$$

# Toy Model

[Hartman, Keller, Stoica '14]  
[Caron-Huot '17]

$$|\alpha_{GB}(0)|^2 \leq \frac{2c_0}{\Delta_{gap}^2 J'(0)}$$

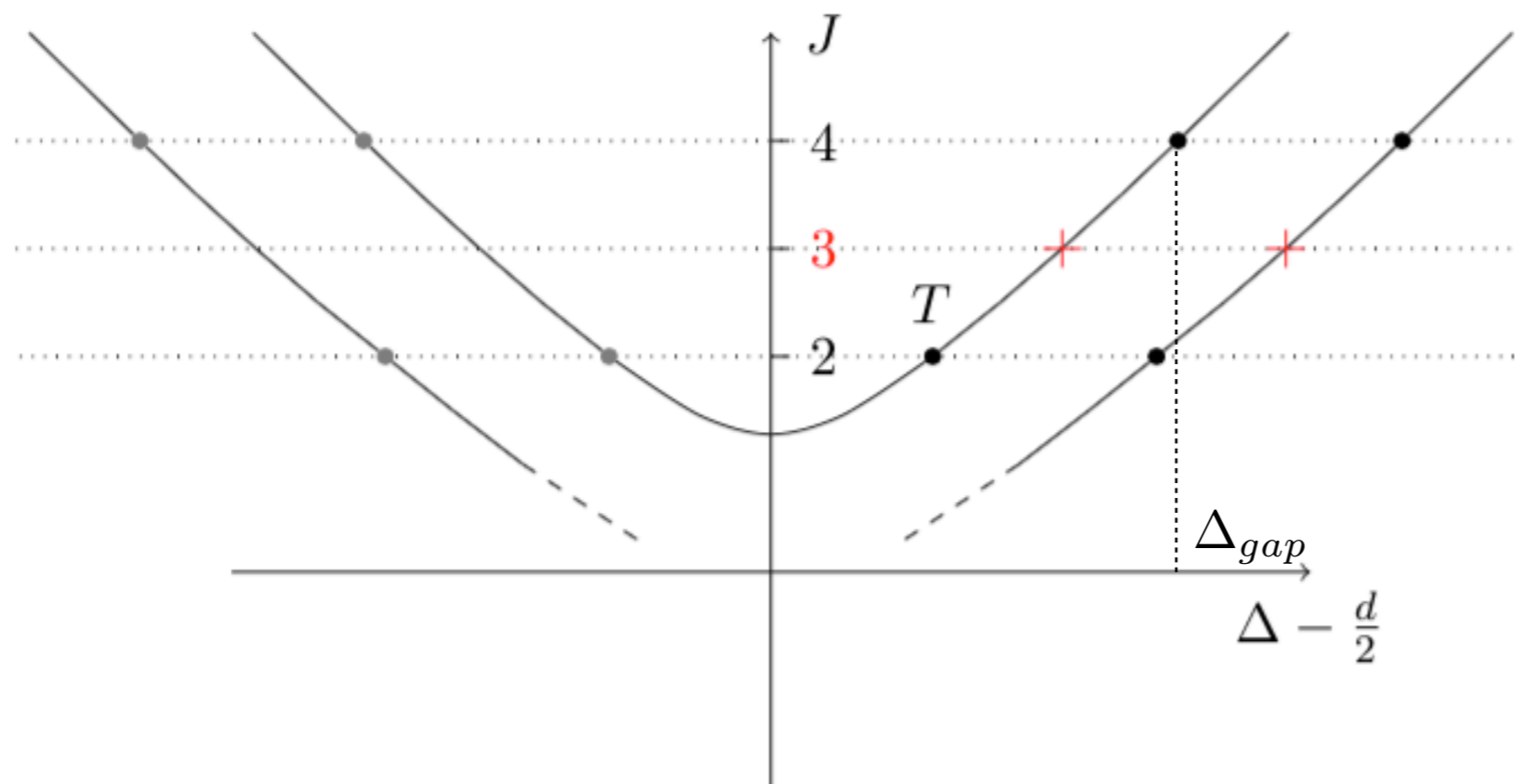


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[Hartman, Keller, Stoica '14]  
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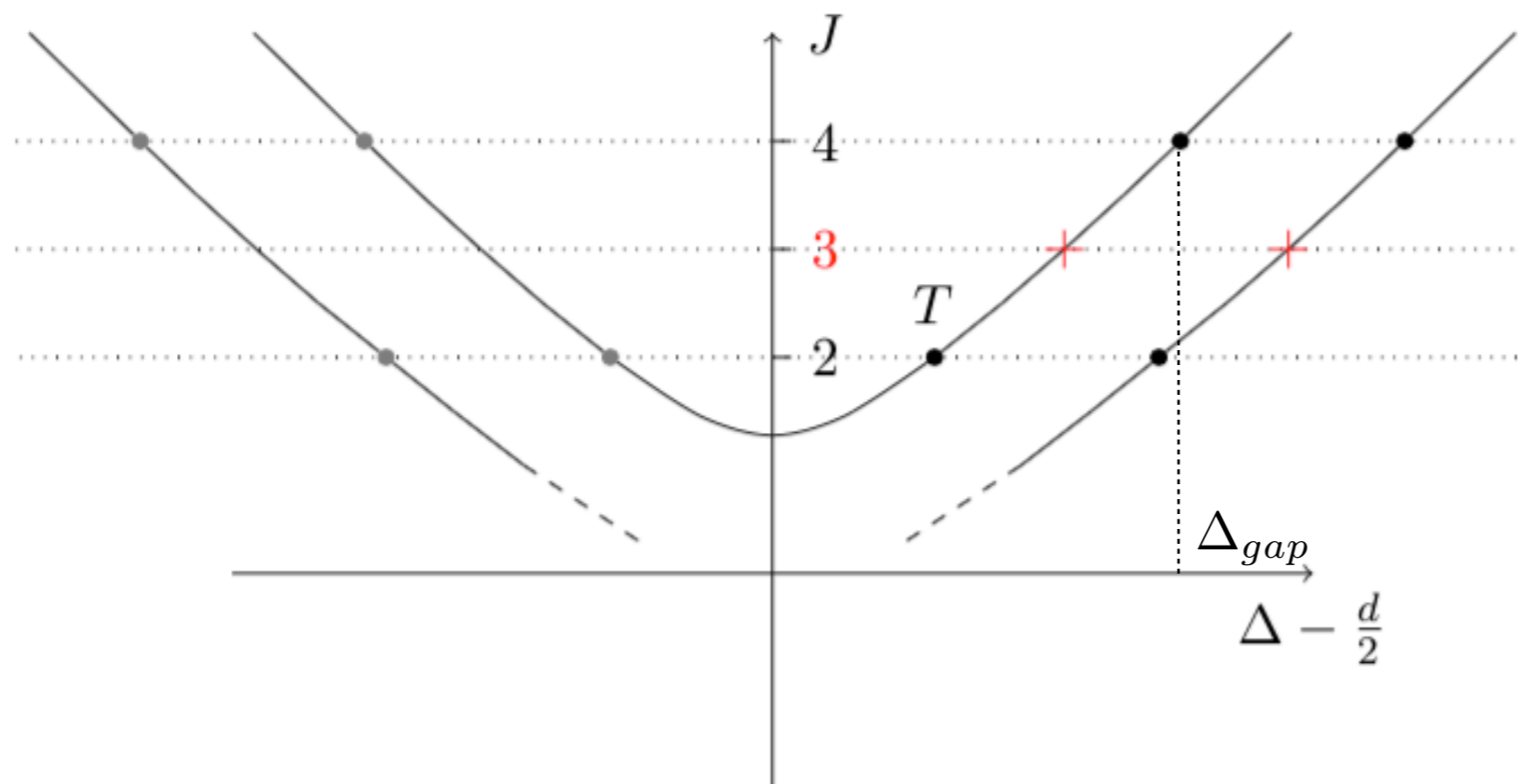
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**spectral gap**



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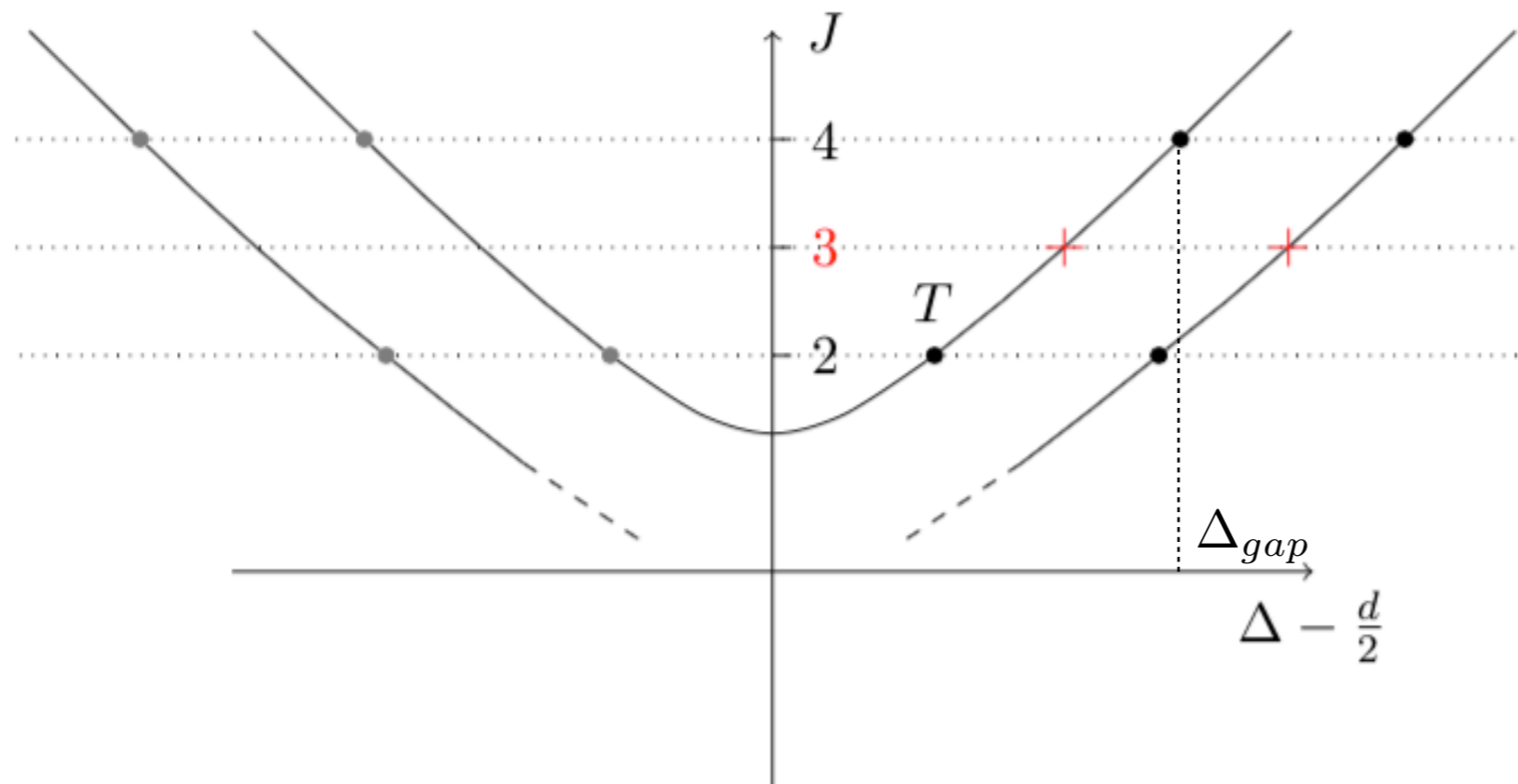
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**Regge intercept  
("Lyapunov exponent")**



$$J'(0) \sim \frac{1}{\Delta_{gap}^2}$$

[Camanho, Edelstein, Maldacena, AZ '14]  
[Costa, Hansen, Penedones '17]  
[Kulaxizi, Parnachev, AZ '17]

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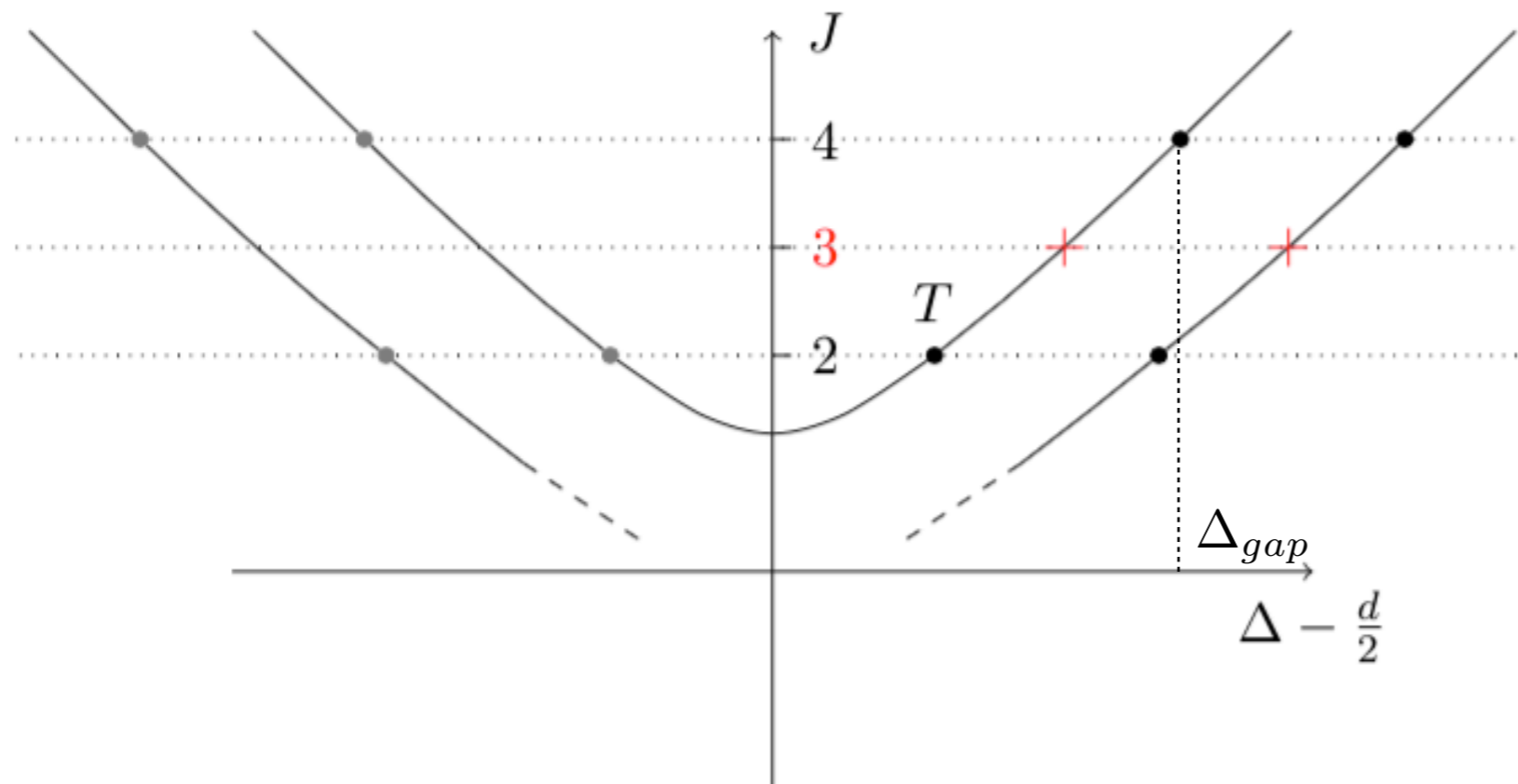
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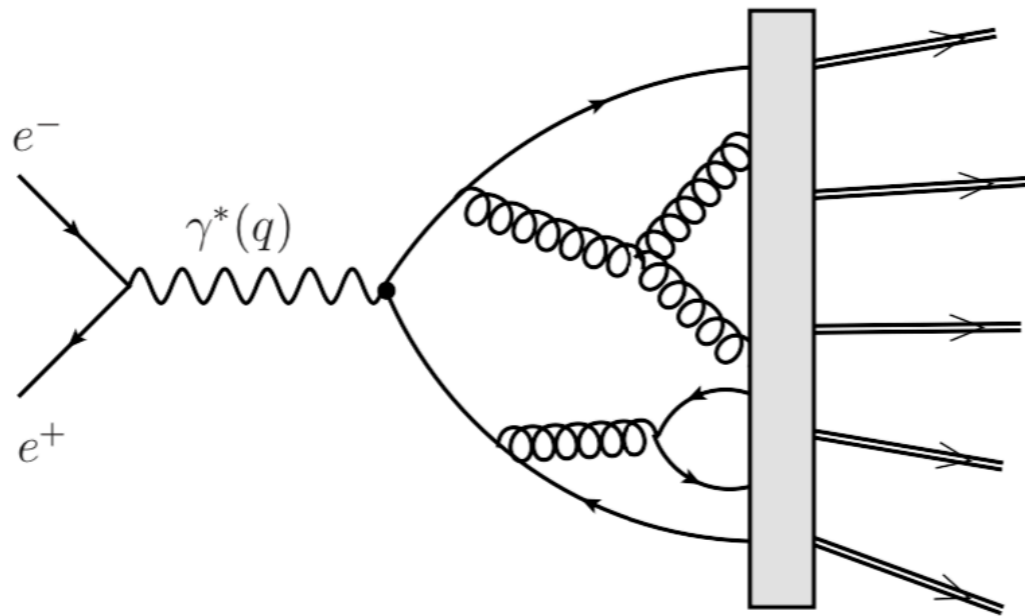
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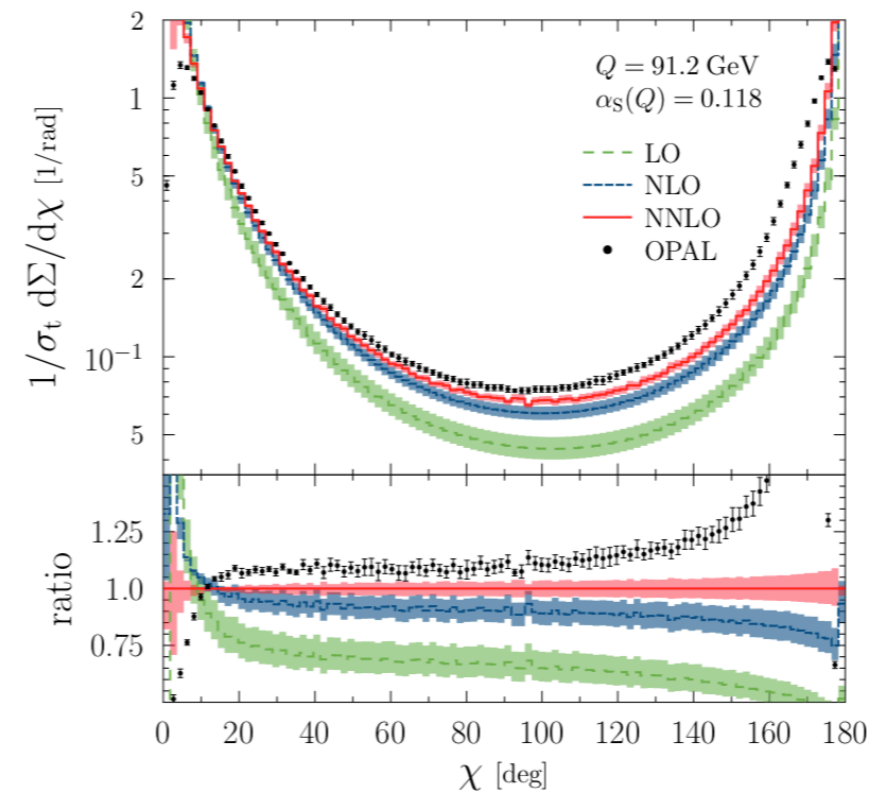
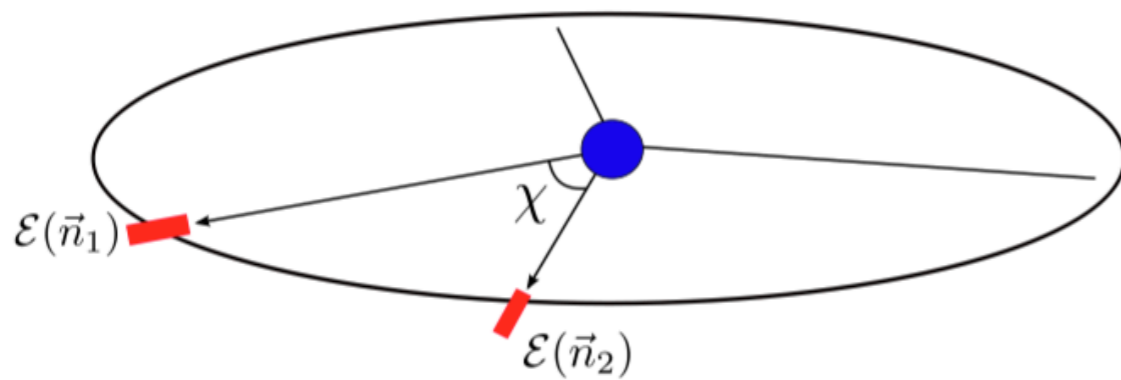
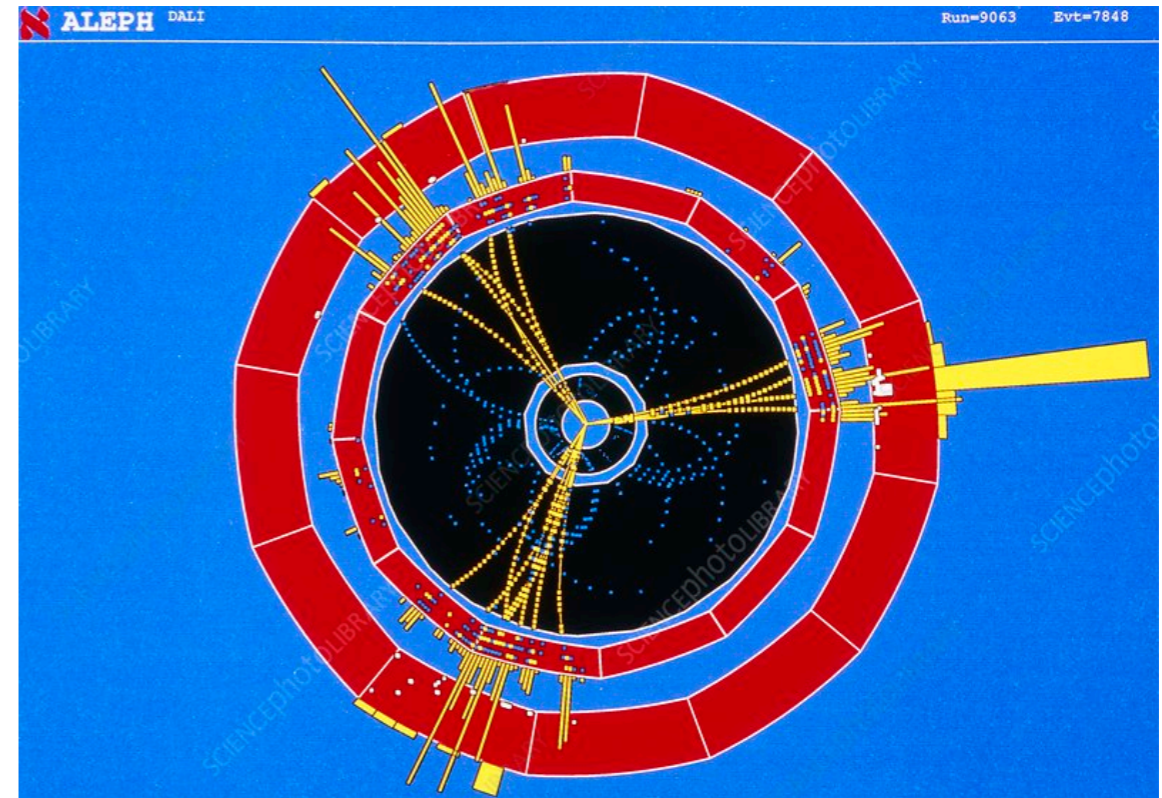
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# Conformal Collider Physics



**very precise experimental data**



[Tulipánt, Kardos, Somogyi '17]



# Conformal Collider Physics

**QCD:**  $\langle \mathcal{E}(\vec{n}_1) \mathcal{E}(\vec{n}_2) \rangle_p = \alpha_s(p) A(\chi) + \alpha_s^2(p) B(\chi) + O(\alpha_s^3)$

**LO**  $\alpha_s(p)$  : [Basham, Brown, Ellis, Love '78]

**NLO**  $\alpha_s^2(p)$  : [Dixon, Luo, Shtabovenko, Yang, Zhu '18]

**40 years!**

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$$\langle \mathcal{E}(\vec{n}_1) \mathcal{E}(\vec{n}_2) \rangle^{\text{QCD}} = \langle \mathcal{E}(\vec{n}_1) \mathcal{E}(\vec{n}_2) \rangle^{\mathcal{N}=4 \text{ SYM}} + \text{“simpler”}$$

[Belitsky, Hohenegger, Korchemsky, Sokatchev, AZ '13]

[Dixon, Moul, Zhu '19] [Korchemsky '19]

**LO+NLO: polylogs**

**NNLO: elliptic integrals!**

[Henn, Sokatchev, Yan, AZ '19]

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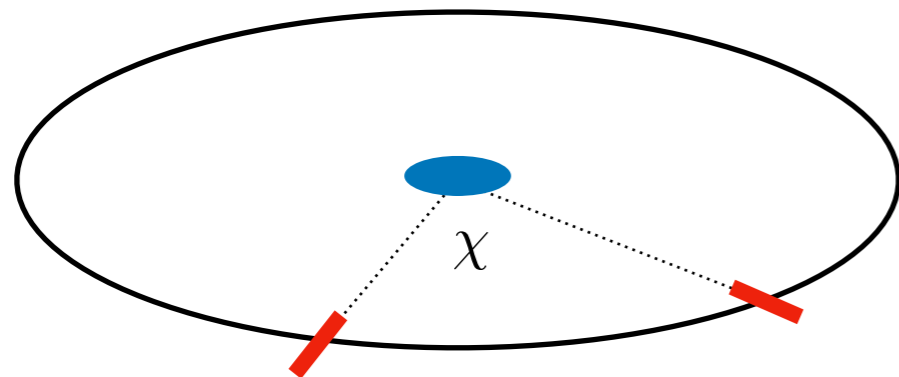
[Sveshnikov, Tkachov 95']

[Korchemsky, Oderda, Sterman 97']

[Hofman, Maldacena 08']

Use correlators instead of amplitudes!

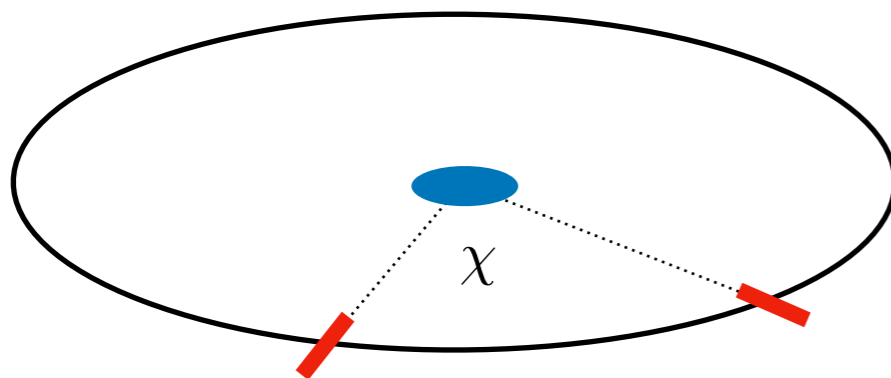
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$$\langle \mathcal{E}(\vec{n}) \rangle = \frac{q^0}{\text{vol}S^{d-2}}$$

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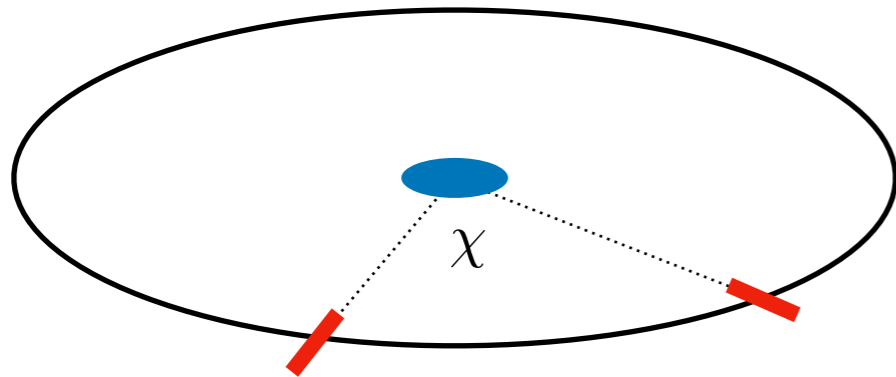
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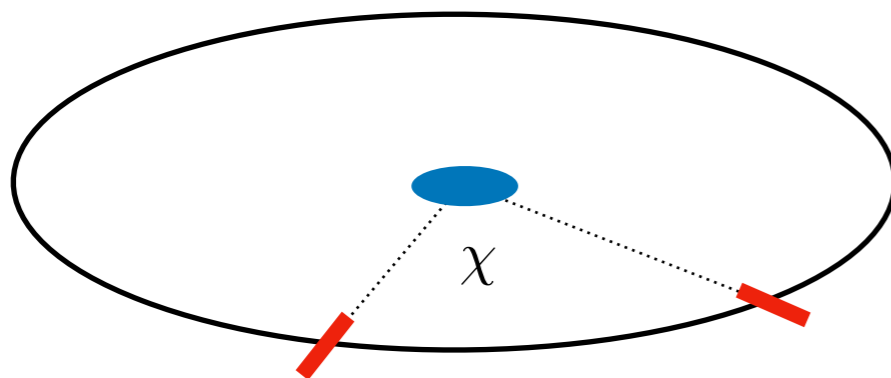
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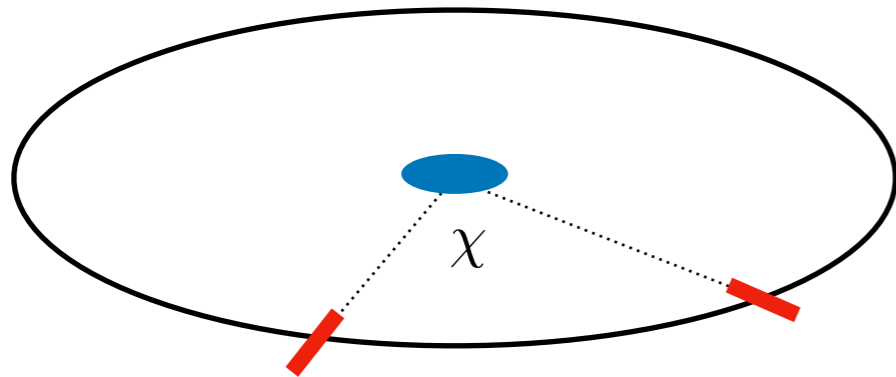
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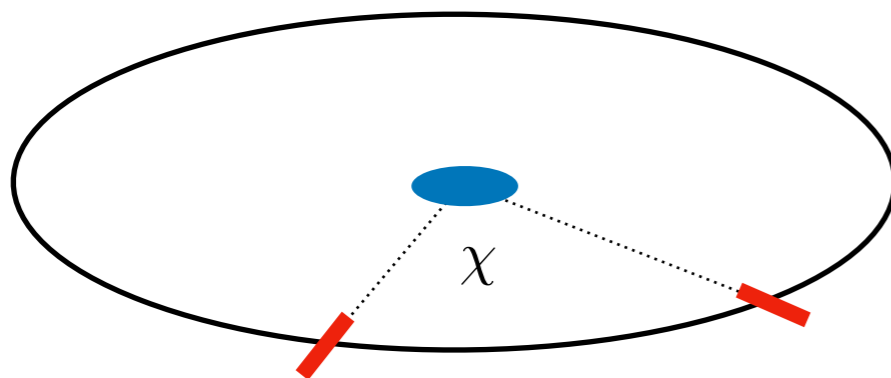
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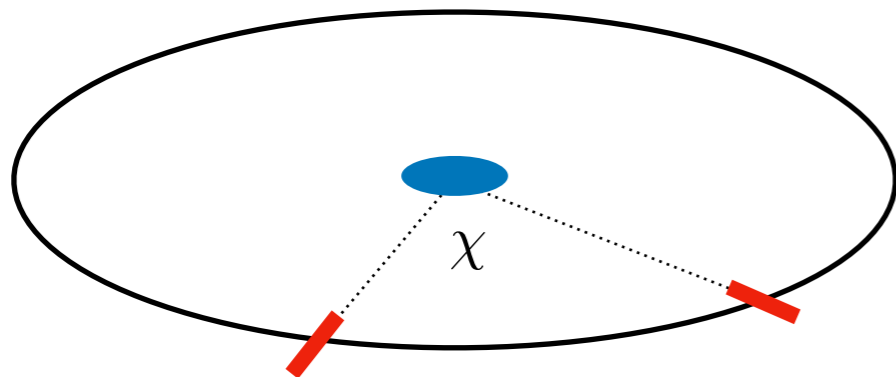
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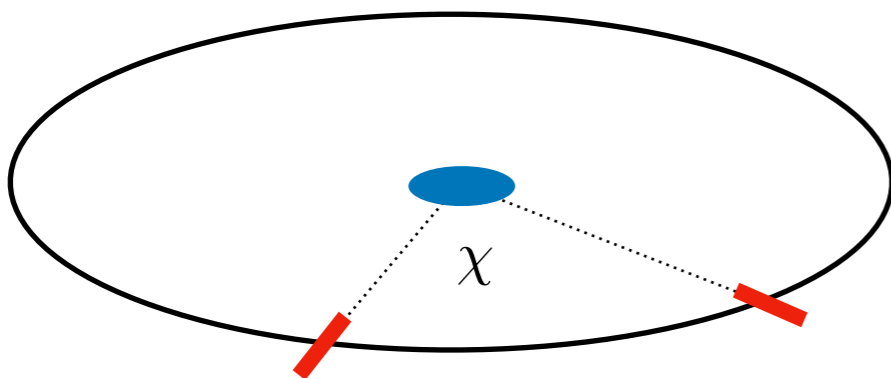
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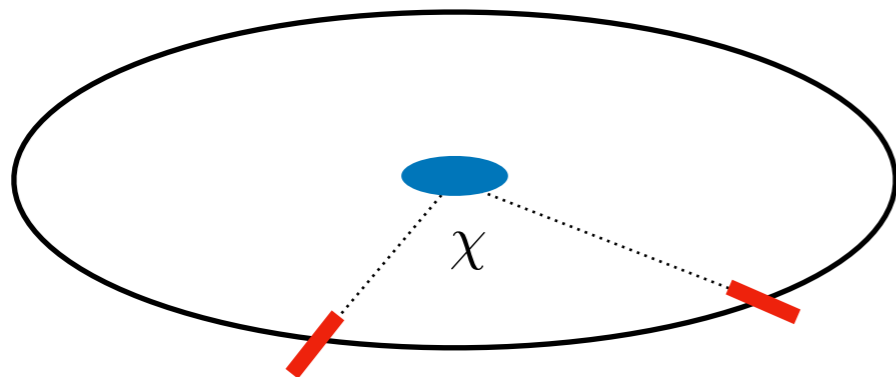
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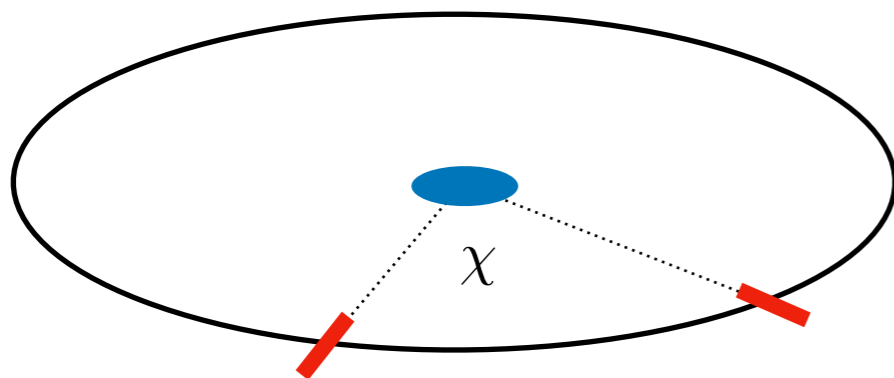
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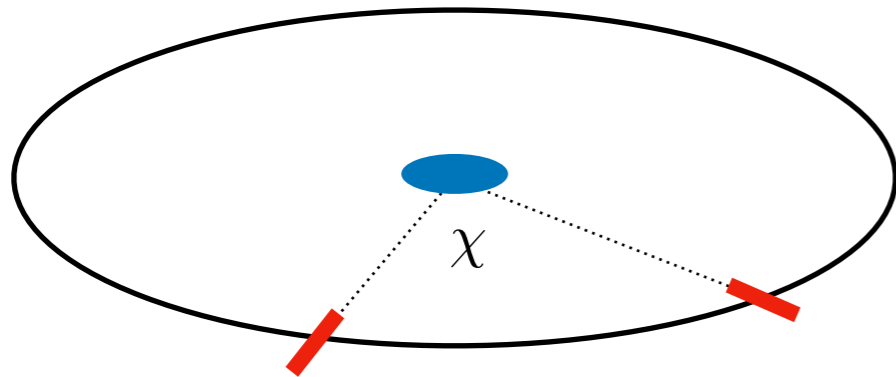
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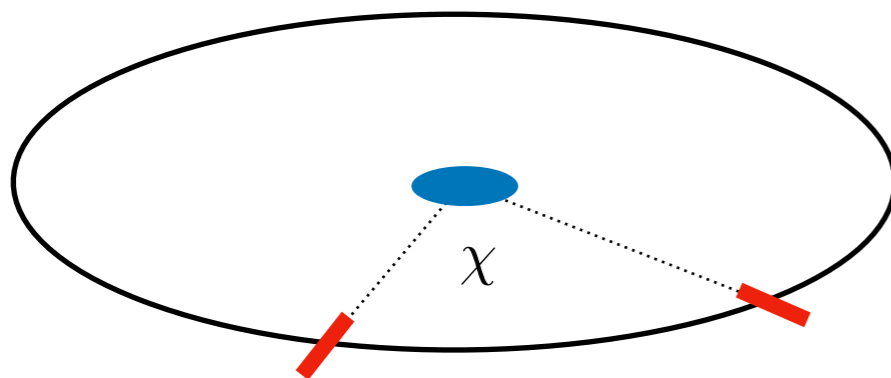
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[Hofman, Maldacena 08']

How do we interpolate between the two pictures?



# Conformal Collider Physics

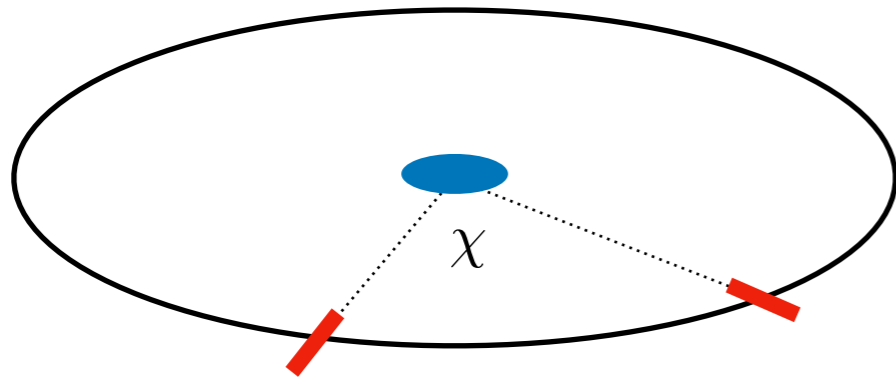
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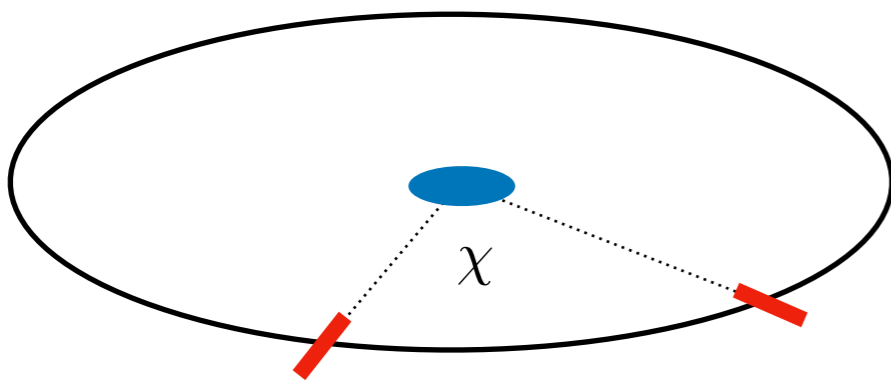
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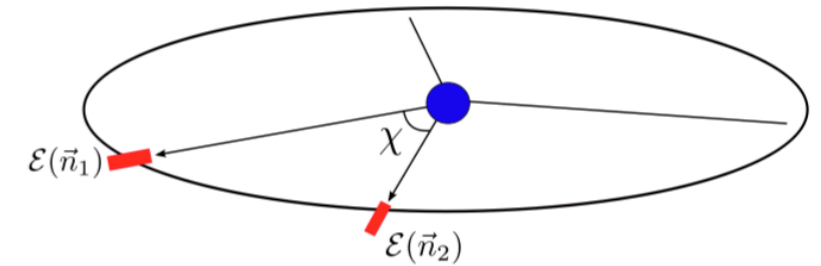
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[Hofman, Maldacena 08']

# Energy Correlators in N=4 SYM

**SUSY:**

$$\langle \mathcal{E}(\vec{n}_1) \mathcal{E}(\vec{n}_2) \rangle \sim \langle \mathcal{O}(\vec{n}_1) \mathcal{O}(\vec{n}_2) \rangle$$



[Belitsky, Hohenegger, Korchemsky, Sokatchev, AZ '13]

**The lightray-lightray OPE (finite coupling):**

$$\langle \mathcal{E}(\vec{n}_1) \mathcal{E}(\vec{n}_2) \rangle = \frac{(p^0)^2}{8\pi^2} \left[ \sum_i p_{\Delta_i} \frac{4\pi^4 \Gamma(\Delta_i - 2)}{\Gamma(\frac{\Delta_i - 1}{2})^3 \Gamma(\frac{3 - \Delta_i}{2})} f_{\Delta_i}^{4,4}(\zeta) + \frac{1}{4} (2\delta(\zeta) - \delta'(\zeta)) \right]$$

$$f_{\Delta}^{\Delta_1, \Delta_2}(\zeta) = \zeta^{\frac{\Delta - \Delta_1 - \Delta_2 + 1}{2}} {}_2F_1 \left( \frac{\Delta - 1 + \Delta_1 - \Delta_2}{2}, \frac{\Delta - 1 - \Delta_1 + \Delta_2}{2}, \Delta + 1 - \frac{d}{2}, \zeta \right)$$

- Sum is over Regge trajectories
- OPE data is evaluated at  $\mathbf{J}=-1$  ( $p_{\Delta_i}$ )
- Correctly captures contact terms (cf. QNEC saturation)
- Passes many perturbative tests and leads to new predictions

$$\zeta = \frac{1 - \cos \chi}{2}$$

**conformal WI:**

$$\int_0^1 d\zeta \langle \mathcal{E} \mathcal{E} \rangle = 1$$

$$\int_0^1 d\zeta (2\zeta - 1) \langle \mathcal{E} \mathcal{E} \rangle = 0$$

# Jets at Finite Coupling in N=4 SYM

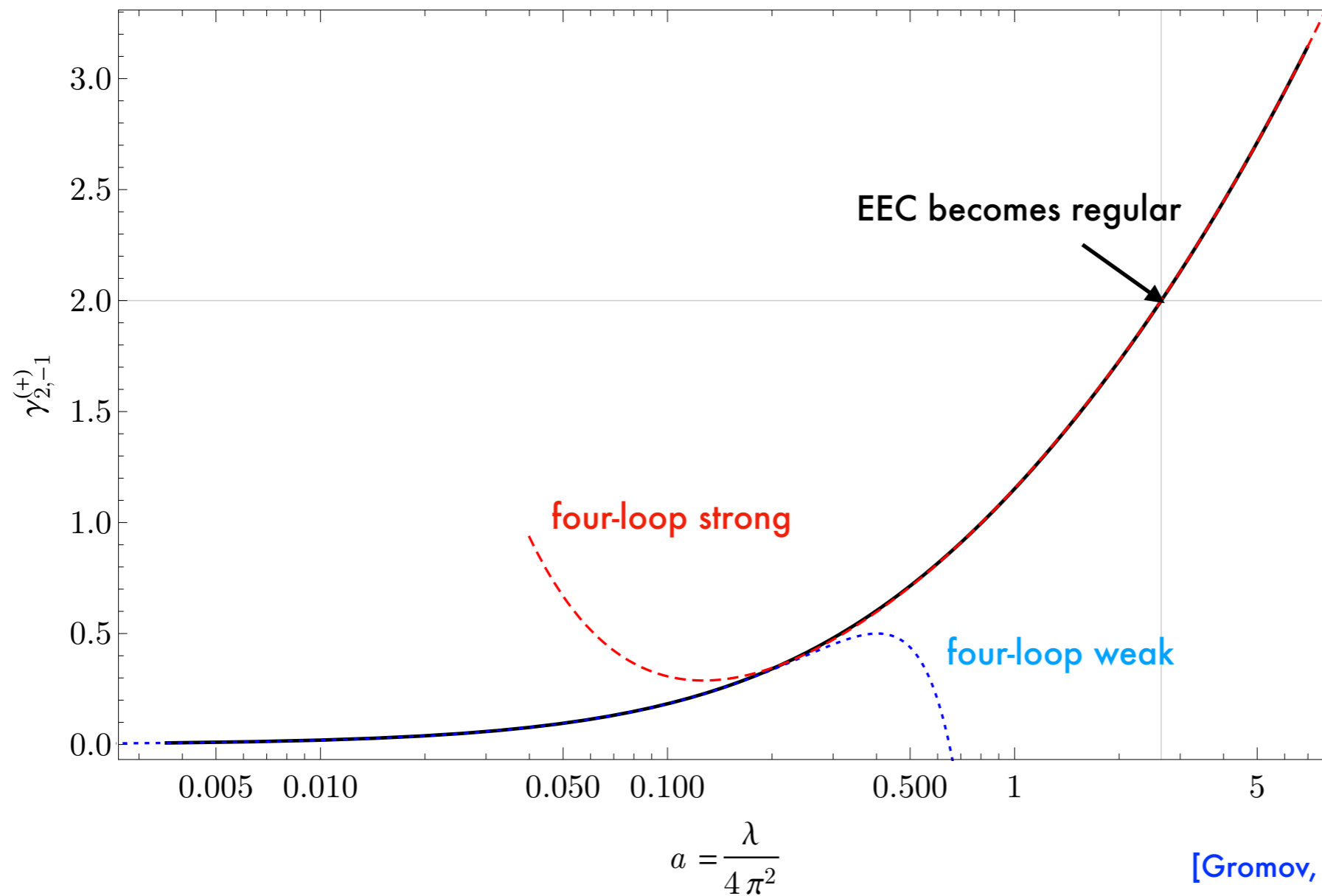
$$\langle \mathcal{E}(\theta) \mathcal{E}(0) \rangle \sim \frac{1}{\theta^2 \left(1 - \frac{\gamma_{2,-1}^+}{2}\right)}$$

[Hofman, Maldacena 08']

[Korchemsky 19']

[Dixon, Moul, Zhu 19']

**integrability:**



[plot by N.Gromov]

[Gromov, Levkovich-Maslyuk, Sizov 15']

[Gromov, Kazakov, Leurent, Volin 13']

# Further Directions

Lorentzian methods/observables:

- superconvergence (dS/flat/AdS, quantum)

$$[\mathcal{E}(\vec{n}_1), \mathcal{E}(\vec{n}_2)] = 0$$

- positivity of the ANEC two-point function constraint

$$\langle \mathcal{O} | \mathcal{E}(\vec{n}_1) \mathcal{E}(\vec{n}_2) | \mathcal{O} \rangle \geq 0$$

- multi-point event shapes, celestial bootstrap, more general lightrays

$$\langle \Psi | \mathcal{E}(\vec{n}_1) \mathcal{E}(\vec{n}_2) \mathcal{E}(\vec{n}_3) \mathcal{E}(\vec{n}_4) | \Psi \rangle$$

- event shapes in QFTs (numerics, effects of beta-function)

[Dixon, Moul, Zhu '19]

- shockwave amplitudes (OPE for amplitudes, CFT S-matrix, soft limits)

# Open Questions

How to efficiently combine Lorentzian methods with numerics?

Is it possible to measure event shapes in a lab?

**coarse-grained holography bootstrap challenge:**

With more efforts we can hopefully derive the rules of AdS EFT.  
(flat space mini-challenge: UV complete  $R^3$ )

**fine-grained holography bootstrap challenge:**

How hard it is to UV complete a given AdS EFT?

Can we exclude some theories which look like perfect AdS EFTs?

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**Thank you!**

# Four-loop Prediction in N=4 SYM

[Korchensky '19]

[Kologlu, Kravchuk, Simmons-Duffin, AZ '19]

To be concrete:

$$\begin{aligned}
 \mathcal{F}_{\mathcal{E}}^{(4),\text{pl}}(\zeta) &= c_0^{(4)} \delta(\zeta) + \frac{1}{24} \left[ \frac{\log^3 \zeta}{\zeta} \right]_0 + \left( -\frac{7}{8} + \frac{1}{16} \pi^2 - \frac{3}{16} \zeta_3 \right) \left[ \frac{\log^2 \zeta}{\zeta} \right]_0 \\
 &+ \frac{1}{4} \left( 31 - \frac{17}{6} \pi^2 + \frac{1}{15} \pi^4 - \frac{1}{6} \pi^2 \zeta_3 + \frac{1}{4} \zeta_3^2 + 3\zeta_5 \right) \left[ \frac{\log \zeta}{\zeta} \right]_0 \\
 &+ \frac{1}{4} \left( -111 + \frac{65}{6} \pi^2 - \frac{3}{16} \pi^4 - \frac{389}{30240} \pi^6 + 10\zeta_3 - 2\pi^2 \zeta_3 - \frac{3}{160} \pi^4 \zeta_3 + 3\zeta_3^2 + 20\zeta_5 + \frac{1}{12} \pi^2 \zeta_5 - \frac{69}{16} \zeta_7 \right) \left[ \frac{1}{\zeta} \right]_0 \\
 &+ c_1^{(4)} \delta(y) + \frac{1}{192} \left[ \frac{\log^7 y}{y} \right]_1 + \frac{5}{384} \pi^2 \left[ \frac{\log^5 y}{y} \right]_1 + \frac{95}{192} \zeta_3 \left[ \frac{\log^4 y}{y} \right]_1 + \frac{29}{1920} \pi^4 \left[ \frac{\log^3 y}{y} \right]_1 \\
 &+ \left( \frac{67}{192} \pi^2 \zeta_3 + \frac{69}{16} \zeta_5 \right) \left[ \frac{\log^2 y}{y} \right]_1 + \left( \frac{367}{48384} \pi^4 + \frac{97}{32} \zeta_3^2 \right) \left[ \frac{\log y}{y} \right]_1 \\
 &+ \left( \frac{187}{5760} \pi^4 \zeta_3 + \frac{95}{192} \pi^2 \zeta_5 + \frac{785}{128} \zeta_7 \right) \left[ \frac{1}{y} \right]_1 + \mathcal{F}_{\mathcal{E}}^{(4),\text{reg}}(\zeta)
 \end{aligned}$$

$$y = 1 - \zeta$$

# Commutativity of light-ray operators

The product of the light-ray operators  $\mathbf{L}[\mathcal{O}_{J_1}](x, z_1)\mathbf{L}[\mathcal{O}_{J_2}](x, z_2)$  is well-defined and commutative **if and only if** \*

$$J_1 + J_2 > \max(2 - \Delta'_0, 1 + J_0)$$

$$J_1 + J_2 > 2 - \tau'_0 + |\Delta_1 - \Delta_2|$$

where

$$\Delta'_0, \tau'_0 \geq \frac{d-2}{2}$$

are smallest non-zero twist and dimension in the OPE of

$$\mathcal{O}_{J_1} \times \mathcal{O}_{J_2}$$

\* assuming the asymptotic light-cone expansion



# CFT Light-Ray Operators

Start with a bi-local object

$$\mathbb{O}_{\Delta, J}^{\pm}(x, z) = \int d^d x_1 d^d x_2 K_{\Delta, J}^{\pm}(x_1, x_2, x, z) \phi_1(x_1) \phi_2(x_2).$$

The kernel is obtained by Wick-rotating and light-transforming the partial wave expansion.

The **residues** are light-ray operators:

$$\mathbb{O}_{\Delta, J}^{\pm}(x, z) \sim \frac{1}{\Delta - \Delta_i^{\pm}(J)} \mathbb{O}_{i, J}^{\pm}(x, z)$$

# Spin Selection Rule

Consider the small separation limit between two light-ray operators

$$\lim_{z_1 \cdot z_2 \rightarrow 0} \mathbf{L}[\mathcal{O}_1](x, z_1) \mathbf{L}[\mathcal{O}_2](x, z_2) = \sum_i (z_1 \cdot z_2)^{\delta_i} \mathbb{O}_{\delta_i, J}(x, z_2)$$

Analogy

$$\mathcal{O}_{\Delta_1}(x) \mathcal{O}_{\Delta_2}(x) = \sum_i \mathcal{O}_{\Delta_1 + \Delta_2}^i(x)$$

This leads to the spin selection rule

[Hofman, Maldacena 08']

$$(J - 1) = (J_1 - 1) + (J_2 - 1) \Rightarrow J = J_1 + J_2 - 1$$

$$\int_{-\infty}^{\infty} dx_1^- T_{--}(x_1^-, x_1^+, \vec{x}_1) \int_{-\infty}^{\infty} dx_2^- T_{--}(x_2^-, x_2^+, \vec{x}_2) = \sum_i \int dx^- \mathcal{O}_{---}$$

# Signature of Light-ray Operators

Analytic continuation in spin is performed separately from even spins (signature +) and from odd spins (signature -).

One way to state this is to consider CRT transformation

$$\text{CRT} : (u, v, \vec{y}) \rightarrow (-u, -v, \vec{y})$$

$$\left( (\text{CRT}) \int_{-\infty}^{\infty} dv \mathcal{O}_{i;v\dots v}(0, v, \vec{y}) (\text{CRT})^{-1} \right)^\dagger = (-1)^{J_i} \int_{-\infty}^{\infty} dv \mathcal{O}_{i;v\dots v}(0, v, \vec{y})$$

The same continues for the non-local operators

$$\left( (\text{CRT}) \mathbb{O}_{\Delta, J}^\pm(x, z) (\text{CRT})^{-1} \right)^\dagger = \pm \mathbb{O}_{\Delta, J}^\pm(x, z)$$

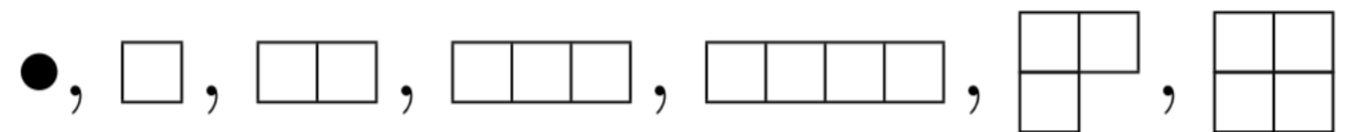
# Transverse Representations

Naively, one would think that light-ray operators transforming in the arbitrary representations of the transverse  $SO(d-2)$  can appear in the OPE.

**Rule:** For the OPE  $\int dv_1 \mathcal{O}_1 \times \int dv_2 \mathcal{O}_2$

1. List all  $SO(d-1,1)$  representations in the OPE  $\mathcal{O}_1 \times \mathcal{O}_2$
2. Remove first row in the corresponding Young diagram

ANEC  $\times$  ANEC



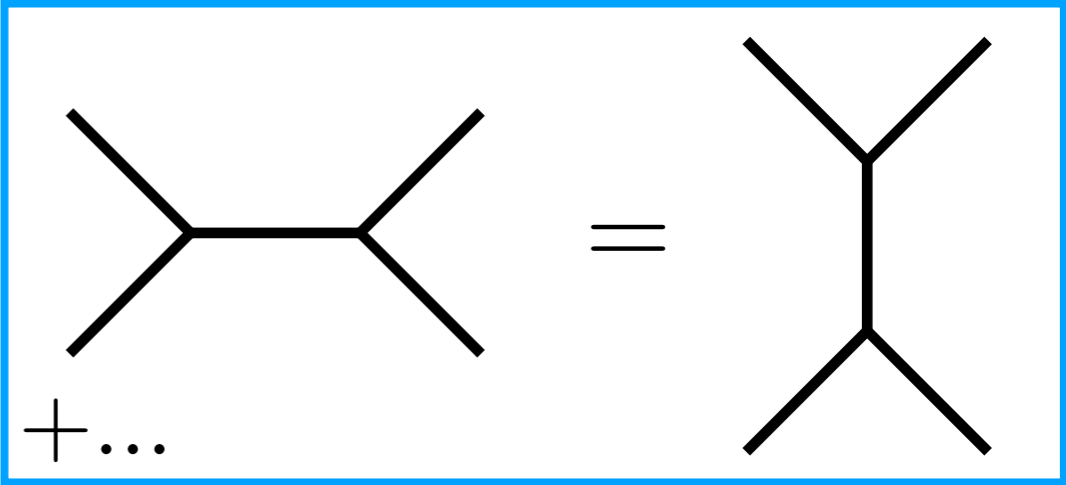
# Flat Space and AdS/dS Bulk

CFT	S-matrix (AdS/dS)
light-ray operator	<p><b>shockwave state</b> (on-shell state in the mixed signature)</p> $p^\mu = (0, p^v, \vec{q}), \quad \vec{q}^2 = 0$
ANEC operator	<b>gravitational shock</b>
event shapes	<p><b>scattering amplitudes</b> (in mixed signature)</p>
bound on Regge	<p><b>bound on Regge</b> (causality)</p> $\lim_{s \rightarrow \infty} \mathcal{A}(s, t) < s^2, \quad t < 0$
commutativity of ANECs	<p><b>superconvergence</b></p> $\int dt \text{Disc}_t A(s, t) = 0$ <p>[Alfaro, Fubini, Rossetti, Furlan 66']</p>
light-ray OPE	<b>amplitude OPE?</b> (worldsheet OPE in string theory)

# Holographic CFTs

$$\frac{1}{l_{Pl}^{D-2}} \int d^D x \sqrt{-g} (R - 2\Lambda + \dots)$$

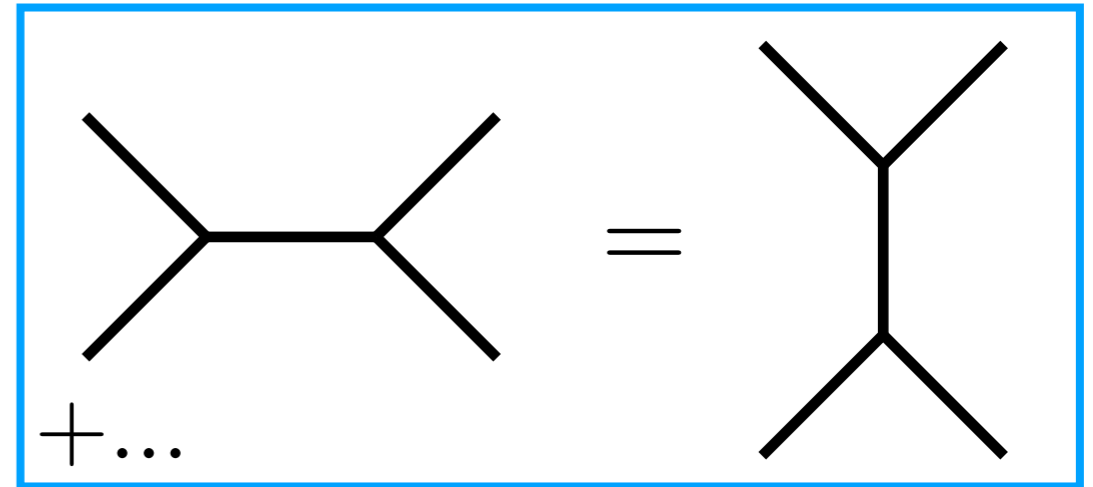
**AdS/CFT**



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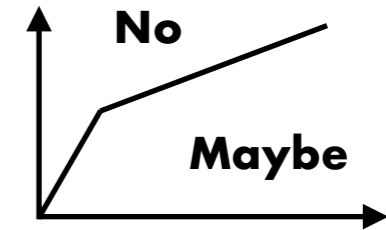
Tentative  
CFT data



NO



MAYBE

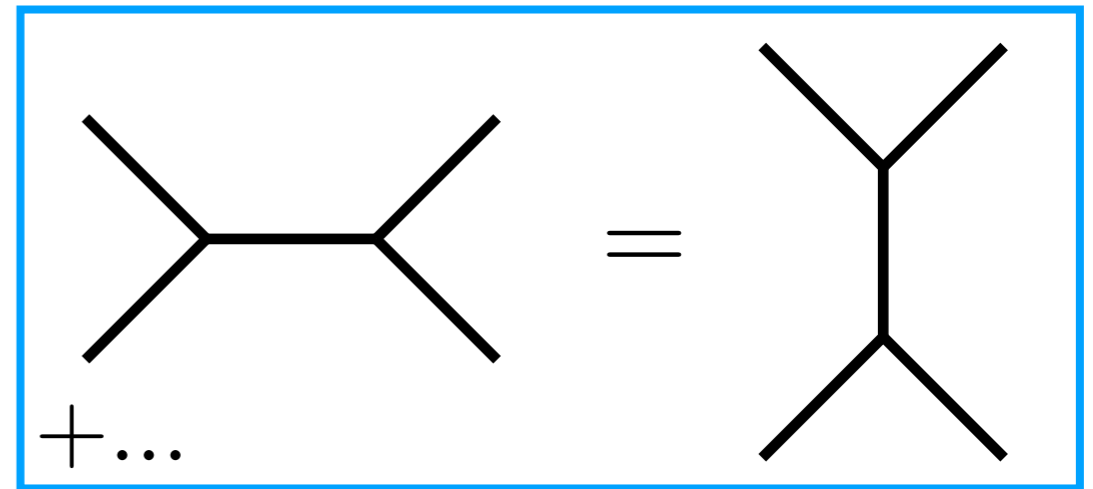


[Rattazzi, Rychkov, Tonni, Vichi '08]

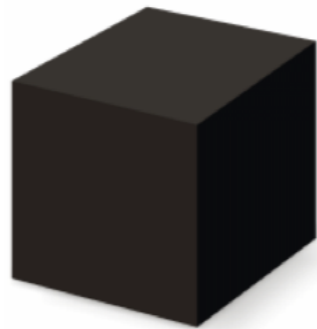
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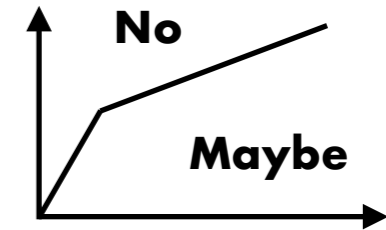


NO



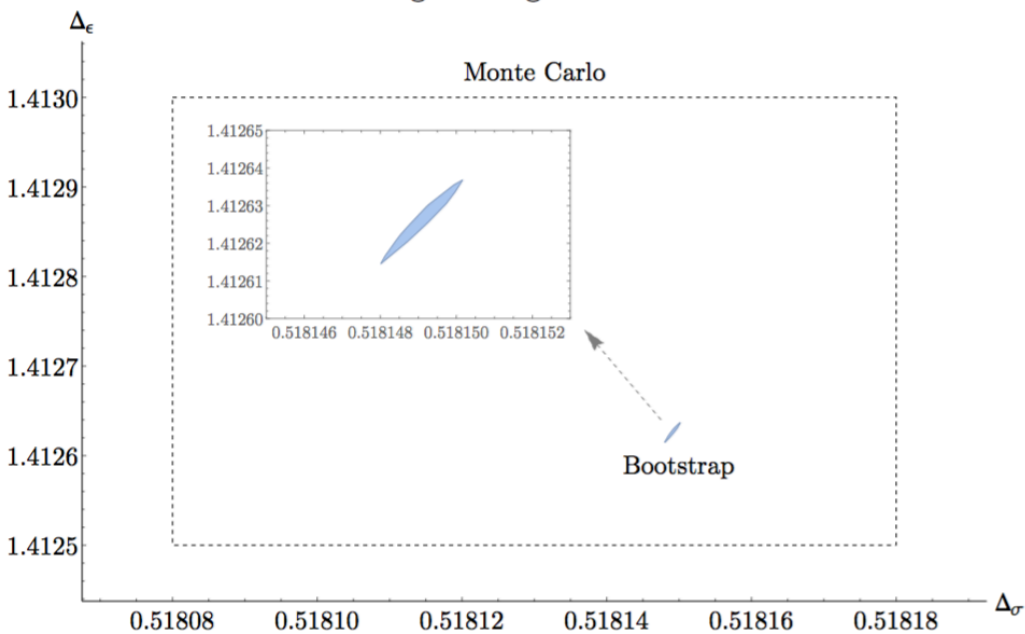
MAYBE

“YES”!



[Rattazzi, Rychkov, Tonni, Vichi '08]

Ising: Scaling Dimensions



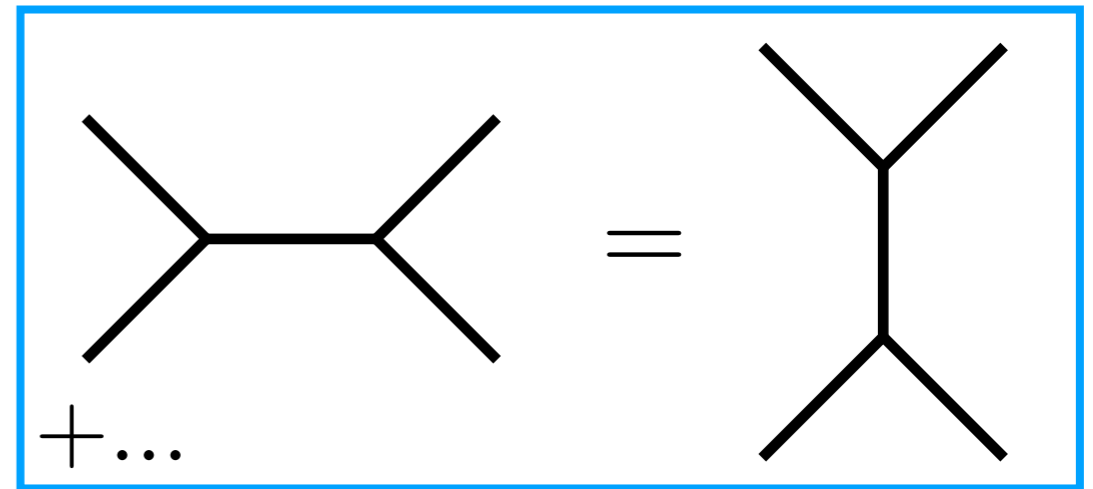
[Kos, Poland, Simmons-Duffin, Vichi '16]



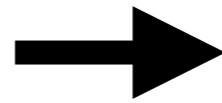
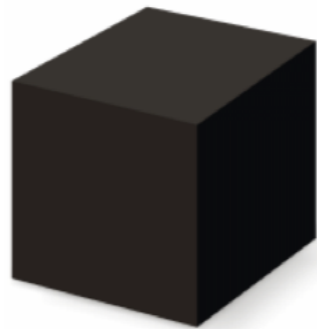
# Holographic CFTs

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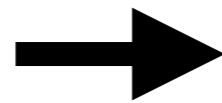
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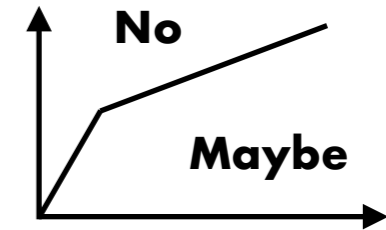


NO



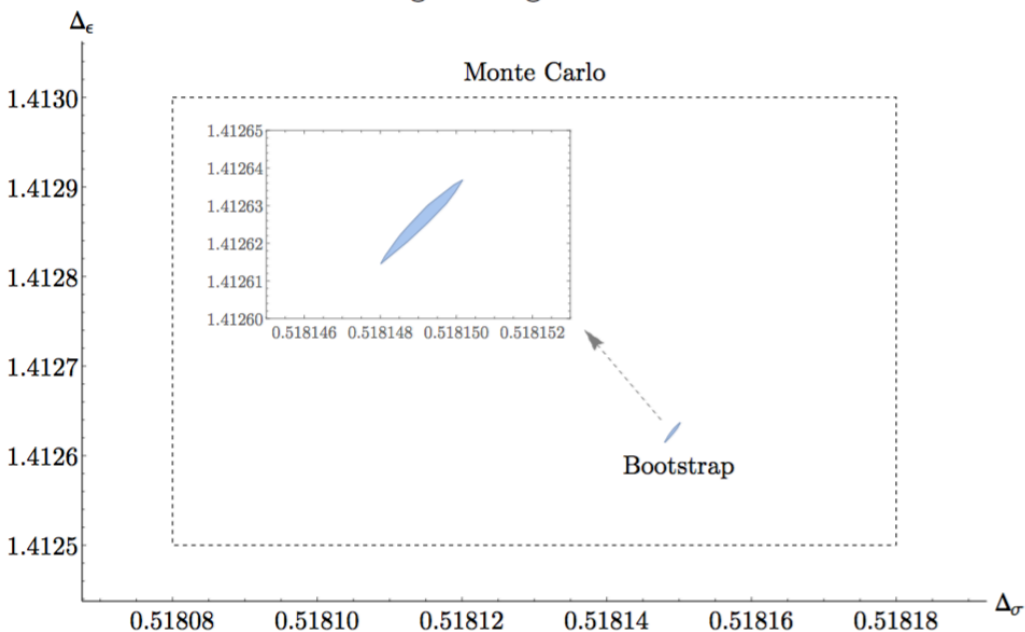
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Ising: Scaling Dimensions



[Kos, Poland, Simmons-Duffin, Vichi '16]

AdS/CFT

**HPPS: any consistent EFT in AdS looks OK!**

[Heemskerk, Penedones, Polchinski, Sully '09]

**fine-grained holography: landscape vs. swampland**  
(hard)

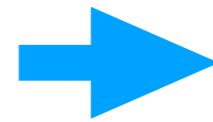
**coarse-grained holography: assume landscape**  
derive the rules of consistent AdS EFTs

(“easy”)

## AdS EFT (“easy”)

$$\frac{1}{l_{Pl}^{D-2}} \int d^D x \sqrt{-g} \left( R - 2\Lambda + \frac{c_2}{M^2} R^2 + \dots \right)$$

**HPPS conjecture:** large  $N$  + large gap

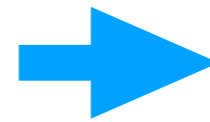


$$\begin{array}{l} M \text{ - string scale} \\ c_2 = O(1) \end{array}$$

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**Causality:**

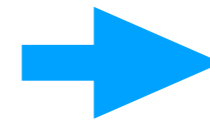
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- non-minimal couplings should timely Reggeize  
(extra HS DoF are needed)

[Camanho, Edelstein, Maldacena, AZ '14]

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(squiggly line curse)

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**Bound on Pomeron couplings:**

$$C_{TTJ}^{R^2}(\nu) = O(\nu^2)$$

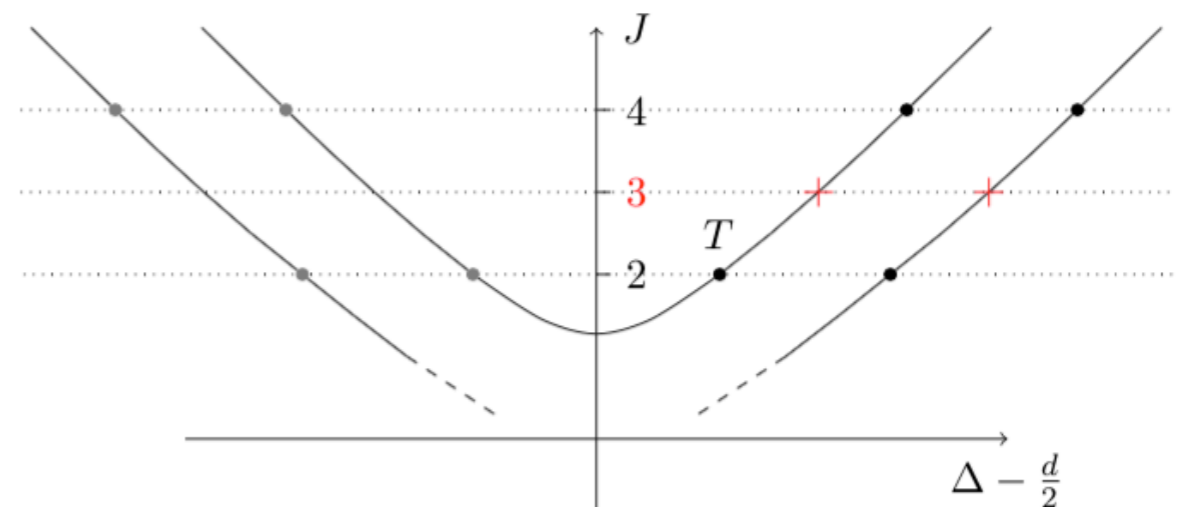
$$C_{TTJ}^{R^3}(\nu) = O(\nu^4)$$

(non-minimal TT-pomeron coupling)

from unitarity

[Costa, Hansen, Penedones '17]

[Kulaxizi, Parnachev, AZ '17]



$$T : \nu = i d/2$$